

Exploring the Origin of Thick Disks Using the NewHorizon and Galactica Simulations

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Abstract

Ever since a thick disk was proposed to explain the vertical distribution of the Milky Way disk stars, its origin has been a recurrent question. We aim to answer this question by inspecting 19 disk galaxies with stellar mass greater than $10^{10} M_{\odot}$ in recent cosmological high-resolution zoom-in simulations: GALACTICA and NEWHORIZON. The thin and thick disks are reasonably reproduced by the simulations with scale heights and luminosity ratios as observed. We then spatially classify the thin and thick disks and find that the thick disk stars are older, metalpoorer, kinematically hotter, and higher in accreted star fraction, while both disks are dominated by the stars formed in situ. Half of the in situ stars in the thick disks are formed before the galaxies develop their disks, and the rest are formed in spatially and kinematically thinner disks and then thickened with time by heating. However, the 19 galaxies have various properties and evolutionary routes, highlighting the need for statistically large samples to draw general conclusions. We conclude from our simulations that the thin and thick disk components are not entirely distinct in terms of formation processes but rather markers of the evolution of galactic disks. Moreover, as the combined result of the thickening of the existing disk stars and the continued formation of young thin disk stars, the vertical distribution of stars does not change much after the disks settle, pointing to the modulation of both orbital diffusion and star formation by the same confounding factor: the proximity of galaxies to marginal stability.

Unified Astronomy Thesaurus concepts: Galaxy formation (595)

1. Introduction

The idea of the two-component disk structure for the Milky Way (MW) was first proposed by Gilmore & Reid (1983) to explain the vertical distribution of disk stars. They measured the number density of resolved stars in the solar neighborhood and found that the vertical structure of the MW disk is well described by a double exponential profile: the thin disk with a scale height of \sim 300 pc and the thick disk with a scale height of \sim 1450 pc (see also Ivezić et al. 2008; Juric et al. 2008). The level of contribution from thick disk stars to the solar neighborhood is suggested to be $\sim 10\%$ (e.g., Bland-Hawthorn & Gerhard 2016).

Galactic spectroscopic surveys such as Gaia-ESO (Gilmore et al. 2012), SEGUE (Yanny et al. 2009), GALAH (De Silva et al. 2015), and APOGEE (Majewski et al. 2017) have provided the metallicity information for a large number of disk stars. The vertical gradient of alpha abundance and metallicity (e.g., Hayden et al. 2014) has indicated that the thick disk consists of alpha-enhanced and metal-poorer populations (e.g., Bland-Hawthorn & Gerhard 2016). Indeed, in many studies, two chemically distinct sequences are thought to be separated in the plane of [Fe/H] and $\left[\alpha/\text{Fe}\right]$, which further supported the idea of two-component disks (e.g., Lee et al. 2011; Anders et al. 2014; Bensby et al. 2014; Duong et al. 2018; Mackereth et al. 2019). These two sequences exhibit different spatial distributions and kinematic properties; the alpha-rich metalpoor sequence tends to have a shorter scale length, larger scale height, and slower rotational velocity than the alpha-poor sequence. On the other hand, some studies found that disk stars of varying chemical abundance show gradually varying thickness, arguing against the presence of two distinct disk structures (e.g., Bovy et al. 2012). Therefore, it remains uncertain whether the thick disk is truly a distinct component with a different origin.

Thick disk studies have been conducted on other galaxies as well. Due to observational limitations, it has been possible only in a few nearby edge-on spiral galaxies to resolve individual disk stars and measure the vertical number density (e.g., Seth et al. 2005). Hence, most studies were based on the vertical brightness profile. For example, Yoachim & Dalcanton (2006) measured the vertical profiles of 34 edge-on disk galaxies with a wide range of stellar mass. They found that the luminosity ratio between the thin and thick disks, $L_{\text{thick}}/L_{\text{thin}}$, depends on the galaxy stellar mass; thin disks contribute more to the total disk luminosity in more massive galaxies, while the luminosity of thick disks is almost comparable to that of the thin disk in low-mass galaxies (see also Comerón et al. 2011, 2014; Martínez-Lombilla & Knapen 2019). The kinematics and stellar population properties of the two disks have been studied only for a small number of galaxies through spectroscopy of the thin disk (close to the galactic midplane) and thick disk regions (typically a few kiloparsecs away from the midplane;

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e.g., Yoachim & Dalcanton 2008; Comerón et al. 2019; Pinna et al. 2019a; Kasparova et al. 2020). They have confirmed that thick disks are, in general, older, relatively metal ([Fe/H])-poorer, and alpha-enhanced.

Theoretically, several scenarios have been proposed to illustrate the formation of thick disks. One of the scenarios is the kinematic heating (thickening) of a preexisting thin disk caused by several possible sources, including minor mergers (e.g., Quinn et al. 1993; Kazantzidis et al. 2008; Villalobos & Helmi 2008), spiral and barred structures (e.g., Sellwood & Carlberg 1984; Saha et al. 2010; Grand et al. 2016), giant molecular clouds (e.g., Spitzer & Schwarzschild 1951; Aumer et al. 2016), and stellar clumps (e.g., Bournaud et al. 2009; Silva et al. 2021). Also, orbital diffusion (radial migration) has been suggested as a possible mechanism to form a thick disk (e.g., Roškar et al. 2008; Schönrich & Binney 2009; Loebman et al. 2011; Fouvry et al. 2017; Halle et al. 2018); stars migrating outward due to the interaction with spiral arms also drift further away from the midplane as well. Recently, Sharma et al. (2020) showed from their chemodynamical model of the MW that radial migration is essential for forming both alphaenhanced and alpha-poor sequences. They concluded that their model does not require a "distinct" thick component, as both sequences are formed in a "continuous" star formation and evolution history of the MW.

In addition to triggering disk heating (e.g., Helmi et al. 2018), mergers are also believed to play an important role in forming thick disks in several ways. For example, Abadi et al. (2003) suggested, based on a simulated galaxy, that the thick disk could be formed by accretion of the stars (formed ex situ) from disrupted satellite galaxies (see also Gilmore et al. 2002; Wyse et al. 2006). Also, several studies using simulations have claimed that gas-rich mergers can induce starbursts in the main galaxies and that many of the thick disk stars are formed in situ during these chaotic merger events (e.g., Brook et al. 2004, 2012; Grand et al. 2020). Based on four MW-mass simulated galaxies, Buck (2020) supported the idea that gasrich mergers result in chemical bimodality of disk stars, but they found that the low-alpha sequence is formed as a result of metal-poor gas-rich mergers that dilute the interstellar medium (see also Bonaca et al. 2020). Most recently, Agertz et al. (2020) found in their one MW-mass simulated galaxy that an alpha-poor sequence started forming after the last major merger and the subsequent formation of an outer metal-poor gas disk (see also Renaud et al. 2020). Thus, they concluded that the two alpha sequences (alpha-enhanced/alpha-poor) are formed during different (merger-dominated/quiescent) growth phases of the galaxy; thus, this transition of the growth phases is the key to creating the bimodal distribution of the stars in the chemical plane. Contrary to this sequential formation of the thin and thick disks, however, some studies proposed a coformation scenario of the thin and thick disks. For example, based on the kinematic and chemical properties of old disk stars in the solar neighborhood, Silva et al. (2021) claimed that both thin and thick disks started to form early, which can be explained by a scenario in which a thick disk is formed by scattering by clumps.

Recent studies using cosmological hydrodynamic simulations have further elaborated on the origin of the thin and thick disks. The overall picture of disk evolution described by many cosmological galaxy simulations is the "inside-out" and "upside-down" formation; when stellar particles in the simulated galaxies are divided into coeval populations, older cohorts have larger scale heights and shorter scale lengths (e.g., Stinson et al. 2013; Martig et al. 2014a; Minchev et al. 2015). In this framework, the two-stage formation of the thick disk is expected (e.g., Ma et al. 2017; Buck et al. 2020); stars formed earlier are born with thicker distributions (e.g., Bird et al. 2013, 2020; Grand et al. 2016), as they are formed out of more turbulent gas at higher redshifts (e.g., Bournaud et al. 2009; Forbes et al. 2012). Subsequently, gradual kinematic heating of the later-formed thinner disk contributes to the growth of the thick disk (e.g., Martig et al. 2014b). Based on the vertical profiles of the mono-age stellar populations in the simulated galaxies, Buck et al. (2020) showed that the thick disk is not a distinct component; rather, the double-component vertical structure can be understood as a gradually varying mixture of young and old stars with vertical height from the galactic plane.

This study aims to explore whether the spatially defined thin and thick disks are distinct components formed by different mechanisms. We use 18 disk galaxies from the NEWHORIZON (NH) simulation that reached z = 0.3 (Dubois et al. 2020) and one disk galaxy at z = 0 from the GALACTICA simulation (S. Peirani et al. 2021, in preparation). These simulations have relatively high spatial and mass resolutions compared to other present-day simulations and thus are ideal to study the disk structure of galaxies. Furthermore, the up-to-date baryonic physical prescriptions including the supernova (SN) and active galactic nucleus (AGN) feedback have been implemented in both simulations. Since these simulations did not trace the alpha element separately from the total metallicity, this study focuses on the spatially defined thin and thick disks.

The paper is organized as follows. Section 2 describes the two simulations and the sample galaxies used in this study. In Section 3.1, we first apply the conventionally accepted doublecomponent fitting to the vertical profiles of galaxies and check if the simulations reproduce the observed properties of the two disks. In Section 3.2, we separate the thin and thick disks geometrically based on the vertical profiles and compare them in terms of ex situ contribution, age, metallicity (Section 3.2.1), kinematics (Section 3.2.2), and properties at birth (Section 3.2.3). In Section 4, we divide the stellar particles formed in situ into mono-age groups and trace the vertical distribution of each mono-age group with time in order to understand how the two disks can be interpreted in terms of disk evolution. In Section 5, we conclude that the two disks are not entirely distinct in terms of formation mechanisms; instead, they are the results of how galactic disks develop and evolve with time.

2. Methodology

2.1. Simulations: NH and Galactica

The NH (Dubois et al. 2020) and GALACTICA (S. Peirani et al. 2021, in preparation) simulations are both high-resolution cosmological hydrodynamic zoom-in simulations from the larger volume of the Horizon-AGN simulation (Dubois et al. 2014). These simulations are run with RAMSES (Teyssier 2002), an Eulerian hydrodynamics code with adaptive mesh refinement, and share the same cosmology based on the WMAP-7 data (Komatsu et al. 2011): Hubble constant $H_0 = 70.4$ km s⁻¹ Mpc⁻¹, total baryon density $\Omega_h = 0.0455$, total mass density $\Omega_m = 0.272$, dark energy density $\Omega_{\Lambda} = 0.728$, amplitude of power spectrum $\sigma_8 = 0.809$, and power spectral index $n_s = 0.967$. The parent simulation, Horizon-AGN, is a large-volume, (100 Mpc h^{-1})³,

cosmological simulation with a spatial resolution of $\Delta x \gtrsim 1$ kpc and a mass resolution of $m_{\rm DM} = 8 \times 10^7 M_{\odot}$ (dark matter particle) and $m_{\rm stellar} = 2 \times 10^6 M_{\odot}$ (stellar particle).

The NH zooms in a spherical region with a radius of 10 comoving Mpc in the field environment of Horizon-AGN. The refinement of each cell in the zoomed region is allowed when the mass of the cell is greater than eight times the initial mass resolution or the size of a dense cell $(n_{\rm H} > 5 {\rm cm}^{-3})$ is smaller than Jeans length to reach $\Delta x \sim 34 {\rm pc}$ at z = 0.0. Additional global cell refinement occurs at $a_{\rm exp} \simeq 0.1$, 0.2, 0.4, and 0.8 to keep the minimum cell size roughly constant. In this study, we used galaxies at z = 0.3, which is close enough to compare the properties of galaxies with those in the local universe. The dark matter and stellar particle resolutions are $m_{\rm DM} = 10^6 M_{\odot}$ and $m_{\rm stellar} = 10^4 M_{\odot}$, respectively, and the spatial resolution is $\Delta x \gtrsim 52 {\rm pc}$ (in physical scale) at z = 0.3.¹⁰ The high-resolution nature of the NH simulation was found to be very useful to pin down the origins of the disk and spheroidal components of field galaxies (e.g., Park et al. 2019).

The ongoing GALACTICA project focuses on individual galaxies in the field environments, extracted from the Horizon-AGN volume (yet not in the NH volume) to explore their evolution in detail down to z = 0.0. The spatial resolution at the final epoch (z = 0.0) is $\Delta x \gtrsim 34$ pc (in physical scale), as targeted by NH. Since all NH galaxies can only be studied down to $z \sim 0.3$, we also explored one GALACTICA galaxy further down to z = 0.0 in more detail. Here we briefly describe the baryonic prescriptions implemented in both NH and GALACTICA simulations. A more detailed description can be found in the introduction paper of the NH project (Dubois et al. 2020).

Gas can cool down to 0.1 K through primordial and metal cooling following the model of Sutherland & Dopita (1993; down to 10^4 K) and Dalgarno & McCray (1972; below 10^4 K). After the reionization epoch at z = 10, gas is heated by a uniform UV background radiation based on Haardt & Madau (1996), and the heating rates are assumed to be reduced by $\exp(-n/n_{\text{shield}})$ in optically thick regions (gas density, $n_{\rm H} > n_{\rm shield} = 0.01 \text{ cm}^{-3}$) due to self-shielding. Stars can form in a cell where the hydrogen number density is greater than $n_{\rm H} = 10 {\rm ~cm^{-3}}$ and the temperature is lower than $2 \times 10^4 {\rm ~K}$ based on the Schmidt relation (Schmidt 1959), $\dot{\rho} = \epsilon_* \rho_{\rho} / t_{\rm ff}$, where $\dot{\rho}$ is the star formation rate (SFR), ϵ_* is the star formation efficiency, ρ_g is the gas density, and $t_{\rm ff}$ is the freefall time. The star formation efficiency (ϵ_*) varies depending on the local turbulent Mach number and virial parameter, following Kimm et al. (2017).

Each stellar particle with a mass of $10^4 M_{\odot}$ is assumed to be a simple stellar population following the Chabrier initial mass function (Chabrier 2005), with lower and upper mass cutoffs of 0.1 and 150 M_{\odot} . We assume that the minimum mass of a star for the Type II SN explosion is $6 M_{\odot}$. When a stellar particle becomes older than 5 Myr, the SN explosion is assumed to take place, returning 31% of the mass of the stellar particle to the surroundings, with a metal yield of 0.05. A mechanical SN feedback scheme is employed following Kimm & Cen (2014).

Supermassive black holes (BHs) are represented as sink particles placed in cells where gas and stellar densities exceed the threshold of star formation and stellar velocity dispersion

higher than 20 km s^{-1} . New sink particles are not allowed to form within a distance of 50 comoving kpc from preexisting sink particles, and two existing BHs are assumed to merge with each other when they get within 150 pc. The initial seed mass of a BH is $10^4 M_{\odot}$, and it grows with a Bondi–Hoyle–Lyttleton accretion rate (Hoyle & Lyttleton 1939; Bondi & Hoyle 1944) $\dot{M}_{\rm BH} = (1 - \epsilon_r \, \dot{M}_{\rm Bondi}),$ where $\dot{M}_{\rm Bondi} = 4\pi\rho (GM_{\rm BH})^2 / (u^2 + c_s^2)^{3/2},$ *u* is the average velocity of the BH relative to the gas velocity, c_s is the average sound speed, ρ is the average gas density, and ϵ_r is the spin-dependent radiative efficiency. The maximum limit of the accretion rate is set to the Eddington rate. Two different types of feedback from the AGN are modeled based on the ratio of the gas accretion rate to the Eddington rate (χ) , following Dubois et al. (2012): the radio mode ($\chi < 0.01$) and the quasar mode ($\chi > 0.01$). In the radio mode, the AGN releases mass, momentum, and energy in the form of bipolar jets with a spin-dependent feedback efficiency, while in the quasar mode, it only deposits thermal energy isotropically into the surrounding gas cells (i.e., increases temperature).

2.2. Sample Selection

Galaxies in the NH simulation are identified based on the AdaptaHOP algorithm (Aubert et al. 2004) with the most massive subnode mode (Tweed et al. 2009), and the minimum number of stellar particles required for a galaxy is 50. At z = 0.3, there are 54 identified galaxies with a stellar mass larger than $10^{10} M_{\odot}$. We apply the stringent mass cut despite the high mass resolution in order to secure a large number of star particles for reliable statistical analysis. Since the zoomed region of the NH simulation is embedded in its parent simulation, Horizon-AGN, some halos in the outskirts of the zoomed region are contaminated by low-resolution dark matter particles. Hence, we only selected the galaxies in the halos with contamination fractions lower than 0.001 (0.1%), which gives us 31 galaxies with masses above $10^{10} \dot{M}_{\odot}$ (22 of them are contamination-free). In this study, we have selected 18 disk galaxies from 31 galaxies that are visually undisturbed and have bulge-to-total ratios, $B/T \leq 0.4$. The bulge-to-total ratio is measured using the stellar particles inside the R_{90} of each galaxy, the radius within which 90% of the total stellar mass is contained. The "bulge" component is defined kinematically using the orbital circularity parameter, ϵ (Abadi et al. 2003), which quantifies how close a stellar orbit is to the circular orbit in the galactic plane by comparing the angular momentum of the stellar particle in the net rotating direction (z-axis) of a galaxy (J_z) and that of a circular orbit with the same energy $(J_{\text{circ}}), \epsilon = J_z/J_{\text{circ}}$. The bulge mass is measured as twice the mass sum of the stellar particles with $-0.5 < \epsilon < 0$, assuming that the circularity of the bulge stars is symmetrically distributed around zero (i.e., random-dominated component). Thus, B/T gives the mass fraction of "nondisk" components with dispersion-dominated kinematics, including the stellar halo. Figure 1 shows the r-band face-on and edge-on images of the 18 selected NH galaxies at z = 0.3. The properties of the simulated galaxies used in this study are given in Table A1.

3. Properties of Thin and Thick Disks

First, we will check whether the models in the simulations reproduce the observed characteristics of the thin and thick disks, such as scale heights and luminosity ratios, when the double-component fitting is applied to the vertical profiles of

 $^{^{10}}$ The simulation is currently running, and $z\,{=}\,0.3$ is the lowest available redshift suitable for this analysis.

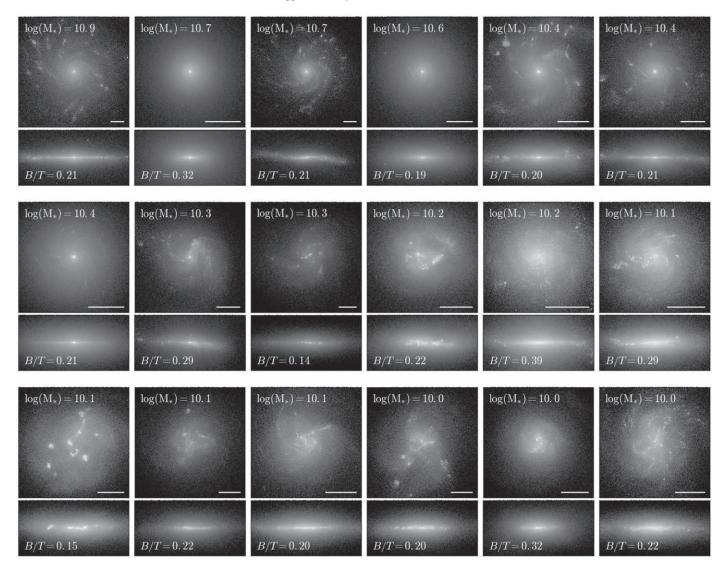


Figure 1. The *r*-band face-on and edge-on images of the 18 selected NH galaxies at z = 0.3 in descending order of stellar mass of galaxies. The extent of each box for the face-on image is 2 R_{90} of each galaxy, while the height of the box for the edge-on image is R_{90} . The R_{90} is the 3D radius containing 90% of the total stellar mass of a galaxy. The white bar represents 5 kpc. The kinematic bulge-to-total ratio (B/T) of each galaxy is presented at the bottom.

the simulated galaxies. Then, we will separate the two disk components based on the vertical profile and identify which stellar particles belong to each component. In an attempt to see how physically distinct the two components are, we will focus on the difference between the two components in various properties, such as the fraction of stars formed ex situ, age, metallicity, kinematics, and birthplaces.

3.1. The Two-component Fits to the Vertical Profiles

3.1.1. The Galactica Galaxy

First, we check the radial and vertical profile of the GALACTICA galaxy at z = 0.0. The top panels of Figure 2 show the face-on and edge-on *r*-band images of the GALAC-TICA galaxy. The *r*-band flux of each stellar particle is calculated based on its age and metallicity following the Bruzual & Charlot (2003) stellar population model, without dust extinction. The galaxy's stellar mass and size are about half that of the MW; the stellar mass of this galaxy is $2.75 \times 10^{10} M_{\odot}$, and the half-mass-radius (R_{50}) and R_{90} , the

radius within which 90% of the total stellar mass is contained, are 1.9 and 8.0 kpc, respectively.

We measure the radial and vertical profiles of this galaxy in both mass and *r*-band luminosity. The radial profile is measured from the face-on images, and the combination of the Sérsic (1963) and exponential disk profiles is applied to the radial profile, which gives the bulge-to-total ratios, $[B/T]_{\rm fit}$, of 0.38 (mass) and 0.18 (*r* band). To measure the vertical distribution, we use the cylindrical coordinate, where the *z*-axis is the direction of the net angular momentum of the stellar particles inside R_{90} . The vertical distribution is measured in a cylindrical bin where $R_{xy} = 3.4 \pm 1$ kpc, corresponding to $2 R_d$, where R_d is the disk scale length measured in the *r* band and fitted with a double-component profile (e.g., van der Kruit & Searle 1981; Yoachim & Dalcanton 2006; Comerón et al. 2011),

$$\rho(Z) = \rho_{\text{thin}} \operatorname{sech}^2\left(\frac{|Z|}{2 \, z_{\text{thin}}}\right) + \rho_{\text{thick}} \operatorname{sech}^2\left(\frac{|Z|}{2 \, z_{\text{thick}}}\right), \quad (1)$$

where ρ_{thin} and ρ_{thick} are the densities of the thin and thick disks in the galactic midplane (|Z| = 0), and z_{thin} and z_{thick} are

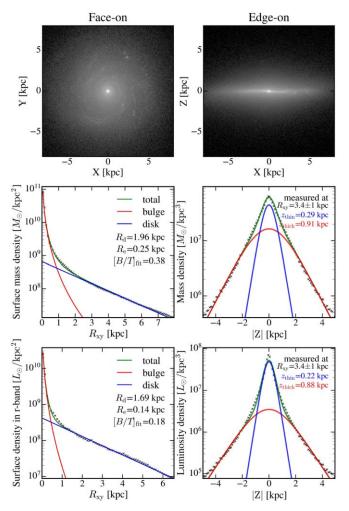


Figure 2. (Top) Face-on and edge-on *r*-band images of the GALACTICA galaxy and the radial and vertical profiles measured in mass (middle) and *r* band (bottom). The radial profiles are fitted with a combination of Sérsic and exponential disk profiles, returning the scale length of the disk (R_d) and bulgeto-total ratios, $[B/T]_{fit}$. The two-component profile is applied to the mass/*r*band vertical profile of the galaxy, from which the scale heights of the thin and thick disks are measured.

their scale heights. The scale heights of the thin and thick disks are $z_{\text{thin}} = 290$ and $z_{\text{thick}} = 910$ pc in mass, while in the *r* band, both disks have slightly shorter scale heights of $z_{\text{thin}} = 220$ and $z_{\text{thick}} = 880$ pc.

To visualize the relative importance of the thin and thick disks in different galactic regions, we measure the vertical distributions in the cylindrical region with radii (R_{xy}) of 2-6 kpc with a bin size of 0.2 kpc and plot the fitted density of the thin and thick disks in each region. In each radial bin, the vertical distribution is obtained by measuring the number (mass) density of the stellar particles inside the window of ± 0.5 kpc to avoid high fluctuations due to the small number of stellar particles. In Figures 3(a) and (b), it is clear that the thin disk component is concentrated near the galactic midplane, while the thick disk component smoothly spreads over the disk regions $(R_{xy} = 2-6 \text{ kpc} \text{ and } |Z| < 5 \text{ kpc})$. The double-component fit seems reasonably good (at least up to $|Z| \sim 4$ kpc), as can be seen in panel (c), where it shows the difference between the sum of the fitted densities of the thin and thick disks and the calculated mass density in each region.

In Figure 3(d), we also construct the projected map showing the thin disk mass ratios in this region. Since we have assumed only two components, the sum of the thin and thick disk mass ratios in each bin is set to 1. The vertical height where the mass densities of the thin and thick disks are comparable, represented as the light yellow regions, increases with the projected radius as well, as a result of disk flaring. The scale heights of thin and thick disks, represented as blue dashed and red dotted lines, both increase with the projected radius at which the vertical profile is measured; from $R_{xy} = 2$ to 6 kpc, the thin disk increases from 260 to 490 pc, and the thick disk increases from 770 to 1400 pc (by a factor of \sim 2). This flaring of the disk can also be found in other galaxy simulations, while the degree of flaring varies across simulations (e.g., Minchev et al. 2015; Grand et al. 2017; Ma et al. 2017; Buck et al. 2020), which may be due to the different merger histories of the galaxies, given that flaring is inevitably affected by mergers (e.g., Bournaud et al. 2009).

Figure 3(e) presents the thin disk *r*-band luminosity ratios in the same region, derived from the vertical profiles in the *r* band in the same way as the mass ratios. The flaring is also visible in the *r*-band profile, nearly to a similar degree as the flaring seen in the mass profile. The *r*-band luminosity near the galactic midplane, however, is dominated more by the thin disk (>80%), as young stars in the thin disk contribute significantly to the total luminosity, which makes the thin disk component more pronounced with a stronger slope change in the vertical distribution (Figure 2).

According to panels (d) and (e), which are based on the vertical profiles, $\sim 30\%$ of the mass and $\sim 10\%$ of the *r*-band luminosity near the galactic midplane appear to belong to the thick disk component. These values are broadly consistent with other simulations. For example, Ma et al. (2017) mentioned that $\approx 36\%$ of the stellar mass at the solar radius ($R_{xy} = 8 \text{ kpc}$) in their simulated MW-mass galaxy belongs to the thick disk according to the two-component fit to the vertical profile. Brook et al. (2012) identified the thick disk component in the chemical plane ([α /Fe]–[Fe/H]), and it contributed to \approx 27% of the stellar mass in the solar neighborhood. On the other hand, several studies performed the kinematic decomposition for all stellar particles in the simulated galaxies and showed that the mass of the thick disk is nearly comparable to that of the thin disk (e.g., Abadi et al. 2003; Obreja et al. 2018, 2019). The mass or luminosity ratio between the thin and thick disks seems to vary greatly depending on the measuring range and methods (e.g., derivation from the decomposition based on kinematics or chemical abundance).

3.1.2. The NH Sample Galaxies at z = 0.3

We also applied the same two-component fits to the *r*-band vertical profiles of the 18 NH sample galaxies at z = 0.3. Note that the vertical profile is measured at $2R_d$ of each galaxy to account for the different disk sizes of the galaxies. Figure 4(a) shows the scale height ratios of the thin and thick disks measured in the *r* band as a function of the circular velocity (V_{circ}) of the galaxies (see also Table A1 for the properties of each galaxy). The circular velocity is measured at R_{90} , following $V_{\text{circ}} = \sqrt{GM(\langle r)/r}$. The colors inside the circles represent the stellar mass of the NH galaxies at z = 0.3, indicating that more massive galaxies have higher circular velocities. We also include the values of the GALACTICA galaxy at z = 0, with $z_{\text{thick}}/z_{\text{thin}} = 4.06$ in the *r* band, as an open

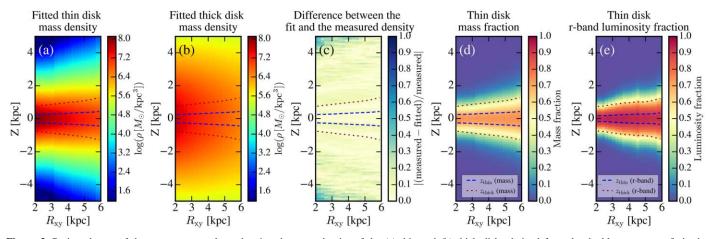


Figure 3. Projected map of the GALACTICA galaxy showing the mass density of the (a) thin and (b) thick disks derived from the double-component fit in the cylindrical regions where $2 \text{ kpc} < R_{xy} < 6 \text{ kpc}$ and |Z| < 5 kpc. (c) Difference between the fitted density derived by the double-component fit and the calculated mass density. (d) Mass ratios of the fitted thin disk. (e) The *r*-band luminosity ratios of the fitted thin disk. Only the two components, thin and thick disks, are assumed in this region, so the sum of the ratios of the thin and thick disks is set to 1. The blue dashed and red dotted lines in each panel are the scale heights of the thin and thick disks in mass (panels (a)–(d)) and the *r* band (panel (e)).

purple diamond. The magenta star shows the scale height ratio of the MW, which is about 3 (e.g., Gilmore & Reid 1983; Juric et al. 2008). Note that the value of the MW is measured based on the number density, not the photometric profile, yet it is still in a good agreement with the NH and GALACTICA galaxies.

Our sample of the NH galaxies shows a broad range of scale height ratios in the *r* band, broadly consistent with observations (e.g., Yoachim & Dalcanton 2006; Comerón et al. 2018; Martínez-Lombilla & Knapen 2019). The diagram is dominated by scatter in both observational and simulation data, but there is a hint of a positive trend in the sense that a more massive galaxy shows a larger ratio between the vertical scale height of the thick and thin disks. The linear fit to the observed data, for reference, has a slope of 0.013, and one standard deviation error is 0.0026. The median value across the sample of the galaxies is $z_{\text{thick}}/z_{\text{thin}} = 3.52$, represented as a dashed line, and gray shading shows the 16th–84th percentiles.

Figure 4(b) shows the *r*-band luminosity ratio between the thick and thin disks $(L_{\text{thick}}/L_{\text{thin}})$ as a function of the circular velocity of the galaxy. We plotted the luminosity ratios in the regions near the galactic midplane (|Z| < 1 kpc) with error bars covering a range of the ratios measured in the vertical range of $|Z| < 2 z_{\text{thick}}$. The colors of the circles again represent the stellar mass of the galaxies. The dashed line shows the median of the ratios in the NH galaxies, and the gray shading again represents the range of 16th–84th percentiles of the luminosity ratios in the samples.

We found that the *r*-band luminosity ratios seem to decrease slightly with the $V_{\rm circ}$ of the galaxies. A similar trend was found in Yoachim & Dalcanton (2006) by fitting a power law to their samples, which is represented as a green solid line in panel (b). We also applied the power-law fit to the luminosity ratios of the NH galaxies, and the blue line shows the obtained fit with a shade of 1σ : $L_{\rm thick}/L_{\rm thin} = 0.36(V_{\rm circ}/100 \,{\rm km \, s^{-1}})^{-0.68}$. It seems that our trend is shallower than the observed one, indicating that thick disks of our simulated galaxies may be brighter than the observations. The $L_{\rm thick}/L_{\rm thin}$ of GALACTICA (purple diamond) and the MW¹¹ (magenta star) fall within the 1σ of our trend.

¹¹ The value of the MW was taken as the local number density between the thin and thick disks: $\rho_{\text{thick}}/\rho_{\text{thin}} = 0.12$ (Juric et al. 2008).

Given that the MW has been forming stars at ~ $1 M_{\odot}$ yr⁻¹ (see, e.g., Robitaille & Whitney 2010), the estimated growth of the disk during the last 3.5 Gyr would be only by a factor of 5%–10%.¹² Therefore, we expect that the properties of the thin and thick disks we examined for the NH galaxies at z = 0.3 would be roughly similar even at z = 0.0, unless they experience mergers after z = 0.3 that could severely disturb the disk structures. As a check, we explored the thin and thick disks of the GALACTICA galaxy when it is at z = 0.3 and 0.0 and confirmed that the scale height and luminosity ratios between the two disks are similar at the two epochs.

3.2. Spatial Decomposition of Thin and Thick Disks

A first step toward investigating how distinct the two disk components are is to separate them and compare their properties, e.g., the contribution of stellar particles formed ex situ, stellar age, metallicity, and kinematics. In many observational studies, thin and thick disk stars have been separated based on the cut in the chemical plane of [Fe/H] and $[\alpha/\text{Fe}]$ (e.g., Lee et al. 2011; Anders et al. 2014; Bensby et al. 2014; Duong et al. 2018; Mackereth et al. 2019). Theoretically, some studies also performed decomposition based on the kinematic properties of stellar particles in the simulated galaxies (e.g., Abadi et al. 2003; Scannapieco et al. 2009; Obreja et al. 2018, 2019). However, it is difficult to spatially separate the thin and thick disk stars because their distribution overlaps in the disk region; for example, in our simulated galaxy, the thick disk component contributes to roughly 30% of the stellar mass near the galactic midplane (Figure 3(d)).

In this study, we attempt to separate the thin and thick disk stars based on the *r*-band vertical profiles measured at $R = 2 R_d \pm 1$ kpc. First, we measured the "cross height" (z_{cross}), where the contributions from the thin and thick disks are equal. To avoid high contamination from each component near the transition zone (close to z_{cross}), we classify all stellar particles below 0.8 z_{cross} as thin disk stars and stellar particles located in the region 1.2 $z_{cross} < |Z| < 2 z_{thick}$ as thick disk stars. Note that while the upper limit of the height for the thick disk is

 $^{^{12}}$ This value is a rough estimate based on the current SFR of the MW. Taking into account the SFR over the past 3 Gyr, the estimate could be higher by a factor of 2 or so.

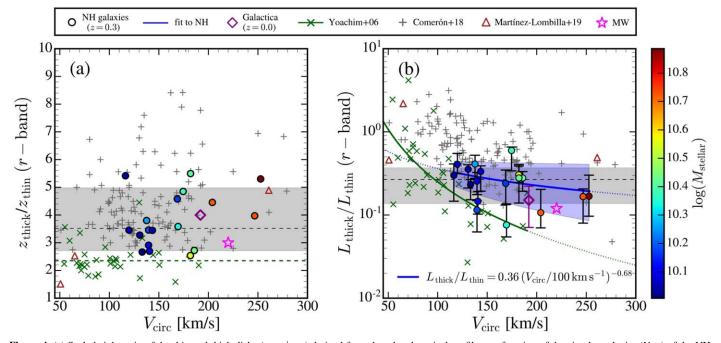


Figure 4. (a) Scale height ratio of the thin and thick disks ($z_{\text{thick}}/z_{\text{thin}}$) derived from the *r*-band vertical profile as a function of the circular velocity (V_{circ}) of the NH galaxies. (b) The *r*-band luminosity ratio of the two disks ($z_{\text{thick}}/z_{\text{thin}}$) in the regions near the galactic midplane (|Z| < 1 kpc). The error bars cover a range of luminosity ratios measured from the midplane at |Z| = 0 (lowest) to the ratios measured up to $|Z| < 2 z_{\text{thick}}$ (highest). The color represents the stellar mass of the NH galaxies at z = 0.3. The values of the scale height and luminosity ratios between the two disks in each galaxy are listed in Table A1. The dashed gray horizontal line in each panel shows the median value of the scale height/luminosity ratios of the NH galaxies, with gray shading showing the range from the 16th to 84th percentile. The values of the GALACTICA galaxy at z = 0.0 are presented as open purple diamonds with $z_{\text{thick}}/z_{\text{thin}} = 4.06$ and $L_{\text{thick}}/L_{\text{thin}} = 0.15$, while the MW vales are marked as open magenta stars, $z_{\text{thick}}/z_{\text{thin}} \sim 3.0$ (e.g., Bland-Hawthorn & Gerhard 2016) and $\rho_{\text{thick}}/\rho_{\text{thin}} \sim 0.12$ (e.g., Juric et al. 2008). The gray plus signs are the values of these observed galaxies are mass ratios between the two disks, $M_{\text{thick}}/M_{\text{thin}}$, instead of luminosity ratios of their sample galaxies. The green solid line is the observed relation suggested by Yoachim & Dalcanton (2006), and the dashed green line in panel (a) is the median scale height ratios of their samples (with $V_{\text{circ}} \sim 50-190 \text{ km s}^{-1})$; the fitted power law to the NH galaxies (with $V_{\text{circ}} \sim 110-260 \text{ km s}^{-1})$, and shading indicates 1σ of the fit: $L_{\text{thick}}/L_{\text{thin}} = 0.25(V_{\text{circ}}/100 \text{ km s}^{-1})^{-0.68}$. We find that thin and thick disks are reprodued in our simulations when the two-component fits are applied and the resulting scale heights and luminosity ratios between the two disks are bro

set to $2 z_{\text{thick}}$ to account for the different thick disk extent of each galaxy, the conclusion does not change even when we set the limit to a fixed value of 2 kpc as adopted in some previous studies. We applied this decomposition technique to the GALACTICA galaxy at z = 0.0 and the 18 NH galaxies at z = 0.3 to separate their thin and thick disks.

Note that when spatially separated, the two disks contain overlapping components from each other. For example, in Figure 3, we have shown that even in the galactic midplane, thick disk stars contribute to $\sim 30\%$ of mass and $\sim 10\%$ of luminosity. This would make the difference in properties between the two disks less dramatic, which will be discussed in the next section. However, the spatially defined thick disk component would be less affected by these overlaps than the thin disk, as the off-plane regions are highly dominated by thick disk stars. Also, in Section 4, we track the vertical distribution of each mono-age population of stars without any spatial separation of thin/thick disks and show that stars are born with thinner vertical distributions but later get thicker with time due to heating. Therefore, our qualitative conclusion is not heavily affected by the overlapping components.

3.2.1. Decomposition Results: Age–Metallicity and the Origins of Stellar Particles

Figure 5 shows the age-metallicity distribution of the decomposed thin and thick disk stellar particles in the

GALACTICA galaxy. The stellar particles in the thin and thick disks are further divided by their birthplace: in situ or ex situ.¹³ The majority (~95%) of the thin disk consists of the stars formed in situ, many of which formed recently within the last 2 Gyr (~37%). On the other hand, ~15% of the stellar particles in the thick disk are formed ex situ and later accreted, mostly around $z \sim 2$ (10–12 Gyr) during a couple of major merger events. Even so, the dominant origin of the thick disk is still the stars formed in situ (85%). However, the important difference is in the age of the in situ stars; the age distribution of the in situ stars of the thick disk is significantly skewed toward larger ages compared to that of the thin disk.

The accretion origin of the thick disk was investigated by Abadi et al. (2003), where they found in their simulation that ~60% of the stellar particles in their kinematically decomposed thick disk came from the disrupted satellite galaxies. Indeed, there is one galaxy, FGC 227, that has a thick disk with a large fraction of counterrotating stars that is thought to be originated from accretions (e.g., Yoachim & Dalcanton 2008). These accreted stars in the thick disk are predicted to have highly dispersion-dominated kinematics compared to the stars formed in situ (e.g., Sales et al. 2009). However, the kinematics of MW

¹³ At each snapshot, we tagged stars younger than 50 Myr inside the R_{90} of the main progenitors of the galaxy in question as stars formed in situ. Stars that have not been tagged at all until the final epoch are considered as ex situ formed stars.

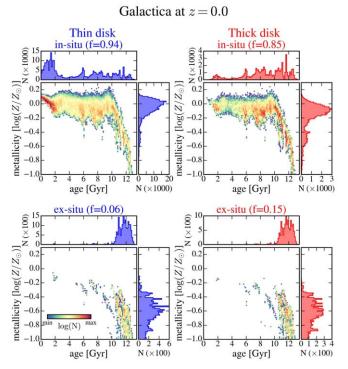


Figure 5. Distribution of the decomposed thin (left; blue histograms) and thick (right; red histograms) disk stars of the GALACTICA galaxy in the plane of age (in gigayears) and metallicity (log(Z/Z_{\odot}). The stellar particles in each component are further divided into in situ (top panels) and ex situ (bottom panels) stellar particles, and their fraction of each component is shown at the top of each panel. We find that the majority of the stars in the thin (~95%) and thick (~85%) disks are the stellar particles formed in situ. The major difference between the thin and thick disks is the age distribution of the in situ stars.

thick disk stars seems to disfavor the accretion origin (e.g., Lee et al. 2011; Ruchti et al. 2011, 2014), and, furthermore, recent observational studies on the kinematics of the thick disks in local galaxies have also provided evidence supporting the scenario in which most of the thick stars are formed in situ (e.g., Comerón et al. 2019; Pinna et al. 2019b). Many other simulations have also suggested much lower fractions of ex situ stars in the thick disks, typically less than a few percent (e.g., Brook et al. 2012; Obreja et al. 2019). For the bulk of our GALACTICA and NH galaxies, the accretion of the stars from disrupted satellite galaxies appears to be insignificant. The median ex situ fractions of the thin and thick disks in the 18 NH galaxies are $f_{ex situ} = 0.06^{+0.05}_{-0.03}$ (thin disks) and $0.11^{+0.16}_{-0.06}$ (thick disks); only two out of 18 galaxies have $f_{ex situ} > 0.3$, one of which has $f_{ex situ} > 0.5$.

The stellar particles in the separated thin and thick disks show differences in age and metallicity. The median age of the thin and thick disks in the GALACTICA galaxy at z = 0 is $5.4^{+5.2}_{-3.6}$ Gyr, respectively, with errors derived from the 16th–84th percentiles. The thin and thick disk components have a median metallicity of $\langle \log(Z/Z_{\odot}) \rangle = -0.05^{+0.09}_{-0.21}$ and $\langle \log(Z/Z_{\odot}) \rangle = -0.16^{+0.12}_{-0.44}$, where $Z_{\odot} = 0.0134$ (Asplund et al. 2009). Table 1 summarizes the differences in age and metallicity between the thin and thick disks in the GALACTICA galaxy at z = 0.0 (second column) and the MW galaxy (fourth column).

The ages of the thin and thick disks (and the difference between the two components) are consistent with those of the MW (e.g., Haywood et al. 2013). However, the metallicity

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difference between the two components of the GALACTICA galaxy, Δ [Fe/H] ≈ -0.12 dex,¹⁴ seems significantly smaller than that found in the MW. For example, when the thin and thick disks of the MW are decomposed based on the chemical compositions, the metallicity difference has been found to be Δ [Fe/H] ~ -0.4 dex (e.g., Lee et al. 2011). One thing we need to consider is that the stellar mass of the GALACTICA galaxy is only half that of the MW, so, in general, the galaxy might not be as enriched as the MW (e.g., Faber 1973; Gallazzi et al. 2006). The other issue is the merger history of the GALACTICA galaxy; it has a significant major merger with a mass ratio of 0.24 at $z \sim 2.2$, followed by rapid mass growth and metal enrichment. This is why the thick disk component, even considering only the stellar particles formed in situ (top right panel in Figure 5), has a bimodal distribution of metallicity with a mild peak at $\log(Z/Z_{\odot}) \sim -0.5$ and a much stronger peak at $\log(Z/Z_{\odot}) \sim -0.1$. On the other hand, the enhanced star formation between zero and 2 Gyr, most of which contributes to the growth of the thin disk, as shown in the top left panel (see also Figure 10(a)), is driven by the interaction with two satellite galaxies, consistent with observations (see also Ruiz-Lara et al. 2020), from which the metalpoor gas is accreted as well. This might have diluted the interstellar medium in the galaxy, thus leading to a small difference in metallicity between the younger stellar particles (with age $\sim 0-2$ Gyr) and the older stellar particles (with age \sim 8–10 Gyr).

Also, when comparing the values between the GALACTICA galaxy and the MW, it is important to note that different definitions of thin/thick disk are adopted, which might affect the differences between the two disks. When the thin disk is defined chemically, as in many of the MW studies (e.g., Lee et al. 2011; Anders et al. 2014; Bensby et al. 2014), "young" thin disk stars can be well separated, as the alpha abundances broadly trace the age of the populations. Since younger stars tend to be more metal-rich and have higher rotational velocity, the difference in properties between the thin and thick disks would be smaller when defined based on spatial cut than when the two disks are chemically defined. Indeed, when we separate the two disks based on a simple "age" cut of 8 Gyr, for example, the differences in properties obviously increase to $\Delta age \sim 7.1 \text{ Gyr}$, $\Delta \log(Z/Z_{\odot}) \sim 0.32 \text{ dex}$, and $\Delta V_{\rm rot} \sim 81 \,{\rm km \, s^{-1}}$. However, this age cut is based on the assumptions that we know a priori that the thick disk stars formed earlier consisting of older stars, regardless of their origins (e.g., in situ or ex situ). On the other hand, when the thick disk is defined spatially, as in this study, we focus on the "thickly distributed" component primarily occupying higher altitudes from the galactic midplane, with the same motivation that the concept of a thick disk was first proposed to explain the vertical distribution.

We have performed the same analysis on the 18 NH galaxies at z = 0.3. The mass-weighted (or *r*-band-weighted) age and metallicity difference in each galaxy is calculated from the median values (weighted average) of the thin and thick disk stellar particles. The median values of the properties of the two disks in the 18 NH samples at z = 0.3 ($t_{univ} \sim 10$ Gyr) are also given in Table 1.

Similarly, the thick disk components in the NH galaxies are older and metal-poorer than the thin disk components, which is

 $[\]frac{14}{14}$ We here assume that Fe scales with Z and the difference in the hydrogen abundance is negligible.

Table 1
Properties of the Thin and Thick Disks in the GALACTICA Disk Galaxy at $z = 0.0$, 18 NH Galaxies at $z = 0.3$, and the MW

	$\begin{array}{c} \text{GALACTICA} \\ (z=0.0) \end{array}$	$\langle 18 \text{ NH Galaxies} \rangle$ (z = 0.3, $t_{\text{lb}}^{a} \sim 3.5 \text{ Gyr}$)	MW 5.0-7.0 ^b	
$M_{\rm stellar} \ [imes 10^{10} M_{\odot}]$	2.8	1.7		
Thin disk age [Gyr]	$5.4^{+5.3}_{-4.4}$	$4.0^{+1.5}_{-1.8}$	<8 ^{c,d}	
Thick disk age [Gyr]	$9.7^{+2.2}_{-3.7}$	$5.6^{+1.0}_{-1.9}$	>8-10 ^{c,d}	
Δ age (median) [Gyr]	4.3	1.6		
Thin disk age (r band) [Gyr]	2.2	1.7		
Thick disk age (r band) [Gyr]	7.8	4.7		
Δ age (r band) [Gyr]	5.7	3.0		
Thin disk $\log(Z/Z_{\odot})$	-0.05	-0.06	$[Fe/H] \sim -0.2^{e}$	
Thick disk $\log(Z/Z_{\odot})$	-0.17	-0.22	$[{\rm Fe}/{\rm H}] \sim -0.6^{\rm e}$	
$\Delta \log(Z/Z_{\odot})$ (median) [dex]	0.12	0.16	0.4	
$\Delta \log(Z/Z_{\odot})$ (<i>r</i> band) [dex]	0.20	0.15		
Thin disk $V_{\rm rot}$ [km s ⁻¹]	172_{-79}^{+54}	109^{+66}_{-21}	220	
Thick disk $V_{\rm rot}$ [km s ⁻¹]	129_{-115}^{+73}	89^{+54}_{-23}	180	
$\Delta V_{\rm rot}$ (median) [km s ⁻¹]	43	20	20–70 ^{e,f}	
Thin disk f _{ex situ}	0.06	$0.06\substack{+0.05\\-0.03}$		
Thick disk $f_{\text{ex situ}}$	0.15	$0.11\substack{+0.16 \\ -0.06}$		

Notes. For the GALACTICA galaxy, all of the given values are the median/*r*-band weighted average values of the stellar particles with errors showing 16th–84th percentiles. The values of each NH galaxy are measured in the same way, and the median values of the 18 NH galaxies are presented in the third column, with errors showing from 16th to 84th percentiles among the sample galaxies.

^a $t_{\rm lb}$: the look-back time from z = 0.0 is ~3.5 Gyr.

^b McMillan (2011).

^c Bensby et al. (2014).

^d Haywood et al. (2013).

^e Lee et al. (2011).

^f Anders et al. (2014).

qualitatively consistent with observations (e.g., Yoachim & Dalcanton 2008; Lee et al. 2011; Pinna et al. 2019a; Kasparova et al. 2020), while the metallicity differences remain small compared to observations. The difference in age and metallicity would likely be larger when measured at z = 0 in typical star-forming galaxies because continued star formation is likely to increase the mean metallicity of young stars in the thin disk. However, the exact amount will depend on the detailed formation history of each galaxy.

3.2.2. Decomposition Results: Kinematics

The thick disk of the MW defined by chemical abundances is thought to have different kinematic properties from the thin disk with a slower rotational velocity by 40–50 km s⁻¹ (see Lee et al. 2011; Anders et al. 2014). Also, similar lags in velocity have been found in simulations where the thick disk stars are selected based on age (see Brook et al. 2012; Minchev et al. 2013). While considering this as a significant difference, some studies have identified the thin and thick disks according to the kinematic properties, for example, using the so-called Toomre diagram (see Bensby et al. 2003). Here we explore the velocity difference between the two components, in our case, separated by the spatial definition, and analyze the cause of the difference by tracking the origin of the stellar particles belonging to each component.

Figure 6(a) shows the rotational velocity distribution of the thin and thick disk stellar particles in the GALACTICA galaxy, normalized by the total number of stellar particles in each

component. The rotational velocity is measured as the tangential velocity, V_{ϕ} , of the stellar particles in the cylindrical coordinate of the galaxy, where the *z*-axis is defined as the rotational axis of the galaxy. The rotational velocity of the thin disk component is $\langle V_{\text{rot,thin}} \rangle = 172^{+54}_{-79} \text{ km s}^{-1}$ (median and the error showing from the 16th to 84th percentile), while the thick disk component exhibits a velocity lag of ~43 km s⁻¹ ($\langle V_{\text{rot,thick}} \rangle = 129^{+73}_{-115} \text{ km s}^{-1}$). We also further divide the stellar particles in each component into stellar particles formed in situ and ex situ and measure their rotational velocities. We find that the velocity lag of the thick disk is caused mostly by the in situ stellar particles ($\Delta V_{\text{rot}}(\text{in situ}) = 39 \text{ km s}^{-1}$), rather than the accreted stellar particles (see Qu et al. 2011).

Panel (b) shows the median rotational velocity (V_{rot}) of the in situ thin (blue solid line) and thick (red solid line) disk stars as a function of their ages. The blue/red dashed lines show the 16th and 84th percentiles of the V_{rot} at a given stellar age of the thin/thick disk stars. The distributions of the in situ thin and thick disk stars in the plane of age and V_{rot} are shown as blue and red contours (0.5σ and 1σ). The vertical hatched region represents the disk settling epoch ($z_{disk settling}$), when the galactic disk structure starts to develop. To quantitatively define this epoch, we used the V/σ of the cold gas ($n_{\rm H} > 10 \text{ cm}^{-3}$ and $T < 2 \times 10^4 \text{ K}$) inside the R_{90} of the galaxy. The V/σ is measured as the mass-weighted mean tangential velocity ($V = \langle V_{\phi} \rangle$) of the cold gas cells in the cylindrical coordinates, where the z-axis is defined as the direction of the net angular momentum of the cold gas cells divided by

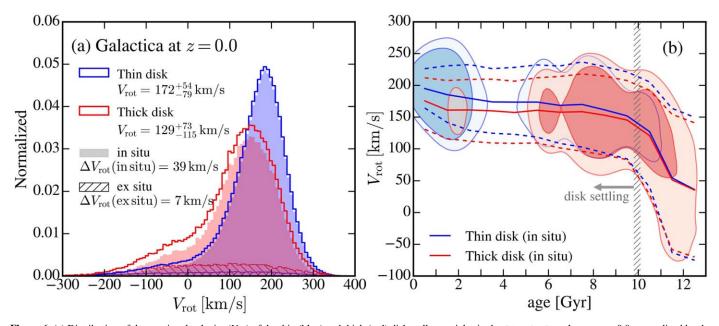


Figure 6. (a) Distribution of the rotational velocity (V_{rot}) of the thin (blue) and thick (red) disk stellar particles in the GALACTICA galaxy at z = 0.0, normalized by the total number of stellar particles in each component. The stellar particles in each component are further divided into stars formed in situ (solid histogram) and ex situ (hatched histogram). The difference in rotational velocity between the two components ($\Delta V_{rot} = 43 \text{ km s}^{-1}$) can be largely explained by the velocity difference between the in situ stellar particles in each component (ΔV_{rot} (in situ) = 39 km s⁻¹). (b) Rotational velocity of the thin (blue line) and thick (red line) disk stellar particles formed in situ as a function of stellar ages. The age distributions of the in situ thin and thick disk stars are shown as blue and red contours showing 0.5 σ and 1 σ . The vertical hatched region is the disk stelling epoch ($z_{disk settling}$), when the galaxy starts to develop its disk structure. We find that the rotational velocity of the stars formed in situ increases with decreasing age, and it is the different age distribution between the thin and thick disks that contributes the most to the difference in V_{rot} between the two components.

mass-weighted 1D velocity dispersion: $\sigma = \sqrt{(\sigma_r^2 + \sigma_{\phi}^2 + \sigma_z^2)/3}$. The $z_{\text{disk settling}}$ is defined as the time when the mean cold gas V/σ for the past 150 Myr (~10 snapshots) first reaches higher than 3, which is used as a criterion for settled disks in some studies (e.g., Kassin et al. 2012; see also Y. Dubois et al. 2021, in preparation).

The rotational velocity of the stars formed in situ increases with decreasing age. In particular, the stellar particles formed in situ before the disk settling epoch (right side of the vertical hatched region) have a much lower rotational velocity compared to the young stars formed recently because the galaxy was much smaller at higher redshifts. It could also be attributed to the fact that many of the stars formed before disk settling were formed with random-dominated kinematics during chaotic mergers that might have prevented the galaxy from settling its disk. What contributes the most to the difference in $V_{\rm rot}$ between the thin and thick disks is the difference in age distribution between the stars in the two components; while many of the thin disk stars are young stars with high $V_{\rm rot}$, approximately 40% of the in situ thick disk stars are formed before the disk settling, contributing to the lower end of the $V_{\rm rot}$ distribution of the thick disk. Also, most of the thick disk stars formed after the disk settling are old stars with ages 6–10 Gyr. One noticeable feature is that for the stars formed after the disk settling (<10 Gyr), the thick disk stars have lower $V_{\rm rot}$ than the thin disk stars with the same age, which may have resulted from disk heating. The difference in $V_{\rm rot}$ for the stars formed in situ after the disk settling is $\Delta V_{\rm rot}$ (in situ, after disk settling) = 25 km s^{-1} .

We have also measured the velocity lag for the 18 NH galaxies. We define the "velocity lag fraction" as the velocity lag normalized by the circular velocity (V_{circ}) of each galaxy to compare the degree of kinematic differences in galaxies with

different masses,

velocity lag fraction =
$$(V_{\text{rot,thin}} - V_{\text{rot,thick}})/V_{\text{circ}}$$
, (2)

where V_{circ} is the circular velocity measured at R_{90} of the galaxy following $V_{\text{circ}} = \sqrt{GM(\langle r \rangle/r}$. All of the NH galaxies have a positive velocity lag fraction, which can be understood according to the vertical gradient of the mean rotational velocity found in several observations (e.g., Ivezić et al. 2008; Carollo et al. 2010) and simulations (e.g., Di Matteo et al. 2011). However, the velocity lag varies across galaxies even after mass (circular velocity) normalization. The median value for the NH galaxies at z = 0.3 is 0.08 with a range from 0.06 (16th) to 0.22 (84th percentile).

There are several elements to consider to understand the velocity lag fraction. First, the number of stars formed ex situ contributes to the lower end of the distribution of $V_{\rm rot}$, as the accreted stars are thought to have dispersion-dominated kinematics with highly eccentric orbits (e.g., Sales et al. 2009). However, as the number of ex situ stars is low for most of the galaxies in our simulations, their contribution to the total kinematics would also not be significant. Second, stars formed in situ before disk settling would have a low rotational velocity, as seen in Figure 6(b). Finally, stars formed in situ after disk settling could have a high $V_{\rm rot}$ at their birth, but their rotational speed could decrease with time due to heating.

First, we examine how the different age distributions of the thin and thick disks (or how old the thick disks are) contribute to the velocity lag of the thick disks. Figure 7(a) shows the velocity lag fraction using only in situ stellar particles as a function of the age of the thick disk. The age of the thick disk was measured from z = 0.0 by adding 3.45 Gyr (look-back time of z = 0.3) to the median age of the stellar particles in the thick disks. Indeed, there seems to be a mild correlation between the

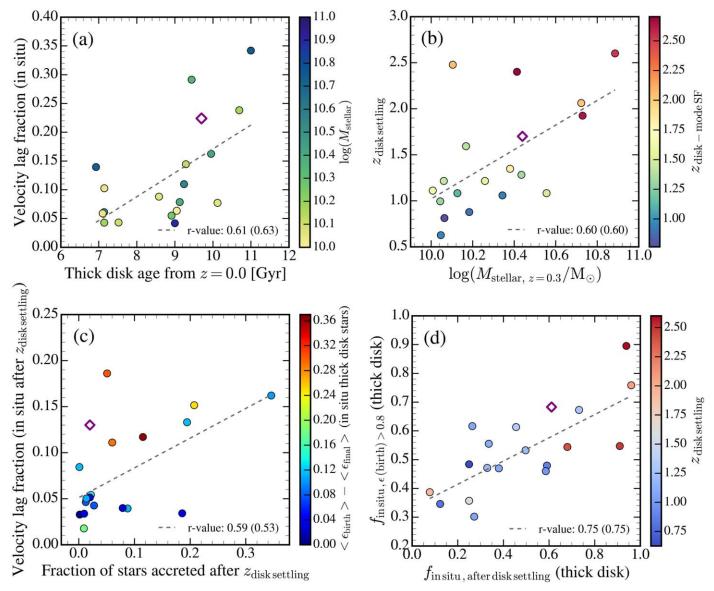


Figure 7. (a) Velocity lag fraction for the in situ stellar particles in the thin and thick disks in the 18 NH galaxies (at z = 0.3) as a function of the age of the thick disks. The age of the thick disks is taken as the median age of the stellar particles in the thick disk component plus $t_{look back} = 3.45$ Gyr to obtain their ages from z = 0.0. The galaxies are color-coded according to their stellar mass. (b) Disk settling epoch ($z_{disk settling}$, defined as the time when the mean cold gas V/σ for the past 150 Myr first reaches higher than 3; see text for details) as a function of the stellar mass of the galaxies at z = 0.3. The galaxies are color-coded by the epoch when a galaxy starts to predominantly form disk stars ($z_{disk-mode SF}$; see the text). (c) Velocity lag fraction for the stellar particles formed in situ after $z_{disk settling}$ as a function of the fraction of stars accreted after $z_{disk settling}$ in the total number of stars in a galaxy. The color represents the change in orbital circularity of the thick disk stars formed in situ between their birth and z = 0.3 (the final epoch). (d) Fraction of stars in the thick disk that are formed in situ with ϵ_{birth} (orbital circularity at birth) greater than 0.8 as a function of the fraction of stars in the thick disk that are formed in situ after $z_{disk settling}$. In all four panels, the values of the GALACTICA galaxy at z = 0.0 are shown as open purple diamonds. The gray dashed line in each panel is the linear fit to the data of the 18 NH galaxies with the Pearson correlation coefficient (r value) given in the lower right corner. The value in parentheses in each panel is the correlation coefficient obtained when the value of the GALACTICA galaxy is also included. We find that different age distributions of the in situ stars in the thin and thick disks contribute greatly to the difference in rotational velocity. Thick disks rotate slower than thin disks because some of them were formed with random-dominated kinematic

velocity lag fraction for the in situ formed stars and the age of the thick disk with a correlation coefficient of 0.6. The color in panel (a) represents the stellar mass of the NH galaxies at z = 0.3, which does not seem to have much to do with the velocity lag fractions or the age of the thick disks.

As seen in Figure 6, stars formed before the disk settling have lower V_{rot} , probably because they were formed during chaotic mergers with less ordered motions. To find out when the galaxies start predominantly forming stars in the disk with ordered motions, we measure when the disk structures begin to appear in the NH galaxies (the disk settling epoch, $z_{\text{disk settling}}$).

As described above, we used a V/σ criterion to identify the $z_{\text{disk settling}}$, and panel (b) shows the $z_{\text{disk settling}}$ of the NH galaxies as a function of their stellar mass at z = 0.3. We find the trend that more massive galaxies tend to settle their disks earlier than less massive galaxies, which is consistent with the trend found in observations (e.g., Kassin et al. 2012). A detailed analysis of the disk settling will be addressed in a separate paper. As a sanity check, we also measure the epoch when the galaxies start to form disk stars predominantly. We define the "disk-mode" star formation as when more than 80% of the newly formed young stars (<100 Myr) are disk stars

(defined as the stars with $\epsilon > 0.5$) and measure the first moment when this disk-mode star formation lasts for 150 Myr, $z_{\text{disk-mode SF}}$. This $z_{\text{disk-mode SF}}$ is represented as the color of each symbol, and it seems that this agrees well with the $z_{\text{disk settling}}$ defined using gas V/σ .

One of the mechanisms behind the velocity lag fraction for the stars formed in situ after $z_{\text{disk settling}}$ would be disk heating. Several sources of heating have been suggested, including mergers (e.g., Quinn et al. 1993) as an external source and spiral arms (e.g., Sellwood & Carlberg 1984) and giant molecular clouds (e.g., Spitzer & Schwarzschild 1951) as internal sources. In panel (c), we plotted the velocity lag fraction for the stars formed in situ after $z_{\text{disk settling}}$ as a function of the fraction of the stars accreted after $z_{\text{disk settling}}$ in the total number of stars in a galaxy. The color of each symbol shows the change in the orbital circularity of the in situ thick disk stars between their birth and the final epoch (z = 0.3), $\langle \epsilon_{\text{birth}} \rangle - \langle \epsilon_{\text{final}} \rangle$. Broadly, thick disks in the NH galaxies with a high velocity lag fraction tend to have much less aligned orbits than at birth. We also find that there is a slight hint of correlation (with a correlation coefficient of 0.59) between the ex situ star fraction, since disk settling and the velocity lag fraction measured for the stars formed in situ after $z_{\text{disk settling}}$. This suggests that mergers contribute to disk heating as an external heating source. However, this does not preclude the possibility of heating caused by secular evolution, as the trend shown in panel (c) is not strong, and when mergers or interactions occur, they often trigger star formation, which contributes to promoting heating by internal sources as well.

Finally, in panel (d), we measured how many of the thick disk stars formed in situ are formed after the disk settling, $f_{\text{in situ, after disk settling}}$, and compare it with the fraction of thick disk stars formed in situ with orbital circularity higher than 0.8, $f_{\text{in situ}, \epsilon_{\text{birth}} > 0.8}$. We find that there is a strong correlation between them. This means that most of the thick disk stars formed after disk settling are born as kinematically thin disk stars $(\epsilon_{\text{birth}} > 0.8)$. In the NH galaxies, a significant fraction of the in situ thick disk stars are born after the disk settling (mean $\langle f_{\rm in\,situ,after\,disk\,settling} \rangle = 0.48$) and as kinematically thin disk stars (mean $\langle f_{\text{in situ},\epsilon_{\text{birth}}>0.8} \rangle = 0.53$). The color of each symbol indicates the $z_{\text{disk settling}}$ of each galaxy; in galaxies that developed their disks earlier, a larger fraction of the stars in the thick disk were formed as kinematically thin disk stars. It should, however, be noted that the fraction of the in situ formed stars after disk settling that comprises the thick disk (in panel (d)) varies from 10% to 95% depending on the details of the star formation and merger accretion history. Therefore, it is important to secure a good number of sample galaxies to derive a representative picture of the disk formation.

3.2.3. Decomposition Results: Properties at Birth

In the previous section, we quantified the difference in rotation speed between the two disks extracted from the two nonoverlapping disk regions of the galaxies. In light of exploring whether they are distinct components put in place by different mechanisms, here we explore the properties of the stellar particles in the two components at birth: their kinematic properties at birth and their birthplaces. For the GALACTICA galaxy, Figure 8(a) shows the final (z = 0) position of the stellar particles in the two components selected by the definition ($R_{xy} = 2 R_d \pm 1 \text{ kpc}$; thin disk: $|Z| < 0.8 z_{cross}$; thick disk: $1.2 z_{cross} < |Z| < 2 z_{thick}$). The magenta circles show the median

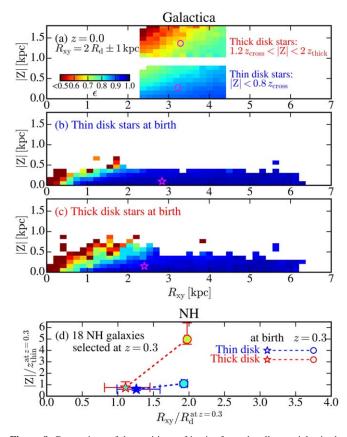


Figure 8. Comparison of the positions of in situ formed stellar particles in the thin and thick disks at the final epoch and at their birth. (a) Final position (at z = 0.0) of the stellar particles in the thin and thick disks of the GALACTICA galaxy, selected by the definition $(R_{xy} = 2 R_d \pm 1 \text{ kpc}; \text{ thin disk: } |Z| < 1 \text{ selected}$ 0.8 z_{cross} ; thick disk: 1.2 $z_{\text{cross}} < |Z| < 2 z_{\text{thick}}$). The position of the stellar particles in the thin/thick disk components at the time of birth is shown in panels (b) and (c). Only the pixelated regions containing more than 0.1% of the total number of stellar particles in each component are displayed. Each pixel is color-coded by the mean orbital circularity (ϵ) of the stellar particles in each region. Panel (d) shows the median changes in the positions of the thin and thick disks for the 18 NH galaxies at z = 0.3. The blue/red circles present the final (z = 0.3) positions of thin/thick disks, while the blue/red stars indicate their birthplaces. To consider different sizes/masses of the NH sample galaxies, we normalized the projected radial distance of each galaxy by the scale length of its disk and the vertical distance by the scale height of the thin disk. We find that a significant fraction of the thick disk stars were spatially and kinematically thinner at birth.

positions (in the plane of R_{xy} and |Z|) of the stellar particles in the two selected components. The color represents the median orbital circularity (Abadi et al. 2003) of the stellar particles residing in each region.

The birth positions of the stellar particles belonging to the thin and thick disks (separated at z = 0.0) are shown in panels (b) and (c). Note that only the stellar particles formed in situ are taken into account when tracking their birthplaces. Only regions containing more than 0.1% of the total number of stellar particles in each component are displayed. The magenta star in each panel points to the median birth position of each component. The stellar particles in both components formed over a wide range of radial distances, and most of them were formed in the inner regions ($R_{xy} = 2-3$ kpc; magenta star) and have migrated outward to the final radial distance ($R_{xy} = 3.4$ kpc). Also, the majority of them formed close to the galactic midplane (|Z| < 0.5 kpc), and they were kinematically much

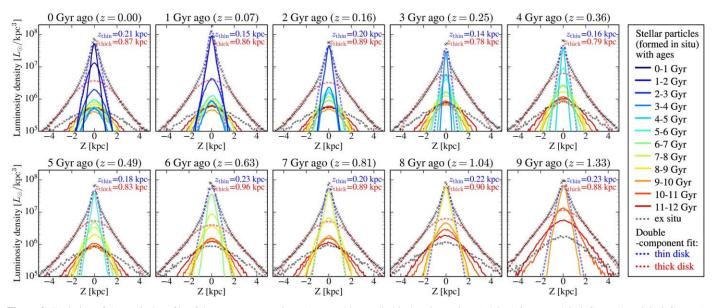


Figure 9. Evolution of the vertical profile of the GALACTICA galaxy (measured in a cylindrical region at $2 R_d \pm 1$ kpc) from z = 1.3 (9 Gyr ago) to 0.0 (0 Gyr ago). The vertical luminosity density is plotted as black crosses. Each solid line shows the vertical distribution of each mono-age group of stellar particles formed in situ. The gray dotted line is the distribution of stellar particles formed ex situ. The double-component fitting to the vertical profile is represented as dashed blue (thin disk) and red (thick disk) lines. The resulting scale heights of the thin and thick disks are displayed on the top of each panel. At all redshifts, the thin disk is dominated by the younger population, while each mono-age population gets thicker and fainter with time, building up the thick disk.

thinner at birth, with an orbital circularity (ϵ) close to 1 (represented as bluer colors).

Figure 8(d) shows the median changes in the positions across the thin and thick disks in the 18 NH galaxies selected at z = 0.3. The blue/red circles are the final (z = 0.3) positions of the stellar particles in the thin/thick disks, and the blue/red stars show where these same stellar particles were formed. To account for the different sizes of the sample galaxies, we normalized their radial distances by the scale lengths of the disk at the final epoch (i.e., R_{xy}/R_d) and the vertical distances by the scale heights of the thin disk measured at z = 0.3 (i.e., $|Z|/z_{\text{thin}}$). The error bars in the x- and y-axes also indicate the 16th-84th percentiles of the radial distances and the vertical distances of the 18 NH galaxies. We find a consistent result for both the GALACTICA and NH galaxies. Both thin and thick disk stars were born close to the galactic center and the midplane and migrated outward and upward (in this diagram). As the bulk of the stellar particles in the two components moves outward and upward, their orbits become less aligned (see the color change of the symbols between the time of birth and z = 0.3). This suggests that the spatially thicker disk in most NH galaxies was not formed by a distinct mechanism but a result of the time evolution of the stars that were born in a thinner distribution with nearly circular orbits.

3.2.4. Decomposition Results: Summary

In Section 3.2, we focused on the difference in various properties between the two spatially separated components. We found that both thin and thick disks are dominated by in situ formed stars, although thick disks have a higher fraction of stellar particles formed ex situ. Thus, the accretion scenario for the thick disk formation is less favored by our simulations. We also showed that thin disks are younger, metal-richer, and rotating faster than thick disks, which is qualitatively consistent with observations. In particular, the important difference between the thin and thick disks is the age distribution of the in situ stars; while many of the thin disk stars formed recently with rotation-dominated kinematics, the thick disk stars are much older and rotating slower. This is because approximately half of the in situ thick disk stars were formed with dispersiondominated kinematics before the galaxies developed their disks, possibly during the mergers (e.g., Brook et al. 2004), and the other half were formed on the disk but slowed down by heating (e.g., Quinn et al. 1993). However, the exact contribution of each process varies greatly across the galaxies and depends on the detailed star formation and merger history. In addition, we explored the distribution and kinematic properties of the stellar particles in the two disks at birth. We found that a significant part of the thick disk was spatially and kinematically thin at birth. All in all, this suggests that the two disks are not entirely distinct components in terms of formation process but rather snapshots in time and space of the continuous evolution of a galactic disk. In the next section, we will investigate the evolution of the disks and discuss their origins.

4. Evolution of the Vertical Structure of Disks

Many theoretical studies have pointed out that galactic disks grow in an "inside-out" and "upside-down" fashion (e.g., Bird et al. 2013, 2020; Stinson et al. 2013; Martig et al. 2014a; Minchev et al. 2015). A galaxy forms a much thinner (in vertical) and more extended (in radial) disk with time, as gas settles into a galaxy. In this context, to further understand the origin of the two disks derived from fitting the vertical profiles, this section will focus on how the disk vertical structures evolve with time. We divide the stellar particles formed in situ into different age groups and see the change in the spatial distribution of each mono-age group.

4.1. Stellar Vertical Profile Evolution: Galactica

Figure 9 shows how the vertical distributions (measured in the cylindrical region at $2R_d \pm 1$ kpc at each redshift) in the *r*

band change over time in the GALACTICA galaxy. Each panel shows the vertical profile at the corresponding epoch, represented as black crosses. The dotted gray lines represent the vertical distributions of stellar particles formed ex situ, which are much thicker compared to the in situ stellar distributions and do not change much over time. The distribution of the mono-age populations formed in situ, indicated as solid lines, becomes thicker with time. As a result, at z = 0, younger stellar particles (bluer lines) appear to have shorter scale heights than older stellar particles (redder lines). The increasing scale height with stellar age is also found in many previous simulation studies (e.g., Martig et al. 2014a; Ma et al. 2017; Buck et al. 2020), and this trend is also clearly visible among the mono-abundance populations in the MW (e.g., Bovy et al. 2012).

For a better visual guide, we measured the scale height of each mono-age population at each epoch using a single sech² function and traced it with time in Figure 10(d). Note that all of the scale heights in this plot are measured in the cylindrical region at $2R_d \pm 1$ kpc for the galaxy at each redshift to consider the size evolution of the galaxy. The evolution of the disk scale length (R_d) is shown in panel (c), and the scale length of this galaxy has not changed much, at least since $z \sim 1.0$ (see Brook et al. 2006). We confirmed that the overall trend remains the same even when we measure all of the scale heights at a fixed cylindrical region (e.g., $R_{xy} = 3.4 \pm 1$ kpc), except for the first two earliest epochs (z > 1.5), at which the galaxy was much smaller. We have adopted the same color key for ages from Figure 9. The scale heights of the thin and thick disks from the double sech² fitting are shown as dashed blue and red lines. We applied the double-component fit only after the galactic disk was developed in a galaxy. The disk settling epoch ($z_{\text{disk settling}}$) is measured by the criterion using the V/σ of cold gas (mean $V/\sigma > 3$ for 150 Myr; see Section 3.2.2 for details), and the evolution of the V/σ of cold gas is shown in panel (b). The epoch of the first emergence of the disk structure in the GALACTICA galaxy is $z_{\rm disk\ settling} \sim 1.7$ ($t_{\rm look\ back} \sim$ 10 Gyr), which is represented as the hatched vertical region. We also added the instantaneous SFR history of the galaxy in panel (a).

The scale height of each mono-age population, represented as colored solid lines in Figure 10(d), increases with time, which is consistent with the kinematic heating of each monoage population after birth (e.g., Bird et al. 2020). The disk heating can be caused by several possible sources, including minor mergers (e.g., Quinn et al. 1993; Kazantzidis et al. 2008) and giant molecular clouds (e.g., Spitzer & Schwarzschild 1951; Aumer et al. 2016). In addition, the distribution of each population not only becomes thicker with time but also gets fainter in the r band with time (fading). This is probably the reason why the slope of the increasing scale height seems to be the steepest right after each mono-age population was born; the distribution appears to be much thicker in luminosity than in mass due to fading. Indeed, we confirm all of the trends in this plot even when tracking the scale heights measured in mass, except that the thickening in the first two time steps becomes slightly smaller.

The youngest stellar particles at each epoch, i.e., the gray solid line in the bottom of Figure 10(d), have a hint of gradually decreasing scale heights with time. The slight upturn in the gray line at $t_{look back} \sim 3-0$ Gyr is due to the close encounter with two satellite galaxies. This encounter also

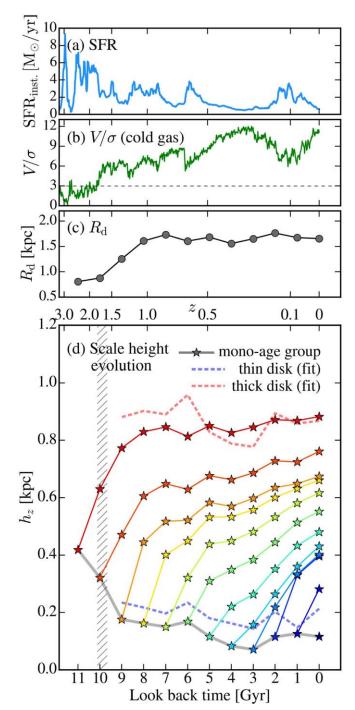


Figure 10. Evolution of the vertical distribution of the disk in the GALACTICA galaxy. (a) Instantaneous SFR as a function of redshift. (b) Evolution of the V/ σ of the cold gas in the galaxy. (c) Evolution of the disk scale length (R_d) of the galaxy. (d) Scale height evolution of mono-age groups of stellar particles, indicated by different colors from red to blue with an age bin of 1 Gyr (same color key as in Figure 9). The vertical distribution is measured at $2 R_d$ of the galaxy at each epoch. The gray solid line connects the scale heights of the youngest stellar particles at each epoch. The dashed blue and red lines are the scale heights (h_z) of the thin and thick disks derived from the doublecomponent fit to the vertical profile measured at each epoch. The vertical hatched region points to $z \sim 1.7$, the time at which the disk structure begins to appear in this galaxy. As the combined result of the thickening of the existing disk stars and the continued formation of young thin disk stars, the vertical distribution (and the scale heights of the thin and thick disks obtained as a result of the fit) does not change much since disk settling. This conspiracy points toward a confounding factor simultaneously regulating star formation and vertical diffusion.

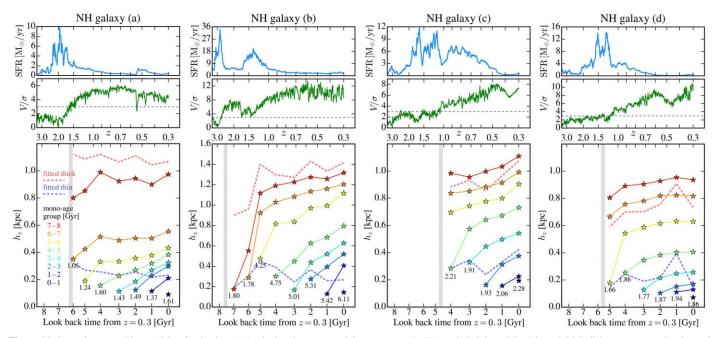


Figure 11. Same format as Figure 10 but for the four NH galaxies down to z = 0.3 as an example. The scale heights of the thin and thick disks are measured at 2 R_d of the galaxy at each epoch, where R_d is the scale length of the disk, which is displayed below the symbols. The thickening of preexisting stars and the formation of young thin disk stars contribute to the vertical distributions; as a result, the scale heights from the fit are broadly consistent, since z = 1 as long as galaxies keep forming young stars without having violent events, such as mergers.

enhances the star formation (panel (a); see also Ruiz-Lara et al. 2020) and at the same time acts as an external heating source. Note the drop of V/σ in panel (b) during the same period.

As the combined result of the thickening of the existing disk stars and the continued formation of young thin disk stars, the vertical profile of the disk itself does not change much over time. Therefore, the fitted scale heights of the thin and thick disks (blue and red dashed lines) remain almost constant since $z \sim 1$ (look-back time ~8 Gyr). This is consistent with the results of other studies (e.g., Brook et al. 2006). Furthermore, Elmegreen & Elmegreen (2006) found from the Hubble Ultra-Deep Field edge-on disk galaxies that their z850-band scale heights are nearly constant over a long period of time (see also Reshetnikov et al. 2019). This conspiracy requires a high degree of synchronization between the efficiency of star formation on the one hand and that of vertical heating on the other.

Recall that star formation efficiency is partially driven by gas turbulence, which is closely impacted by the level of gravitational fluctuations within the disk. As shown in Y. Dubois et al. (2021, in preparation), the cosmic appearance of galactic disks in fact implies a fine-tuning between cooling and heating processes; cosmic evolution promotes a transition toward secularly driven morphology, which steers disks toward an effective Toomre Q parameter (gas+star) close to 1. In turn, the latter becomes an attractor value.¹⁵ In the vicinity of Q = 1, star formation is thus modulated by the dynamically induced level of turbulence in the gas disk. Indeed, several studies have shown that in a marginally stable disk, the velocity dispersion of newly formed young stars correlates with the surface SFR density (e.g., Bird et al. 2020). In parallel, the efficiency of stellar orbital diffusion (combined radial migration and vertical heating) is also amplified by the square of the gravitational

susceptibility (Fouvry et al. 2017) and therefore strongly boosted near marginal stability. The net effect will be the joint recurrent formation of a new population of younger (dynamically cold) stars and the vertical diffusion and radial migration of the older population. This stratifies stars by age vertically while preserving the double-component vertical density profile of the existing disk, as is observed. Proximity to marginal stability is the confounding factor.

4.2. The Evolution of NH Galaxies until $z \sim 0.3$

We have also investigated the evolution of the scale heights of the thin and thick disks and the mono-age groups of stellar particles in the NH disk galaxies down to $z \sim 0.3$. To explore the continuous evolution of the thin and thick disks over a considerable period of time, we selected 12 out of the 18 massive disk galaxies in the NH simulation that developed their disk structures at least by z = 1 ($z_{\text{disk settling}} > 1$) and maintained their disks until z = 0.3 without experiencing violent events, such as significant mergers (with a fraction of ex situ stars accreted after z = 1 lower than 0.1). The purpose of this subsampling is to achieve reliable and stable measurements of disk properties. However, the overall measurements and conclusion stay the same even if we use all 18 galaxies. Since they have a quiescent mass growth history after z = 1, their disk scale lengths have not changed much. The mean change in disk scale length between z = 1 and 0.3 is only 18%.

We found that the scale heights of the thin and thick disks in these 12 galaxies evolve in response to the combined effect of disk thickening (distribution of existing older stars becoming thicker) and continued formation of disk stars in thin distributions. We brought the evolution of the four NH galaxies as examples in Figure 11 in the same format as Figure 10. We measured the vertical scale heights at $R = 2 R_d \pm 1$ kpc at each epoch, and the R_d at each epoch is listed below the symbols. We trace the evolution of the thin and thick disks from the disk

 $[\]frac{15}{15}$ In short, the closer Q is to 1, the shorter the feedback loop timescale and the tighter the loop.

settling epoch measured using the same V/σ (cold gas) criterion.

For the NH galaxy in panel (a), the galaxy started to build up its disk at $z \sim 1.6$ (vertical hatched region), and since then, the scale heights of both the thin and thick disks remain almost constant until $z \sim 0.3$, just like the GALACTICA galaxy presented in Figure 10.

In the case of the NH galaxy in panel (b), its disk has appeared in the galaxy since $z \sim 2.6$, and the two-component fit to the vertical profile yields scale heights of ~ 250 and \sim 850 pc. Then it had two mergers at $z \sim 1.5$ (each with a mass ratio of ~1:10); thus, the SFR soared and the V/σ of the cold gas fell slightly at this epoch. After the merger, the scale heights of both thin and thick disks increased, partially due to the abrupt size growth of the galaxy; the scale length of the disk increased from 1.47 kpc (6 Gyr ago) to 4.25 kpc (5 Gyr ago). Additionally, during this merger epoch, young stars were formed in a slightly thicker distribution out of more turbulent gas. However, since $z \sim 1$, there is no significant merger that could disrupt the disk or lead to any dramatic change in size or other galaxy properties. Hence, the scale heights of both the thin and thick disks do not change much until $z \sim 0.3$. Also, the disk scale length increases by only 30% during this period (from 4.75 to 6.11 kpc).

The same scenario applies to the NH galaxy in panel (c). The scale heights are nearly constant between $z \sim 1$ (after the galaxy developed its disk structure) and 0.5. For the last 2 Gyr, however, the scale heights of both disks have increased, as the galaxy does not form many young stars in this period; without the contribution of newly formed young stars to the total luminosity close to the midplane, the *r*-band vertical distribution only gets thicker with time. The extreme case is the NH galaxy in panel (d), where the galaxy has been nearly quenched since $z \sim 0.6$. Between 1 and 2 Gyr ago, the overall vertical distribution became thicker and smoother. Only recently did the galaxy form a small number of new stars, and the thin disk with a sharp vertical distribution near the galactic midplane began to appear again, reducing both scale heights (see the two dashed lines).

Figure 12 summarizes the scale height evolution of the 12 NH galaxies. The scale heights of the thin and thick disks remain virtually constant for the last 4 Gyr between z = 1.0 and 0.3 (i.e., roughly 8 Gyr in look-back time from the present epoch). This is consistent with the result from the GALACTICA galaxy in the previous section. It seems that the vertical distribution of the disks in a galaxy and the scale heights of the two components from the fit do not change much since the disk settling epoch, provided that the galaxy does not experience serious external disturbances but rather maintains star formation activity. Secular processes have taken over and regulate star formation and heating jointly, so as to maintain both scale heights.

It should be noted that numerical simulations are affected by the reliability of numerical computations. It is not entirely clear how numerical effects contribute to the disk heating (e.g., House et al. 2011). We can probably say that our simulations suffer less than many previous ones, considering the substantially improved spatial and mass resolutions. Besides, most of the recent simulations seem to agree on the importance of heating in the disk evolution (e.g., Aumer et al. 2016; Grand et al. 2016).

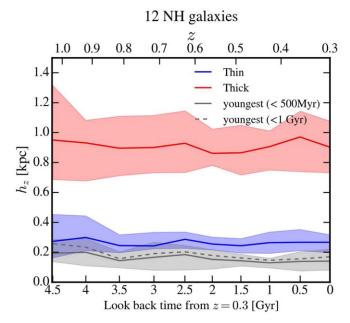


Figure 12. Time evolution of the median vertical scale heights of the thin (blue) and thick (red) disks in the 12 NH galaxies from z = 1 to 0.3 (roughly 4–8 Gyr ago in look-back time from z = 0.0). The shaded regions indicate the 16th– 84th percentiles of the vertical scale heights at each epoch. We selected 12 out of 18 disk galaxies in NH, which have settled their disks at least by z = 1 and maintained their disks without experiencing significant mergers (where the fraction of ex situ stars accreted after z = 1 is lower than 0.1). The scale height of the youngest (<0.5 or <1.0 Gyr) stars at each epoch is also displayed as a gray solid or dashed line for reference. We find no time evolution (at least since z = 1) in the vertical distribution (and, thus, the scale heights from the fit) of the galaxies with a quiescent growth history.

5. Summary and Conclusion

The goal of this study was to see whether the spatially defined thin and thick disks derived from the vertical profile of a galaxy are distinct components formed by different formation mechanisms. We used 18 massive disk galaxies (with $M_{\text{stellar}} > 10^{10} M_{\odot}$) from the NH simulation that reached z = 0.3 and one disk galaxy (with $M_{\text{stellar}} = 2.75 \times 10^{10} M_{\odot}$) from the GALACTICA simulation that reached z = 0.0. These simulations have unprecedentedly high spatial resolution (aimed to reach $\Delta x \sim 34$ pc at z = 0.0) for a relatively large volume simulation (NH), which makes them ideal to investigate the detailed structures of galaxies. The results of this study can be summarized as follows.

- 1. We applied the widely accepted two-component fit to the *r*-band vertical profiles, and the thin and thick disks were reasonably well reproduced in our GALACTICA and NH simulations. The scale height/luminosity ratios between the thin and thick disks in the simulated galaxies, obtained from the fitting, are broadly consistent with observations.
- 2. We spatially decomposed the thin and thick disks and compared the properties of stellar particles in the two components (Table 1). Thick disks have a higher contribution of stellar particles formed ex situ, but both thin and thick disks are still dominated by in situ formed stars. The thin disks in our simulated galaxies are younger, metal-richer, and rotating faster, which is qualitatively consistent with observations. We found that different age distributions of the in situ formed stars in the

thin and thick disks contribute most to the different kinematics between the two components; while thin disks mostly consist of young stars with highly rotationdominated kinematics, thick disk stars are much older and rotating slower because some of them were formed with dispersion-dominated kinematics before disk settling, and others formed on the disks were also slowed down by heating. Roughly half of the in situ thick disk stars are formed on the disk after disk settling, but the exact number depends on the detailed star formation and merger history of galaxies.

- 3. We traced the birthplace of stellar particles in each component and their kinematic properties at birth. We found that a large number of the thick disk stars were spatially (formed close to the midplane) and kinematically (formed with higher orbital circularity) much thinner at birth. This suggests that the two disks are not entirely distinct in terms of formation process but rather are snapshots in time and space of the continuous evolution of a galactic disk.
- 4. Tracking the distribution of the mono-age populations, we found that the two-component disk (from the fit) is the result of the evolution of the disks where the galaxy continues to form young thin disk stars, while at the same time, the preexisting disks get thicker with time due to orbital diffusion. As a result of the two effects, in most cases, the vertical distributions (scale heights) have not changed much since $z \sim 1$, as long as the galactic disks are in place and galaxies keep forming young stars without having violent events, such as mergers. The confounding factor tuning both the star formation of young (thin disk) stars and the rate of vertical diffusion is the $Q \sim 1$ attractor value (Y. Dubois et al. 2021, in preparation), which accelerates both processes.

One important characteristic of thick disks that we have not directly covered in this study is their alpha abundances. It seems well established from many observations that MW disk stars show a bimodal distribution in the plane of $[\alpha/Fe]$ -[Fe/H], which is often associated with the thin and thick disks (e.g., Lee et al. 2011; Anders et al. 2014; Bensby et al. 2014; Duong et al. 2018; Mackereth et al. 2019). Also, there have been many studies using cosmological simulations of individual galaxies to explain the origin of this bimodality (e.g., Brook et al. 2012; Agertz et al. 2020; Buck 2020; Grand et al. 2020; Renaud et al. 2020). Since the simulations we used for this study did not trace the alpha elements separately, we instead investigated the age distribution of the stars in the thin and thick disk regions and found that the two distributions appear to be different; for example, in Figure 5, the age distribution of the thin disk stars is skewed toward younger ages (0-2 Gyr), while most of the thick disk stars were formed much earlier (8-12 Gyr ago). So, it is important to note that, in terms of age (and thus formation epoch, and probably alpha abundances as well), the two disks are distinct.

However, what we found in our study is that their formation processes are not distinct; both disks are mostly formed in situ, and most of the stars in the thick disks were formed as thinner components when they were younger. They later evolved (migrated through heating) to become thicker components. In this regard, the two spatially separated components cannot be directly compared with the chemically distinct sequences in the plane of $[\alpha/Fe]$ –[Fe/H]. While chemically defined sequences (whether stars are in an alpha-poor or alpha-enhanced sequence) are imprinted at birth (formation), spatially defined components) are the result of both formation *and* evolution.

We started this investigation by assuming that a break in the vertical mass or luminosity profiles of a disk galaxy indicates the presence of two separate components in the disk, i.e., thin and thick disks. Our simulations, however, show that spatially defined thin and thick disks are not entirely distinct components in terms of formation process. Rather, they are two parts of a single continuous disk component that evolves with time as a result of the continued star formation of thin disk stars and disk heating.

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Appendix

In this appendix, we summarize the properties of the GALACTICA and the NH galaxies used in this study in Table A1.

 Table A1

 Properties of the GALACTICA (z = 0.0) and NH (z = 0.3) Galaxies

Galaxy ID ^a	M_{stellar}^{b} (×10 ¹⁰ M_{\odot})	$R_{\rm d}^{\rm c}$ (kpc)	R_{90}^{d} (kpc)	$V_{\rm circ}^{\rm e}$ (km s ⁻¹)	B/T^{f}	$z_{\rm thick}/z_{\rm thin}^{\rm g}$	$L_{ m thick}/L_{ m thin}{}^{ m h}$	$z_{disk settling}^{i}$	f _{contam.} j (%)
GALACTICA ^k	2.8	1.7	8.0	192	0.24	4.06	$0.15\substack{+0.07 \\ -0.08}$	1.7	0.00
NH 1 ¹	7.7	6.1	22	252	0.21	5.30	$0.20\substack{+0.23\\-0.10}$	2.6	0.00
NH 2	5.4	0.8	8.0	246	0.32	3.97	$0.20\substack{+0.06\\-0.11}$	1.9	0.00
NH 3	5.3	4.0	23	204	0.21	4.45	$0.12\substack{+0.14\\-0.04}$	2.1	0.00
NH 4 ^m	3.6	2.3	11	181	0.19	2.54	$0.44_{-0.11}^{+0.20}$	1.1	0.00
NH 5	2.7	2.3	9.1	185	0.20	2.72	$0.39\substack{+0.11\\-0.15}$	1.3	0.01
NH 6	2.6	2.6	12	181	0.21	5.49	$0.39\substack{+0.29\\-0.23}$	2.4	0.00
NH 7 ⁿ	2.4	1.9	7.9	174	0.21	4.85	$1.48_{-0.97}^{+0.44}$	1.3	0.06
NH 8	2.2	1.8	12	169	0.29	3.58	$0.08\substack{+0.07\\-0.02}$	1.1	0.00
NH 9	1.8	3.4	17	137	0.14	3.80	$0.70_{-0.32}^{+0.40}$	1.2	0.00
NH 10	1.5	1.5	8.7	139	0.22	3.46	$0.13_{-0.06}^{+0.04}$	0.9	0.07
NH 11 ⁰	1.5	1.6	6.5	168	0.39	4.58	$0.32\substack{+0.22\\-0.16}$	1.6	0.00
NH 12	1.3	1.5	7.5	140	0.29	2.69	$0.17\substack{+0.06\\-0.06}$	1.1	0.01
NH 13	1.3	3.0	11	139	0.15	2.91	$0.34_{-0.13}^{+0.14}$	2.5	0.00
NH 14	1.2	3.0	13	119	0.22	3.45	$0.69^{+0.53}_{-0.23}$	0.8	0.00
NH 15	1.1	2.0	9.2	143	0.20	3.45	$0.50_{-0.26}^{+0.14}$	1.2	0.06
NH 16	1.1	3.5	13	116	0.20	5.41	$0.43_{-0.26}^{+0.27}$	0.6	0.00
NH 17	1.1	1.3	10	130	0.32	3.27	$0.55_{-0.28}^{+0.12}$	1.0	0.00
NH 18	1.0	2.1	9.6	133	0.22	2.66	$0.30\substack{+0.06\\-0.12}$	1.1	0.00

Notes.

^a Galaxy IDs: NH galaxies are listed in descending order of stellar mass.

^b M_{stellar} : stellar mass of galaxies.

^c $R_{\rm d}$: disk scale length of galaxies.

^d R_{90} : radius containing 90% of total stellar mass.

^e V_{circ} : circular velocity of galaxies measured at R_{90} .

f B/T: bulge-to-total ratios, where the "bulge" mass is defined as twice the mass sum of the stellar particles with $-0.5 < \epsilon < 0$.

 $z_{\text{thick}}/z_{\text{thin}}$: scale height ratios between the thin and thick disks.

^h $L_{\text{thick}}/L_{\text{thick}}/L_{\text{thick}}$ luminosity ratio between the two disks in |Z| < 1 kpc with errors showing from the ratios measured at the galactic midplane (|Z| = 0 kpc) and in the regions $|Z| < 2 z_{\text{thick}}$.

 $i_{\text{Zdisk settline}}$ disk settling epoch, defined as the time when the mean V/σ of the cold gas inside the R_{90} of a galaxy for the past 150 Myr reaches higher than 3.

 f_{contam}^{j} : number fraction of low-resolution dark matter particles inside the halos in percentages.

^k GALACTICA is investigated at z = 0.0.

¹ NH galaxy (b) in Figure 11.

^m NH galaxy (c) in Figure 11.

ⁿ NH galaxy (d) in Figure 11.

^o NH galaxy (a) in Figure 11.

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