# PUSHing Core-collapse Supernovae to Explosions in Spherical Symmetry. V. Equation of State Dependency of Explosion Properties, Nucleosynthesis Yields, and Compact Remnants 

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#### Abstract

In this fifth paper of the series, we use the parameterized, spherically symmetric explosion method PUSH to investigate the impact of eight different nuclear equations of state (EOS). We present and discuss the explosion properties and the detailed nucleosynthesis yields, and predict the remnant (neutron star or black hole) for all our simulations. For this, we perform two sets of simulations. First, a complete study of nonrotating stars from 11 to $40 M_{\odot}$ at three different metallicities using the SFHo EOS; and, second, a suite of simulations for four progenitors ( $16 M_{\odot}$ at three metallicities and $25 M_{\odot}$ at solar metallicity) for eight different nuclear EOS. We compare our predicted explosion energies and yields to observed supernovae and to the metal-poor star HD 84937. We find EOS-dependent differences in the explosion properties and the nucleosynthesis yields. However, when comparing to observations, these differences are not large enough to rule out any EOS considered in this work.


Unified Astronomy Thesaurus concepts: Core-collapse supernovae (304); Neutron stars (1108); Black holes (162); Explosive nucleosynthesis (503)
Supporting material: machine-readable table

## 1. Introduction

When massive stars ( $\gtrsim 8 M_{\odot}$ ) reach the end of their hydrostatic lives, they undergo gravitational collapse of their core. This collapse can result in a spectacular explosion, called a core-collapse supernova (CCSN), which disrupts all but the very core of the star and leaves behind a neutron star (NS). In these bright and energetic events many chemical elements are synthesized and subsequently ejected in the explosion, thus enriching the surrounding gas with "metals" (elements heavier than He). For some stars, the gravitational collapse of the core cannot be turned around into a successful explosion. Instead, they fail to explode and ultimately form black holes (BHs). Exactly which stars successfully explode and which stars fail to explode remains an open question. Moreover, the exact explosion mechanism (by which the stalled shock resulting from the core collapse is revived) is still not fully understood, despite decades of efforts.

The CCSN problem is complex, requiring the inclusion of general relativity, (magneto)hydrodynamics, neutrino transport, and physics of nuclear matter at high densities in simulations. Additionally, CCSNe need to be simulated in full threedimensional space. This means that despite considerable progress in model sophistication (see Müller 2020, and references therein for a discussion of the status of explosionengine simulations), CCSN simulations remain computationally expensive endeavors which are not suitable for large-scale investigations of tens to hundreds of models. Here, we use a complementary approach which allows us to more systematically study the effects of one of the crucial-and poorly known-ingredients: the nuclear equation of state (EOS).

[^0]The mass-radius relationship of NSs is one method to constrain the nuclear EOS (see Miller et al. 2019, 2021, Riley et al. 2019, 2021, Raaijmakers et al. 2020, and Pang et al. 2021 for some recent examples). Combining the laboratory measurement of the neutron skin at PREX-II with pulsar timing observations in the radio and X-ray and using a Bayesian statistics approach led to complementary constraints on the mass-radius relationship (Biswas 2021). Additional constraints can be derived from the detection of a binary NS by LIGO/ VIRGO (Abbott et al. 2017a) and from the kilonova and the gamma-ray burst afterglow (Abbott et al. 2017b).

There exist several studies in the literature with a focus on the nuclear EOS in CCSNe. For example, Schneider et al. (2019) constructed a series of finite-temperature EOS for different effective nucleon masses and investigated their impact on the collapse of a $20 M_{\odot}$ star in spherical symmetry and in an octant-3D simulation. They conclude that a larger effective mass, while keeping all other parameters in the EOS fixed, leads to larger neutrino heating and hence an increased likelihood for explosion. A similar result was found by Yasin et al. (2020), using spherically symmetric simulations with an increased heating factor to achieve explosions. During the revision of this paper, a study conducted in spherical symmetry by Boccioli et al. (2022) found that the EOS which generates higher central entropy soon after bounce produces a faster and stronger explosion. In axisymmetric simulations with Boltzmann transport, the different nuclear composition due to different EOS models resulted in different energy losses due to photodissociation, leading to an explosion in one case and no explosion in the other case (Harada et al. 2020). In a 3D simulation of a $18.8 M_{\odot}$ star, the shock runaway occurs earlier for a hotter proto-neutron star (PNS), which has higher neutrino luminosities and harder neutrino spectra (Bollig et al. 2021). The amount of (neutrino-driven) mass ejection in failed supernovae carries the imprint of the stiffness of the nuclear EOS (Ivanov \& Fernández 2021). The neutrino signal from
failed supernovae can be used to constrain the temperaturedependence of the nuclear EOS (da Silva Schneider et al. 2020). The impact of the nuclear EOS can also be seen in the gravitational wave (GW) signal from CCSNe. In particular for fast rotating stars, the early GW signal has some EOS dependency (Richers et al. 2017). While all of these studies found some effect due to the properties of the nuclear EOS used, no truly systematic investigations have been undertaken.

This work builds upon a series of investigations using the PUSH method. The PUSH method is an effective method which is built upon the neutrino-driven mechanism for the central engine of CCSNe. The main idea of the PUSH method is to mimic the enhanced neutrino energy deposition as observed in multidimensional simulations in computationally more efficient, spherically symmetric simulations. The PUSH method was first introduced in Perego et al. (2015; hereafter Paper I) and subsequently refined in Ebinger et al. (2019; hereafter Paper II). The PUSH method has been used to study the explosion and remnant properties of solar metallicity progenitors in Paper II and of low- and zero-metallicity progenitors in Ebinger et al. (2020; hereafter Paper IV). We presented the detailed nucleosynthesis yields from PUSH models in Curtis et al. (2019; hereafter Paper III) for solar metallicity models and in Paper IV for low- and zerometallicity models. The light curves and time-dependent spectra have been calculated and analyzed for all exploding models across all metallicities in Curtis et al. (2021). All of these studies have been performed using the HS(DD2) nuclear equation of state (Hempel \& Schaffner-Bielich 2010).
In this paper, we investigate how the explosion properties, remnant properties, and nucleosynthesis yields depend on the nuclear EOS. For this, we have selected six nuclear EOS models which can accommodate a maximum NS mass of $>2$ $M_{\odot}$ : the SFHo and SFHx from Steiner et al. (2013); the HS(DD2), HS(TM1), and HS(NL3) from Hempel \& SchaffnerBielich (2010) and Hempel et al. (2012); and the BHB $\lambda \phi$ EOS model from Banik et al. (2014). In addition, we include two EOS models commonly used in the literature: LS220 (Lattimer \& Douglas Swesty 1991) and that of Shen et al. (1998a, 1998b) for comparison.

This article is organized as follows. In Section 2 we discuss our setup for this study, including the input models and the nuclear EOS models. In Section 3 we present the key findings on the explosion properties when using the SFHo EOS model. We then investigate the trends for all eight nuclear EOS models for three $16 M_{\odot}$ progenitors at different metallicities and a 25 $M_{\odot}$ progenitor at solar metallicity in Section 4. Section 5 discusses the nucleosynthesis yields and trends across compactness and progenitor metallicity for the SFHo EOS. We compare our results with observations of supernovae and with abundances observed in metal-poor stars in Section 6. Finally, we present the resulting NS and BH distributions for the SFHo EOS. We summarize the work in Section 8.

## 2. Models and Input

### 2.1. Hydrodynamics and Neutrino Transport

We simulate the collapse, bounce, and postbounce evolution using the same setup as in our previous works (Paper II, Paper III, and Paper IV) except for the nuclear equation of state (see Section 2.2). Hence, we only summarize here the key points relevant to this study. We solve the general relativistic
hydrodynamic equations in spherical symmetry using AGILE (Liebendörfer et al. 2002), which features an adaptive grid and implicit time evolution. We apply the deleptonization scheme from Liebendörfer (2005) during the collapse phase. For electron flavor neutrinos $\left(\nu_{e}\right)$ and antineutrinos $\left(\bar{\nu}_{e}\right)$, we use the isotropic diffusion source approximation (IDSA) scheme of Liebendörfer et al. (2009). For heavy-lepton flavor neutrinos and antineutrinos ( $\nu_{x}=\nu_{\mu}, \bar{\nu}_{\mu}, \nu_{\tau}, \bar{\nu}_{\tau}$ ) we use an advanced spectral leakage (ASL) scheme (Perego et al. 2016). More details of the individual components of our code can be found in Ebinger et al. (2019).

To achieve explosions in otherwise not exploding models in spherical symmetry, we use the PUSH method introduced in Paper I and Paper II. PUSH is a physically motivated, effective method that mimics in spherical symmetry the enhanced heating (due to convection and accretion) observed in multidimensional simulations. A fraction of the heavy-flavor neutrino energies is deposited behind the shock via a parameterized heating term $Q_{\text {push }}^{+}(r, t)$ (see Equation (4) in Paper I). This heating includes a spatial term (so that the extra heating only occurs where electron neutrinos and antineutrinos are heating), a temporal term (which includes the free parameters $k_{\text {push }}$ and $t_{\text {rise }}$ ), and a dependence on the spectral energy flux of a single heavy-lepton neutrino flavor.

For the calibration of the free parameters in the PUSH method, we follow Paper IV and use the standard calibration presented in Paper II. In this calibration, $t_{\text {rise }}=400 \mathrm{~ms}$ and $k_{\text {push }}(\xi)=a \xi^{2}+b \xi+c \quad$ (where $a=-23.99, \quad b=13.22$, and $c=2.5$ ) is parameterized as function of the compactness (as introduced in O'Connor \& Ott 2011):

$$
\begin{equation*}
\xi_{M}=\frac{M / M_{\odot}}{R(M) / 1000 \mathrm{~km}} . \tag{1}
\end{equation*}
$$

With this setup, we perform hydrodynamic simulations of the collapse, bounce, and postbounce evolution. We use a total of 180 radial zones, which includes the progenitor star up to the helium shell. With the adaptive grid, a greater number of zones are placed in regions where the thermodynamic quantities show steeper gradients. Hence, in the postbounce and explosion phases, the surface of the PNS and the shock are the regions that are better resolved. We follow the evolution for up to 5 s for exploding models. If the shock reaches the edge of the computational domain before then, the simulation is terminated at that time.

We categorize the outcome of each simulation as "exploding model", "failed SN" or "BH formation". For the failed SN and BH -forming models, the simulation time depends on individual models and is not of much importance in this paper. We differentiate a "direct collapse", meaning no stalled shock, and "failed SN", for a stalled shock that never revives, by looking at the central density evolution. If the central density rises very rapidly and reaches more than $10^{15} \mathrm{~g} \mathrm{~cm}^{-3}$ we call it a BH forming model.
The explosion energy and other explosion properties are calculated in the same way as in Perego et al. (2015). The explosion energy is the sum of thermal, kinetic, and gravitational energy integrated over the mass of the star from the outer layers to the time-dependent mass cut. The mass cut at each time step is set at the mass coordinate which has the highest value of explosion energy. The explosion time is obtained from the time after bounce when the shock reaches 500 km .

Table 1
EOS Models Used in this Study

| Label | EOS | Model for Uniform <br> Nuclear Matter | Nuclei | $n_{B}^{0}$ <br> $\left(\mathrm{fm}^{-3}\right)$ | $K$ <br> $(\mathrm{MeV})$ | $J$ <br> $(\mathrm{MeV})$ | $L$ <br> $\left(\mathrm{MeV} \mathrm{fm}^{-3}\right)$ | $m_{n}^{*} / m_{n}$ | $m_{p}^{*} / m_{p}$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | | $M_{\text {max }}$ |
| :---: |
| $\left(M_{\odot}\right)$ | | References |
| :---: |

Note. Saturation density $n_{B}^{0}$, incompressibility $K$, symmetry energy $J$, symmetry energy slope coefficient $L$, effective neutron mass $m_{n}^{*}$, effective proton mass $m_{p}^{*}$, and maximum mass $M_{\max }$ of a cold neutron star. RMF: relativistic mean field. NSE: nuclear statistical equilibrium. CLD: compressible liquid drop. SNA: single-nucleus approximation. TFA: Thomas-Fermi approximation.
References. (1) Steiner et al. (2013), (2) Hempel \& Schaffner-Bielich (2010), (3) Hempel et al. (2012), (4) Banik et al. (2014), (5) Lattimer \& Douglas Swesty (1991), (6) Shen et al. (1998b), (7) Shen et al. (1998a).

### 2.2. Nuclear Equation of State

In this work, we explore eight different nuclear equations of state (listed in Table 1). Six of these EOS models-namely, SFHo, SFHx, HS(TM1), HS(NL3), HS(DD2), and BHB $\lambda \phi-$ are based on the relativistic mean-field (RMF) interaction of nucleons and include a nuclear statistical equilibrium (NSE) distribution of nuclei below saturation densities. These six EOS models differ in the parameterization of the nuclear interaction and the nuclear mass tables used for the experimentally unknown nuclei. All of these EOS models allow for a maximum NS mass above $2 M_{\odot}$. In the following discussions we will reference the EOS models by their names without the HS prefix, e.g., HS(DD2) will be referred to as DD2 (see also the first column in Table 1). In addition, we include two EOS models commonly used in the literature: the LS220 model (Lattimer \& Douglas Swesty 1991) and the Shen-STOS EOS model (Shen et al. 1998a, 1998b). Both of these EOS models also support a maximum NS mass of $\sim 2 M_{\odot}$. The mass-radius relationship at $T=0.1 \mathrm{MeV}$ for all eight EOS models is shown in Figure 1. The horizontal lines are the mass measurement for pulsar PSR J0348 +0432 (Demorest et al. 2010). This was the most massive NS observed. Only very recently (i.e., during the final stages of the work presented here) this has been surpassed by PSR J1810 +1744 , for which Romani et al. (2021) derived a mass of $2.13 \pm 0.04 M_{\odot}$ using spectrophotometry. There are no radius constraints for these pulsars. However, recent NICER observations provide a mass and a radius constraint for two pulsars: PSR J0030 +0451 (Miller et al. 2019; Riley et al. 2019) and PSR J0740 + 6620 (Miller et al. 2021; Riley et al. 2021), shown as crosses in Figure 1.

The SFHo and SFHx parameterizations were developed from the NS mass-radius measurements combined with the charge radii and binding energies of ${ }^{208} \mathrm{~Pb}$ and ${ }^{60} \mathrm{Zn}$ (Steiner et al. 2013). For the experimentally unknown nuclei, the mass table from the finite range droplet model (FRDM) is used. The SFHo EOS is more consistent with the observations of NS mass and radii as well as with theoretical constraints from nuclear experiments on matter near and below saturation density known at the time. The SFHx EOS model is similar to the SFHo EOS model, except that it attempts to minimize the radius of low-mass NSs while remaining consistent with other constraints. The NL3 parameterization uses binding energies and charge radii of 10 nuclei and of neutrons and the mass table


Figure 1. The mass-radius relationship for the EOS models of this work at $T=0.1 \mathrm{MeV}$. The horizontal line with error bars represents the constraint from pulsar PSR J0348 +0432 . The gray shaded line indicates pulsar PSR J1810 +1744 . The crosses represents the mass-radius constraints obtained from PSR J0030 + 0451 (black) and PSR J0740 +6620 (brown). The black dashed line is at $1.4 M_{\odot}$.
from Lalazissis et al. (1999). The TM1 parameterization is similar to NL3. It was fit to charge radii and binding energies of heavy nuclei and uses the mass table of Geng et al. (2005). It differs from NL3 at high densities due to the inclusion of vector self-interactions. Finally, the DD2 and the BLB $\lambda \phi$ EOS models are both based on the DD2 parameterization, which uses experimental nucleon masses and the same FRDM mass table for experimentally unknown nuclei as SFHo and SFHx. The BHB $\lambda \phi$ EOS additionally includes the lambda hyperon and the repulsive hyperon-hyperon interaction (represented by the $\phi$ ). It is important to note that these six EOS models represent six discrete EOS models. While they can be ordered by increasing values of any of the parameters listed in Table 1, they also differ in their other properties, including the parameterization of the nuclear interaction. Hence, one cannot easily make statements about the effect of any of these parameters alone on the explosion properties and the nucleosynthesis yields.

The EOS developed by Shen et al. (1998a, 1998b; "Shen") uses a RMF approach and the Thomas-Fermi approximation for the nuclei. The LS220 EOS developed by

Lattimer \& Douglas Swesty (1991) with the incompressibility parameter $K=220 \mathrm{MeV}$ is based on a nonrelativistic parameterization of the nuclear interactions and the nuclei are calculated in the liquid-drop approach. Both of these EOS models use the single-nucleus approximation, in which the distribution of nuclei at finite temperatures is represented by a single nucleus (SNA). While this approximation does not affect the EOS much (Burrows \& Lattimer 1984), it only describes the composition in an averaged way, which may affect the supernova dynamics.

We also include an extension of the EOS to non-NSE conditions by introducing a transition region. In this region, we apply some parameterized burning for temperatures between 0.3 and 0.4 MeV and introduce a temperature-dependent burning timescale. This transforms the initial non-NSE composition toward NSE. In the non-NSE region, we describe the nuclear composition using 25 representative nuclei which include neutrons, protons, $\alpha$ nuclei, and a few asymmetric isotopes up to iron-group nuclei. We map the abundances of the progenitor to these nuclei in a way that is consistent with the provided electron fraction $Y_{e}$. To have a consistent description of the two regions, we use the same underlying calculations for NSE and non-NSE regimes (Hempel \& Schaffner-Bielich 2010) except for some modifications. We neglect the excited states of nuclei and do not account for excluded volume effects. Also, the nucleons are treated as noninteracting Maxwell-Boltzmann gases. This helps us to get rid of spurious effects in the transition region. However, some differences persist between the two regions because of the limited number of nuclei considered in non-NSE.

### 2.3. Initial Models

We use four series of spherically symmetric, nonrotating progenitor models having three different values of metallicity $\left(Z=Z_{\odot}, Z=10^{-4} Z_{\odot}\right.$, and $\left.Z=0\right)$ and spanning zero-age main sequence (ZAMS) masses from $\sim 11-40 M_{\odot}$. These preexplosion models are taken from Woosley et al. (2002) and Woosley \& Heger (2007) and were generated using the KEPLER evolution code. The progenitor models are labeled by their ZAMS masses with a letter prefix representing the series, and hence the metallicity of the models. For solar metallicity, we use the Woosley et al. (2002) "s-series" model and Woosley \& Heger (2007) "w-series" model. For low metallicity, we use the models from Woosley et al. (2002), which have a metallicity of $10^{-4} Z_{\odot}$ ("u-series"). For zero metallicity we use the models from Woosley et al. (2002) with zero metallicity ("z-series"). All of these models have also been used in Paper II-Paper IV. A complete list of all the preexplosion models used in this study is given in Table 2.

### 2.4. Nucleosynthesis Postprocessing

For the successfully exploding models, we calculate the detailed nucleosynthesis in a postprocessing approach using the nuclear reaction network CFNET (Fröhlich et al. 2006a), as in Paper III and Paper IV. The network includes 2902 isotopes from free nucleons to neutron-rich and neutron-deficient isotopes up to ${ }^{211} \mathrm{Eu}$. We use the reaction rate library REACLIB (Cyburt et al. 2010), which uses experimentally measured reaction rates. For those reactions where experimental rates are not known, REACLIB uses n -, p -, and $\alpha$ capture reaction rates from theoretical predictions of Rauscher \& Thielemann (2000). Our network also includes weak

Table 2
Preexplosion Models Used in this Study

| Series | Label | Min. Mass <br> $\left(\boldsymbol{M}_{\odot}\right)$ | Max. Mass <br> $\left(\boldsymbol{M}_{\odot}\right)$ | $\Delta m$ <br> $\left(\boldsymbol{M}_{\odot}\right)$ | References |
| :--- | :---: | :---: | :---: | :---: | :---: |
| s-series | s | 10.8 | 28.2 | 0.2 | 1 |
|  |  | 29.0 | 40.0 | 1.0 | 1 |
| w-series | w | 12.0 | 35.0 | 1.0 | 2 |
|  |  | 35.0 | 40.0 | 5.0 | 2 |
| u-series | u | 11.0 | 40.0 | 1.0 | 1 |
| z-series | z | 11.0 | 40.0 | 1.0 | 1 |

Note. The s-series and w-series have solar metallicity $\left(Z=Z_{\odot}\right)$. The u-series has subsolar metallicity $\left(Z=10^{-4} Z_{\odot}\right)$. The z-series has zero metallicity ( $Z=0$ ).
References. (1) Woosley et al. (2002), (2) Woosley \& Heger (2007).
interactions, where the electron and positron capture rates are taken from Langanke \& Martínez-Pinedo (2001). The $\beta^{-} / \beta^{+}$ decay rates are obtained from the nuclear database NuDat2 (if available) and Möller et al. (1995). The capture reactions of $\nu$ and $\bar{\nu}$ on free nucleons are also included in our network.

For the postprocessing, we take the ejecta from our hydrodynamic simulations and divide them into mass elements of equal mass $\left(10^{-3} M_{\odot}\right)$. We call each of these mass elements a "tracer". Each tracer has a mass of $10^{-3} M_{\odot}$. The thermodynamic evolution of each tracer particle is known for the duration of the hydrodynamic simulation. As in Paper II and Paper IV, we postprocess only those tracers which reach a peak temperature $\geqslant 1.75$ GK.

For the innermost tracers, the peak temperature is $\geqslant 10 \mathrm{GK}$. We assume NSE condition for these tracers and start the postprocessing when the temperature drops below 10 GK during the expansion. For the tracers that do not reach such high temperatures, we postprocess them from the beginning of the hydrodynamical simulation. In both cases, the initial electron fraction $Y_{e}$ is taken to be the same as the value in the hydrodynamical simulation and then it is evolved in our network consistent with the nuclear reactions.
For tracers where at the end of the hydrodynamic simulation the temperature and density are high enough for nucleosynthesis to occur, we extrapolate these using a free expansion for the density $\rho$ and an adiabatic expansion for the temperature, as in Paper III and Paper IV:

$$
\begin{gather*}
r(t)=r_{\mathrm{final}}+t v_{\mathrm{final}}  \tag{2}\\
\rho(t)=\rho_{\mathrm{final}}\left(\frac{t}{t_{\mathrm{final}}}\right)^{-3}  \tag{3}\\
T(t)=T\left[s_{\mathrm{final}}, \rho(t), Y_{e}(t)\right] \tag{4}
\end{gather*}
$$

where $r$ is the radial position, $v$ the radial velocity, $\rho$ the density, $T$ the temperature, $s$ the entropy per baryon, and $Y_{e}$ the electron fraction of the tracer. The subscript "final" corresponds to the end time of the hydrodynamical simulation. We calculate the temperature at each time step using the EOS from Timmes \& Swesty (2000). We end the nucleosynthesis calculation when the temperature of the tracer drops below 0.05 GK .

## 3. Systematic Explosion Properties from the SFHo EOS

In this section, we present and discuss the explosion properties of our simulations using the SFHo EOS model. As mentioned earlier in Section 2.3, we use progenitors from four


Figure 2. Explosion outcomes for simulations using the SFHo EOS for all four series of progenitor models: s-series $\left(Z=Z_{\odot}\right.$, blue), w-series ( $Z=Z_{\odot}$, green), u-series $\left(Z=10^{-4} Z_{\odot}\right.$, yellow), and z-series $(Z=0$, red). Each colored bar represents an exploding model (leaving behind a neutron star) and each black bar corresponds to a nonexploding model (leaving behind a black hole).
different series with different metallicities, namely the s-, w-, u -, and z -series.

### 3.1. Explosion Outcomes

Figure 2 shows the outcome of our simulations using the SFHo EOS for all four progenitor series. This gives a summary of which models explode and which do not explode. It can be seen from the figure that there is no ZAMS mass which divides the exploding models from the nonexploding models. Instead, there are islands of nonexploding models lying in between exploding ones. This is in agreement with other similar studies using a different nuclear EOS with our PUSH setup (Paper II and Paper IV) or using other effective simulation setups (Ugliano et al. 2012; Pejcha \& Thompson 2015; Ertl et al. 2016; Müller et al. 2016; Sukhbold et al. 2016; Couch et al. 2020; Mabanta et al. 2019).

In Figure 3 we show the explosion energy, remnant mass, and ejecta mass for all the progenitor models used in this work. The colored bars represent the simulations of this work using the SFHo EOS. The histogram indicated by the black line represents the simulations with the DD2 EOS, taken from Paper II (s-series and w-series) and from Paper IV (u-series and z-series), which we include for comparison.

The top four panels show the explosion energy as a function of the ZAMS mass. We obtain explosion energies of $\sim 0.15-1.9 \mathrm{~B}$ (where $1 \mathrm{~B}=1$ Bethe $=10^{51} \mathrm{erg}$ ). Progenitors with very low and very high ZAMS masses and also those which lie next to nonexploding models have the lowest explosion energies. This is in agreement with the results obtained using the DD2 EOS (black lines; see also Figure 12 in Paper II and Figure 3 in Paper IV). Preexplosion models with ZAMS masses around $15 M_{\odot}$ result in the highest explosion energy for the $w-$, $s$-, and $u$-series. For the z-series, the highest explosion energy is obtained for ZAMS masses around $17 M_{\odot}$. The highest explosion energies obtained for the SFHo EOS (1.9 B) is slightly higher than the highest explosion energy for the DD2 EOS. Overall, the simulations using SFHo result in higher explosion energies (up to $15 \%$ ). This is due to the neutrino luminosities being systematically higher for SFHo compared to DD2.

The bottom four panels correspond to the ejecta masses (lighter color) and remnant masses (darker color). For all the
four series, we obtain remnant masses around $1.3-2.0 M_{\odot}$. Overall we make less massive remnants with the SFHo EOS than with DD2. The ejecta masses are computed from the stellar mass at collapse minus the remnant mass, hence they are very similar between simulations with SFHo and simulations with DD2. For all four series, the ejecta mass increases up to $20 M_{\odot}$, beyond which the ejecta mass decreases for the s- and w-series due to line-driven mass loss at solar metallicity. For the $u$ - and z -series the ejecta mass continues to increase with increasing ZAMS mass.

For almost all progenitors, the outcome of stellar collapse is the same for the SFHo EOS and for the DD2 EOS. The exceptions to this are three progenitors (s25.0, s25.2, s39.0) which have a drastically different outcome depending on the nuclear EOS used. We discuss these three models in detail in Section 4.2.

### 3.2. Trends with Compactness

As we have seen in the previous section, the ZAMS mass is not a good indicator for whether a model explodes or not. Here, we look at the outcome of our simulations as a function of compactness $\xi_{2.0}$ at bounce to identify any emerging trends.

In Figure 4, we show the correlation between explosion properties (explosion energy, remnant mass, and explosion time) and the compactness of the progenitor. The colored points present the simulations of this work using the SFHo EOS. The gray points are the equivalent simulations using the DD2 EOS and are taken from Paper II and Paper IV. The explosion energy is highest for models with compactness around $0.2-0.4$ (for SFHo models), and it is lowest for the models with the lowest and the highest compactness values. This trend is the same for all four series of models, and hence independent of the metallicity. Overall, the simulations using the SFHo EOS have slightly higher explosion energies than the simulations using the DD2 EOS (where the peak explosion energies are obtained for models with compactness also between 0.2 and 0.4).

For exploding models, the remnant mass is directly correlated to the compactness of the progenitor. As the compactness increases, so does the mass of the NS formed after core collapse. This trend is independent of which nuclear EOS is used in the simulation. However, the remnant masses from the SFHo EOS are slightly lower than those from the DD2 EOS. Most models that do explode, explode within $0.3-0.5 \mathrm{~s}$ after bounce. The explosion time has a mild parabolic dependence on the compactness, which is inverse of that of the explosion energy. Models with the highest compactness, and also models with the lowest compactness, take the longest to explode. This trend in explosion time is related to our calibration of the PUSH method, and hence is not a true prediction from the simulations. Moreover, the models using SFHo explode earlier than the models using DD2. This, combined with the fact that the models using SFHo explode more energetically than the models using DD2, indicates that the stiffer EOS (DD2) makes it more difficult for models to explode, and hence if the model does explode, it takes more time. For all three quantities, there is no obvious trend with metallicity.

## 4. Explosion Properties from Eight Different Nuclear EOS

In the previous section, we presented the overall trend of the explosion properties of four progenitor series for simulations


Figure 3. Top four panels: explosion energy as a function of the zero-age main sequence (ZAMS) mass. Bottom four panels: remnant mass (solid color) and ejecta mass (lighter shade) as a function of the ZAMS mass for all four series of preexplosion models. The s-series is represented in blue, the $w$-series is in green, the $u$-series is in yellow, and the z -series is in red. Note there is a scale break in the $y$-axis in the bottom four panels to accommodate the different scales of remnant mass and ejecta mass. The colored bars are for SFHo EOS and the histograms given by the black line are for the DD2 EOS from Paper II and Paper IV . The gray bars correspond to nonexploding models.
using the SFHo nuclear EOS and compared them to simulations from previous work using the DD2 nuclear EOS. In this section, we present the results from simulations using a
total of eight different nuclear EOS models. Six EOS models (SFHo, DD2, SFHx, TM1, NL3, and $\mathrm{BHB} \lambda \phi$ ) are described in Section 2.2 and two models (LS220 and Shen) are included for


Figure 4. From top to bottom: explosion energy, neutron star (baryonic mass) and explosion time for the s-series (blue circles), w-series (green stars), u-series (yellow triangles), and $z$-series (red squares) as a function of the compactness $\xi_{2.0 b}$ at bounce. The colored symbols represent results from the SFHo EOS. The results for simulations using the DD2 EOS with the same progenitor sets are shown in gray.
comparison as they are widely used in the literature. Some aspects of the simulations using SFHo are discussed in the previous section. The simulations using DD2 are taken from Paper II, Paper III, and Paper IV. In Section 4.1, we focus on a $16 M_{\odot}$ progenitor at three different metallicities (s16.0, u16.0, and z16.0) and summarize the explosion properties in Table 3. In Section 4.2 we discuss the interesting case of the $25 M_{\odot}$ progenitor at solar metallicity (s25.0).

### 4.1. Trends with Nuclear EOS

In Figure 5 we compare the explosion energy (top) and remnant mass (bottom) for all eight EOS models and three progenitor models. The explosion energy is not correlated with any single parameter of the EOS as given in Table 1. Yasin et al. (2020) found in a study using one parameterization for the nuclear interaction and varying one parameter at the time that
-of the parameters they studied-the effective mass has the largest impact on the explosion properties. For our setup, where the EOS differ in more than a single parameter, we do not find a correlation of the explosion energy with the effective mass, which is not surprising given the different setup. To do a quantitative analysis of the uncertainty from each parameter in the EOS on the explosion properties one would have to use a quite different setup with a continuous parameterization of the EOS (e.g., as suggested in Du et al. 2022). For a given progenitor, the explosion energy varies by $15 \%$ for the s16.0 model, by $17 \%$ for the u16.0 model, and by $18 \%$ for the z16.0 model across all nuclear EOS used here. The remnant mass, however, varies by only $\sim 1 \%$ in all three cases.

### 4.2. Models with EOS-dependent Outcomes

In this section, we discuss the models for which the outcome (explosion or no explosion) depends on the nuclear EOS used in the simulation. As mentioned in Section 3.1 these are three solar metallicity progenitors (s25.0, s25.2, s39.0) with ZAMS mass close to nonexploding models (s24.8, s25.4). All three models have a relatively high compactness ( $\xi_{2.0}>0.6$ ). These progenitors explode with four of the nuclear EOS models (SFHo, SFHx, NL3, and TM1) and with the two commonly used EOS models (LS220 and Shen), while they do not explode with DD2. The evolution is very similar for all three progenitors with mixed outcome. The central density evolves rapidly and then flattens out for all EOS models, which results in a successful explosion. In the nonexploding case (DD2 EOS), the central density keeps rising as a function of time without any hint of turnover. For the $\mathrm{BHB} \lambda \phi$ model, the core undergoes a small second collapse around 1.2 s . Since BHB $\lambda \phi$ is the only EOS considered here which includes hyperons, it is not surprising that the evolution is different compared to the other EOS.
To answer the question of what causes a model to explode or not to explode, we look into the neutrino luminosities and energies for an exploding case (SFHo with PUSH) and two nonexploding cases (DD2 with PUSH; SFHo without PUSH). We choose the $25 M_{\odot}$ progenitor as a representative model. The top panel of Figure 6 shows the temporal evolution of the electron neutrino, electron antineutrino, and the heavy-flavor neutrino luminosities. In all three cases we see an initial peak around 0.1 s postbounce followed by a plateau.

Up to about 0.4 s post bounce, the luminosities are qualitatively similar in all three cases. However, the case using the SFHo EOS has consistently higher luminosities in all three neutrino flavors when compared to the case using the DD2 EOS. Beyond 0.4 s , the luminosities are fundamentally different. In the exploding SFHo case the neutrino and antineutrino luminosities drop as the explosion sets in. In the DD2 case (which fails to explode) and the nonexploding SFHo case the neutrino and antineutrino luminosities remain relatively high due to the continued accretion onto the central object. The most important factor in driving the explosion in the SFHo case is the second bump in the neutrino and antineutrino luminosities around 0.25 s post bounce. This provides extra heating behind the shock and aids in achieving a successful explosion with the SFHo EOS. This second bump in the neutrino luminosity is an inherent property of the SFHo nuclear EOS and is not a relic of the PUSH method. When we use the SFHo EOS without PUSH, the model does not explode. In this case, the electron neutrino and antineutrino luminosities

Table 3
Explosion Properties of s16.0, u16.0 and z16.0 Models with Different EOS

| Model | EOS | $\xi_{2.0, \mathrm{~b}}$ | $\begin{gathered} E_{\text {expl }} \\ \text { (B) } \end{gathered}$ | $\begin{aligned} & M_{\mathrm{cut}} \\ & \left(M_{\odot}\right) \end{aligned}$ | Layer of $M_{\text {cut }}$ | $\begin{aligned} & \hline{ }^{56} \mathrm{Ni} \\ & \left(M_{\odot}\right) \end{aligned}$ | $\begin{aligned} & \hline \hline{ }^{57} \mathrm{Ni} \\ & \left(M_{\odot}\right) \end{aligned}$ | $\begin{aligned} & \hline \hline{ }^{58} \mathrm{Ni} \\ & \left(M_{\odot}\right) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| s16.0 | SFHo | 0.234048 | 1.3650 | 1.5244 | Si-O | $8.00 \times 10^{-2}$ | $3.13 \times 10^{-3}$ | $7.95 \times 10^{-3}$ |
|  | SFHx | 0.234293 | 1.2413 | 1.5300 | Si-O | $7.78 \times 10^{-2}$ | $3.10 \times 10^{-3}$ | $7.90 \times 10^{-3}$ |
|  | TM1 | 0.235293 | 1.4071 | 1.5293 | Si-O | $7.83 \times 10^{-2}$ | $2.96 \times 10^{-3}$ | $7.59 \times 10^{-3}$ |
|  | NL3 | 0.235675 | 1.4607 | 1.5263 | Si-O | $7.98 \times 10^{-2}$ | $2.99 \times 10^{-3}$ | $7.29 \times 10^{-3}$ |
|  | DD2 | 0.232932 | 1.2365 | 1.5372 | Si-O | $7.54 \times 10^{-2}$ | $2.96 \times 10^{-3}$ | $7.41 \times 10^{-3}$ |
|  | BHB $\lambda \phi$ | 0.232932 | 1.2362 | 1.5372 | Si-O | $7.55 \times 10^{-2}$ | $2.96 \times 10^{-3}$ | $7.41 \times 10^{-3}$ |
|  | LS220 | 0.240236 | 1.4177 | 1.5183 | Si-O | $7.87 \times 10^{-2}$ | $3.17 \times 10^{-3}$ | $8.80 \times 10^{-3}$ |
|  | Shen | 0.233976 | 1.5861 | 1.5142 | Si-O | $7.59 \times 10^{-2}$ | $2.80 \times 10^{-3}$ | $7.11 \times 10^{-3}$ |
| u16.0 | SFHo | 0.407177 | 1.8681 | 1.7433 | Si-O | $1.49 \times 10^{-1}$ | $2.66 \times 10^{-3}$ | $1.32 \times 10^{-3}$ |
|  | SFHx | 0.407626 | 1.7126 | 1.7525 | Si-O | $1.45 \times 10^{-1}$ | $2.64 \times 10^{-3}$ | $1.50 \times 10^{-3}$ |
|  | TM1 | 0.409084 | 1.8459 | 1.7560 | Si-O | $1.43 \times 10^{-1}$ | $2.21 \times 10^{-3}$ | $0.59 \times 10^{-3}$ |
|  | NL3 | 0.412725 | 1.8548 | 1.7559 | Si-O | $1.43 \times 10^{-1}$ | $2.07 \times 10^{-3}$ | $0.59 \times 10^{-3}$ |
|  | DD2 | 0.403058 | 1.6606 | 1.7689 | Si-O | $1.36 \times 10^{-1}$ | $2.38 \times 10^{-3}$ | $0.96 \times 10^{-3}$ |
|  | BHB $\lambda \phi$ | 0.403042 | 1.6575 | 1.7690 | Si-O | $1.36 \times 10^{-1}$ | $2.38 \times 10^{-3}$ | $1.00 \times 10^{-3}$ |
|  | LS220 | 0.415827 | 2.0133 | 1.7322 | Si-O | $1.53 \times 10^{-1}$ | $2.86 \times 10^{-3}$ | $4.36 \times 10^{-3}$ |
|  | Shen | 0.405708 | 1.9770 | 1.7388 | Si-O | $1.42 \times 10^{-3}$ | $2.01 \times 10^{-3}$ | $0.72 \times 10^{-3}$ |
| z16.0 | SFHo | 0.140235 | 0.9396 | 1.4917 | Si-O | $5.61 \times 10^{-2}$ | $0.79 \times 10^{-3}$ | $0.26 \times 10^{-3}$ |
|  | SFHx | 0.140364 | 0.8507 | 1.4959 | Si-O | $5.44 \times 10^{-2}$ | $0.81 \times 10^{-3}$ | $0.49 \times 10^{-3}$ |
|  | TM1 | 0.140896 | 1.0493 | 1.4884 | Si-O | $5.71 \times 10^{-2}$ | $0.75 \times 10^{-3}$ | $0.23 \times 10^{-3}$ |
|  | NL3 | 0.141000 | 1.0973 | 1.4859 | Si-O | $5.78 \times 10^{-2}$ | $0.72 \times 10^{-3}$ | $0.33 \times 10^{-3}$ |
|  | DD2 | 0.139895 | 0.9201 | 1.4949 | Si-O | $5.41 \times 10^{-2}$ | $0.76 \times 10^{-3}$ | $0.26 \times 10^{-3}$ |
|  | BHB $\lambda \phi$ | 0.139895 | 0.9011 | 1.4961 | Si-O | $5.41 \times 10^{-2}$ | $0.76 \times 10^{-3}$ | $0.25 \times 10^{-3}$ |
|  | LS220 | 0.138217 | 0.9372 | 1.4871 | Si-O | $5.73 \times 10^{-2}$ | $0.91 \times 10^{-3}$ | $0.41 \times 10^{-3}$ |
|  | Shen | 0.140313 | 1.1802 | 1.4784 | Si-O | $5.57 \times 10^{-2}$ | $0.68 \times 10^{-3}$ | $0.54 \times 10^{-3}$ |

(gray lines) follow the same behavior up to $\sim 0.4 \mathrm{~s}$ post bounce including the second bump. After $\sim 0.4 \mathrm{~s}$, the electron neutrino and antineutrino luminosities remain high, following the nonexploding case using the DD2 EOS (as is expected from continued accretion in nonexploding models).

In addition, up to $\sim 0.4 \mathrm{~s}$ post bounce the mean energies of all three neutrino flavors is a few MeV higher for the SFHo EOS when compared to the case using the DD2 EOS (as shown in the bottom panel of Figure 6). The higher neutrino energies and luminosities results in slightly earlier explosions. This is accompanied by faster shock evolution and faster PNS contraction for SFHo as compared to DD2.

## 5. Nucleosynthesis Yields

Our setup has several important features for the nucleosynthesis predictions, in particular for the innermost layers of the ejecta. In these layers, iron-group elements are synthesized through explosive burning (complete and incomplete silicon burning) and some isotopes beyond iron can be formed via a $\nu$ p-process (Fröhlich et al. 2006a). In the PUSH setup, the mass cut and the explosion energy evolve simultaneously and are not independent of each other. Moreover, the neutrino-matter interactions are treated self-consistently, thereby setting the electron fraction $Y_{e}$ (especially of the innermost ejecta) consistent with the evolution of the explosion and the neutrino emission from the PNS. In our models, the $Y_{e}$ of the very innermost ejected tracer is very low, sometimes allowing for the production of elements up to mass number $A \sim 130$. However, the mass resolution in our models is quite coarse for the neutrino-driven wind, and hence we do not further investigate this in the present work.

For different EOS we expect to see changes in the abundances of elements synthesized in the innermost ejecta,
i.e., of iron-group and trans-iron-group elements. While the peak temperatures and densities (setting the conditions under which freeze-out happens) are mostly set by the explosion strength, the nuclear EOS determines the PNS evolution and with it the properties of the neutrino and antineutrino fluxes (which are setting the electron fraction, $Y_{e}$ ).

In this section we present and discuss the nucleosynthesis yields of all exploding models, which we identify by the progenitor model and the nuclear EOS used in the explosion simulation. The setup for the nucleosynthesis is identical in all cases. We do not include those models which failed to explode as they are expected to have very little ejecta (Lovegrove \& Woosley 2013; Lovegrove et al. 2017). We identify trends among the models using the SFHo EOS (Section 5.1) and discuss in more details the simulations of three representative progenitors (s16.0, u16.0, and z16.0) using all eight nuclear EOS of this work (Section 5.2).

### 5.1. General Trends for Models using the SFHo EOS

In Figure 7 we present the elemental yields of four irongroup elements-manganese, iron, cobalt, and nickel-as a function of the explosion energy for simulations with the SFHo EOS (solid points). In addition, the corresponding results for simulations with the DD2 EOS (taken from Paper III and Paper IV) are included as transparent points. The color of each point corresponds to the mean $Y_{e}$ of the region where most of the element is made. First, we focus on how the nuclear EOS affects the yields and the general trends with explosion energy.

Production of elemental manganese is highly $Y_{e}$ dependent. Models with a $Y_{e}$ close to 0.5 have low Mn yields, and vice versa (see also Paper III). Most of the s-series progenitors have a relatively high $Y_{e}$ in the relevant layers, and therefore low manganese yields. This is also the case for the u -series and


Figure 5. Explosion energy (top) and remnant mass (bottom) for a $16 M_{\odot}$ model at three different metallicities (s16.0 in blue, u16.0 in yellow, and z16.0 in red).
z -series progenitors. The w -series is different from the s -, u and z -series. The network used during the the hydrostatic evolution is much larger for the w-series, which results in the realization of a large range of $Y_{e}$ values in the relevant layers of the precollapse star and therefore intermediate Mn yields.
The only stable isotope of $\mathrm{Mn}\left({ }^{55} \mathrm{Mn}\right)$ is produced as ${ }^{55} \mathrm{Co}$ in proton-rich layers ( $Y_{e}>0.5$ ) and incomplete Si-burning zones. The amount of proton-rich ejecta is the same for SFHo models and DD2 models $\left(\sim 0.007 M_{\odot}\right.$, or about $10 \%$ of the ejecta where iron-group elements are made). Hence, we expect little difference between the Mn yields from SFHo models and from DD2 models. We find about 5\% difference in Mn yields between SFHo and DD2 for a given progenitor model. All uand z -models, as well as almost all w-models, have higher Mn yields with SFHo than their DD2 counterparts. Generally, the s-models have lower Mn yields with SFHo than with DD2, which has higher $Y_{e}$ values in the relevant layers.

Next, we discuss elemental iron, which has a strong correlation with the explosion energy (higher explosion energy means higher Fe yields; the exceptions to this, s25.0, s25.2, and s39.0, are discussed in Section 4.2 and also the "almost failing models"; see Paper IV). The main contribution to elemental iron comes from ${ }^{56} \mathrm{Fe}$, which is made as ${ }^{56} \mathrm{Ni}$ primarily in Si burning zones. Hence, we expect only small differences in the Fe yields between the SFHo and DD2 models, primarily due to the differences in the explosion energies. We find about half the models have differences in the Fe yields of less than $5 \%$; the other half of the models has differences of less than $12 \%$. Only a small number of models (s11.0, s11.2, s11.6, s11.8, s19.6, s20.2, and u17.0) have lower explosion energies with SFHo


Figure 6. Temporal evolution of the neutrino luminosities (top) and mean energies (bottom) for s25.0 with two different nuclear EOS: SFHo (red) and DD2 (blue). For comparison, the gray lines represent the model using the SFHo EOS without PUSH.
compared to DD2. These models accordingly have lower Fe yields than their DD2 counterparts.

The behavior of elemental cobalt is a combination of what we have seen for Mn and for Fe . The Co yields show a correlation with explosion energy as well as a $Y_{e}$ dependence. Overall, a higher explosion energy means a higher Co yield. In addition, for a fixed explosion energy, a higher $Y_{e}$ implies a higher Co yield. The w-series has intermediate $Y_{e}$ values, but the lowest Co yields. The lowest $Y_{e}$ values (found mostly in s-series models) also have low Co yields. The models of all series with the highest $Y_{e}$ values in the relevant zones have the highest Co yields, across all explosion energies. Additionally, as for Mn and Fe , SFHo models have up to $15 \%$ higher Co yields than DD2 models.

Finally, elemental nickel also has strong correlation with explosion energy and has significant $Y_{e}$ dependence. The Ni yields have two distinct branches, one with low $Y_{e}$ and high Ni yields, and the other with high $Y_{e}$ and lower Ni yields. The uand z-series mostly populate the latter branch (high $Y_{e}$, low Ni yields). The w-series has intermediate $Y_{e}$ values and corresponding intermediate Ni yields. The highest Ni yields are in models of the s-series with the lowest $Y_{e}$ in the relevant layers. The two notable exceptions to this trend are the two models at the lowest explosion energies with $\sim 5 \times 10^{-3} M_{\odot}$ of Ni. These are, once again, the models with EOS-dependent outcomes. The $Y_{e}$ dependence of the elemental Ni yields originate from the contributions of nonsymmetric Ni isotopes, i.e., from ${ }^{58} \mathrm{Ni}$ and ${ }^{60} \mathrm{Ni}$. ${ }^{58} \mathrm{Ni}$ is formed in Si-burning zones as itself while ${ }^{60} \mathrm{Ni}$ is produced as ${ }^{60} \mathrm{Cu}$ and ${ }^{60} \mathrm{Zn}$ in the complete Si-burning zone.


Figure 7. From top to bottom: elemental yields of $\mathrm{Mn}, \mathrm{Fe}, \mathrm{Co}$, and Ni after the explosion as a function of the compactness for the s-series (circles), w-series (stars), u-series (triangles), and z -series (squares). The colored symbols are for simulations with the SFHo EOS, where the color represents the $Y_{e}$, and the transparent symbols are simulations with the DD2 EOS (taken from Paper III and Paper IV).

In general, the SFHo models make up to $20 \%$ more Ni than the corresponding DD2 models.
Next, we discuss the yields of the four isotopes ${ }^{56} \mathrm{Ni},{ }^{57} \mathrm{Ni}$, ${ }^{58} \mathrm{Ni}$, and ${ }^{44} \mathrm{Ti}$ (see Figure 8) for which we have observational constraints from SN 1987A and a few other supernovae. ${ }^{56} \mathrm{Ni}$ is produced from Si burning in the inner layers of a collapsing


Figure 8. Same as Figure 7, but for isotopic yields of ${ }^{56} \mathrm{Ni},{ }^{57} \mathrm{Ni},{ }^{58} \mathrm{Ni}$, and ${ }^{44} \mathrm{Ti}$ (from top to bottom).
star. The temperature and density conditions in these layers are very similar for SFHo and DD2 EOS. Therefore, the ${ }^{56} \mathrm{Ni}$ yields are also similar for both EOS, with the SFHo models generally having $\sim 20 \%$ higher yields than the DD2 models (due to the higher explosion energies). The small number of models which have a lower explosion energy with SFHo compared to with DD2 also have lower ${ }^{56} \mathrm{Ni}$ yields compared to their DD2 counterpart. There is one extreme exception (w22.0), which has a higher explosion energy with SFHo but a much lower ${ }^{56} \mathrm{Ni}$ yield compared to DD2.

Generally, the correlation of ${ }^{56} \mathrm{Ni}$ yields and explosion energy are quite strong and independent of the progenitor metallicity. The points in the top left (high ${ }^{56} \mathrm{Ni}$ and low explosion energy) are the models with EOS-dependent outcomes (see Section 4.2 and the "almost failing models" in Paper IV).

The ${ }^{57} \mathrm{Ni}$ yields strongly depend on the $Y_{e}$ of the model. Models with high $Y_{e}$ make less ${ }^{57} \mathrm{Ni}$ and vice versa. The s-series progenitors group into two distinct $Y_{e}$ branches. Most of the s-series models and the u- and z-series models have high $Y_{e}$ and therefore lower ${ }^{57} \mathrm{Ni}$ yields. Some of the s-series models have low $Y_{e}$ and hence comparatively higher ${ }^{57} \mathrm{Ni}$ yields. Lastly, the w-series models have intermediate $Y_{e}$ values (see above) and produce intermediate amounts of ${ }^{57} \mathrm{Ni}$. The SFHo yields are generally up to $\sim 20 \%$ higher compared to their DD2 counterpart (similar to ${ }^{56} \mathrm{Ni}$ ). The exceptions to this are the w22.0 model (which makes twice as much ${ }^{57} \mathrm{Ni}$ as its DD2 counterpart) and a handful of models with very low explosion energy.

Similar to ${ }^{57} \mathrm{Ni}$, the ${ }^{58} \mathrm{Ni}$ yields also have a strong $Y_{e}$ dependence. For the bulk of our models the ${ }^{58} \mathrm{Ni}$ production occurs at $Y_{e}$ values of around 0.498 . For only five models (s16.8, s25.2, s27.2, and s27.8) the dominant production site of ${ }^{58} \mathrm{Ni}$ is in a proton-rich environment. Without those five models, we see a similar behavior as for ${ }^{57} \mathrm{Ni}$, where higher $Y_{e}$ values result in lower ${ }^{58} \mathrm{Ni}$ yields. Again, the w-series has intermediate $Y_{e}$ values and hence intermediate ${ }^{58} \mathrm{Ni}$ yields. The $\mathrm{u}-, \mathrm{z}-$, and some s-series models have high $Y_{e}$ values and hence low ${ }^{58} \mathrm{Ni}$ yields. The SFHo models have up to $50 \%$ higher ${ }^{58} \mathrm{Ni}$ yields than the DD2 models.
Lastly, we discuss ${ }^{44} \mathrm{Ti}$, for which the yields are somewhat correlated with the explosion energy. Here, the comparison between SFHo and DD2 models is more interesting than for the Ni isotopes. For SFHo models where the explosion energy is less than $10 \%$ larger than in the DD2 case, about half the SFHo models have lower ${ }^{44} \mathrm{Ti}$ yields and the other half have higher ${ }^{44} \mathrm{Ti}$ yields than in the DD2 case. For SFHo models where the explosion energy is more than $10 \%$ higher than for the corresponding DD2 model, the ${ }^{44} \mathrm{Ti}$ yields are up to $10 \%$ higher than for DD 2 .

### 5.2. Nucleosynthesis Results from All Eight Nuclear EOS

In this section, we expand our discussion to include all eight nuclear EOS models considered in this work. We will use three models (s16.0, u16.0, and z16.0-with one ZAMS mass at each metallicity) for this.
We start by continuing the discussion of the isotopic yields of ${ }^{56} \mathrm{Ni},{ }^{57} \mathrm{Ni},{ }^{58} \mathrm{Ni}$, and ${ }^{44} \mathrm{Ti}$. In Figure 9 we plot the postexplosion mass fraction of ${ }^{56} \mathrm{Ni},{ }^{57} \mathrm{Ni},{ }^{58} \mathrm{Ni}$, and ${ }^{44} \mathrm{Ti}$ (together with ${ }^{16} \mathrm{O}$ and ${ }^{28} \mathrm{Si}$ for reference) as a function of the mass coordinate outside of the mass cut. The shaded background in each plot marks the combined width of the ${ }^{56} \mathrm{Ni},{ }^{16} \mathrm{O}$, and ${ }^{28} \mathrm{Si}$ layers for all EOS models. The overlap between the different layers indicates the maximum and minimum width among all eight cases.

Overall, the ${ }^{56} \mathrm{Ni}$ layer follows a quite similar behavior for all EOS models on a progenitor-by-progenitor basis. Among the three progenitors, the low-metallicity u16.0 model has the broadest ${ }^{56} \mathrm{Ni}$ layer and also the largest difference in the location of the transition to the ${ }^{28} \mathrm{Si}$ layer between different EOS models ( $0.178-0.204 M_{\odot}$ ). The same trend is also present in the transition between the ${ }^{28} \mathrm{Si}$ and ${ }^{16} \mathrm{O}$ layer. The solar


Figure 9. Postexplosion composition profile as a function of the mass coordinate outside the mass cut for the $16 M_{\odot}$ progenitor from the s-series (top), the u -series (middle), and the z -series (bottom). The background shading denotes the ${ }^{56} \mathrm{Ni},{ }^{28} \mathrm{Si}$, and ${ }^{16} \mathrm{O}$ layers. The overlap in shading indicates the differences due to different EOS models used.
metallicity model s16.0 has a thinner ${ }^{56} \mathrm{Ni}$ layer, with the Ni layer extending to $\sim 0.125-0.127 M_{\odot}$ (the exceptions are DD2 and $\operatorname{BHB} \lambda \phi$ at $0.119-0.120 M_{\odot}$ ). The zero-metallicity model z16.0 has the thinnest ${ }^{56} \mathrm{Ni}$ layer of the three progenitors discussed here. The different EOS models fall into two groups with respect to the transition from ${ }^{56} \mathrm{Ni}$ to ${ }^{28} \mathrm{Si}$. For most EOS
models, this transition occurs $0.08-0.082 M_{\odot}$ outside of the mass cut; only for TM1, NL3, and the Shen EOS does it occur at a slightly larger mass coordinate $\left(0.085-0.087 M_{\odot}\right.$ outside of the mass cut).
${ }^{44} \mathrm{Ti}$ is coproduced with ${ }^{56} \mathrm{Ni}$, but at about three orders of magnitude lower levels. As for ${ }^{56} \mathrm{Ni}$, the ${ }^{44} \mathrm{Ti}$ mass fraction is similar between different EOS models. The effect of using different EOS models is most visible at the edges of the ${ }^{44}$ Ti-rich zone. For the s16.0 models, these differences are small. They are largest for u16.0, where for SFHo and LS220 the (relatively) ${ }^{44}$ Ti-rich region extends furthest toward the ${ }^{28} \mathrm{Si}$ layer.
${ }^{57} \mathrm{Ni}$ (and ${ }^{58} \mathrm{Ni}$ ) are coproduced with ${ }^{56} \mathrm{Ni}$. The peak mass fractions are very similar among different EOS models within the same progenitor. However, at the inner edge of the ${ }^{57} \mathrm{Ni}$-rich zones, we see variations (up to a factor of 2) between different EOS models. This is due to EOS-induced differences in the local electron fraction in these innermost ejecta layers. The ${ }^{58} \mathrm{Ni}$ mass fractions show the same behavior, but even ${ }_{57}$ more pronounced than for ${ }^{57} \mathrm{Ni}$ (up to a factor of 10). For both ${ }^{57} \mathrm{Ni}$ and ${ }^{58} \mathrm{Ni}$, the mass fractions at the inner edge are enhanced as compared to the main value throughout the ${ }^{57,58} \mathrm{Ni}$-rich zones. Whether ${ }^{57} \mathrm{Ni}$ or ${ }^{58} \mathrm{Ni}$ are produced at higher levels also depends on the local electron fraction. In the case of s16.0 and z16.0, these layers have a slightly lower $Y_{e}(0.4978-0.4980)$ than the corresponding layer in u16.0 (which have a $Y_{e^{\circ}}$ of $0.4984-0.4988$ ). Hence, the more neutron-rich isotope ${ }^{58} \mathrm{Ni}$ dominates over ${ }^{57} \mathrm{Ni}$ in s16.0 and z16.0.

For a given progenitor, the conditions in the explosive Siburning layers are very similar between simulations with different EOS models. Hence, any difference in the abundances synthesized in those layers is due to differences in the local $Y_{e}$ value. In Figure 10, we plot the $Y_{e}$ for the different EOS models as a function of the mass coordinate outside the mass cut. We omit our innermost ejected tracer, which represents the neutrino-driven wind. Our mass resolution of $10^{-3} M_{\odot}$ is not sufficiently fine to resolve the wind properly.

For all three progenitors shown, the innermost $\sim 0.01 M_{\odot}$ of the ejecta are neutron-rich $\left(Y_{e} \simeq 0.43-0.44\right)$. The variations among six of the EOS models (SFHo, SFHx, TM1, NL3, DD2, and $\operatorname{BHB} \lambda \phi$ ) are smaller than the difference between this group and the two reference EOS models (LS220 and Shen). In particular, the Shen EOS is quite different and in one case does not reach $Y_{e}$ values below 0.46 . These layers of relatively low $Y_{e}$ are where mostly the isotopes with mass numbers $A \gtrsim 130$ are synthesized (see insert in top panel of Figure 10 for the abundances from a representative tracer at $Y_{e}=0.434$ ). This can also be seen in the final overall abundances of u16.0 (see Figure 11), where the calculations with the Shen EOS have a distinct lack of material with $A \gtrsim 130$ in the final abundances.

Outside of the innermost neutron-rich layers there is a region of proton-rich ejecta, seen as peak in the $Y_{e}$ evolution. This occurs for every EOS and every progenitor model in our study. The peak $Y_{e}$ value that is reached and the amount of proton-rich material is slightly different for different EOS models. However, overall, these proton-rich layers undergo alpha-rich and proton-rich freeze-out. The differences in final mass fractions are about $3 \%-8 \%$ (see bottom inserts of Figure 11, which show the difference between the highest and lowest mass fraction for a given mass number $A$ normalized to the average mass fraction at this $A$ ).


Figure 10. Postexplosion $Y_{e}$ evolution for the $16 M_{\odot}$ progenitor of the s- (top), u - (middle) and z -series (bottom) as a function of the mass coordinate outside of the mass cut. The insert shows the final mass fractions from two representative tracers, one at $Y_{e}=0.434$ and one at $Y_{e}=0.527$.

## 6. Comparison with Observations

In this section, we compare the results of our simulations to observations of local supernovae (Section 6.1) and of metalpoor stars (Section 6.2). Observations of CCSNe provide us with important information about the explosion energy and the amount of ${ }^{56} \mathrm{Ni}$ produced. Metal-poor stars carry in their atmospheres the signature of one or a few previously exploded CCSNe.

### 6.1. Local Supernovae

Here, we compare the results of our simulations to the observations of supernovae in the local universe ( $z<0.01$ ). The observational data are the same as in Paper IV (see Table 4


Figure 11. Final yields after decay for the $16 M_{\odot}$ progenitor of the s- (top), u(middle), and $z$-series (bottom) as a function of the mass number with eight different EOS models. The bottom insert shows $\Delta=\left|X_{\max }-X_{\min }\right| / X_{\text {avg }}$, the difference between the highest and the lowest abundance for each mass number normalized by the average over all eight cases.
in Paper II and Müller et al. 2017 for the original references). The left panel of Figure 12 shows the $1 \sigma, 2 \sigma$, and $3 \sigma$ confidence intervals of the kernel density estimate (KDE) for the ${ }^{56} \mathrm{Ni}$ yields and explosion energy both weighted with the initial mass function (IMF) for simulations using the SFHo EOS (blue, this work) and for simulations using the DD2 EOS (red, Paper II and Paper IV). The confidence intervals are computed for the combined results from all four progenitor series (solar, low, and zero metallicity). In the right panel, we show-for the SFHo EOS only-the impact of excluding lowand zero-metallicity models ( $u$ - and z-series) from the KDE (green) compared to including all metallicities in the KDE
(red). Note that the red contour lines are the same in both panels.

The KDE for the combined ${ }^{56} \mathrm{Ni}$ yields and explosion energies (left panel) is centered around $m\left({ }^{56} \mathrm{Ni}\right)=0.06$ and $E_{\text {expl }}=1.13 \mathrm{~B}$. Almost all of the observational data overlap with the $3 \sigma$ confidence interval for our simulation results. There are a few outliers with very low and very high ${ }^{56} \mathrm{Ni}$ masses, originating from low-mass ( $<10 M_{\odot}$ ) and very-highmass progenitors ( $>40 M_{\odot}$ ), which we do not include in our study.
The KDE confidence levels for the combined ${ }^{56} \mathrm{Ni}$ masses and explosion energies are very similar between the SFHo and the DD2 case. At the $3 \sigma$ confidence level the slightly higher explosion energies obtained with SFHo (together with the corresponding slightly lower explosion energies for DD2) become visible in the contour line.

As mentioned earlier in this section, the observations are of SNe in the local universe (redshift $z<0.01$ ). Hence, in the right panel, we compare the KDE for solar metallicity models only to the observations. In this case, the KDE is centered around $0.07 M_{\odot}$ and 1.3 B , which is a shift toward higher ${ }^{56} \mathrm{Ni}$ mass and higher explosion energy. This is because the low- and zerometallicity models ( $u$ - and $z$-series) explode with lower explosion energy and make slightly smaller amounts of ${ }^{56} \mathrm{Ni}$. The shift in the distribution is in the direction of where the observational data are more concentrated.

Overall, we can conclude that the results from our method are consistent with constraints from observations for both the SFHo and the DD2 EOS. Unfortunately, the differences between the two EOS models is too small in this analysis to identify which one is the more-favored EOS.

### 6.2. Metal-poor Stars

The atmospheres of low-mass, long-lived, metal-poor stars can provide us with information about the nucleosynthesis processes in CCSNe, originating from short-lived massive stars. These CCSNe would have deposited their yields in the gas from which these low-mass, metal-poor stars were formed. Here, we compare the yields predicted from our simulations with the observationally derived abundances in a well-observed metal-poor star. We focus on the Fe-group elements, which are formed in primary explosive nucleosynthesis processes in the explosion.

We compare the predicted iron-group elements from our simulations with the observed abundances of the metal-poor star HD 84937 in Figure 13. The triangles are the abundances derived from neutral and singly ionized transitions, taken from Sneden et al. (2016). Each colored square in the figure corresponds to one exploding model (using the SFHo EOS). Note that our results are not IMF weighted to illustrate the range of yields for each element (and hence how sensitive the results are to different conditions found in different models).

Overall, our data agree with observations. We find that scandium and zinc are synthesized at levels comparable to the observed values. Both of these elements are difficult to produce in sufficient amounts in nucleosynthesis calculations that neglect the neutrino interactions and employ a canonical explosion energy of 1 B , like the traditional piston and thermal bomb setup. In case of hypernovae, the enhanced explosion energies lead to overproduction of Sc and Zn even without the inclusion of neutrino interactions (Nomoto et al. 2006). Fröhlich et al. (2006b) used a careful treatment of neutrino


Figure 12. Left panel: kernel density estimates (KDE) of the explosion energy distribution and of the $\mathrm{Ni}^{56}$ mass distribution, both weighted with the initial mass function, for SFHo (red) and DD2 (blue) for all models combined. The contour lines represent $1 \sigma, 2 \sigma$, and $3 \sigma$ confidence levels. The observed SNe are shown with gray crosses. Right panel: same, but comparing the KDE for all SFHo models (red, same as on the left) to the KDE for only solar metallicity SFHo models (green).
interactions which led to an enhanced production of Sc and Zn at canonical explosion energies of 1 B . Our models presented here coproduce Zn with Fe and we find a smaller spread of [ $\mathrm{Zn} / \mathrm{Fe}]$ for low-metallicity and zero-metallicity progenitors as compared to solar-metallicity progenitors. We also find that only the w-series (solar metallicity) progenitors consistently produce Mn , in agreement with observations. From the other progenitors series, only a handful of s- (solar metallicity) and z-models (zero metallicity) produce similarly high levels of Mn . Most of the s- and z-models and all u-models (low metallicity) strongly underproduce Mn compared to observations. This is due to the size of the network used during stellar evolution, which sets the range of possible $Y_{e}$ values. In the case of a small network (s-, u-, and z-series) the $Y_{e}$ cannot take intermediate values required for high Mn production. Since the production of Mn is quite sensitive to the local $Y_{e}$ value, the local $Y_{e}$ leaves an imprint on the resulting $[\mathrm{Mn} / \mathrm{Fe}]$ ratio. Titanium is typically systematically underproduced in spherically symmetric nucleosynthesis models (see also Paper I for a detailed discussion of the uncertainties in the Ti yields).

## 7. Remnant Properties

The mass distribution of the compact remnants formed in our simulations of core collapse are yet another result-in addition to the explosion energies, ejecta mass, and elemental yieldsthat can be compared with observations. We use the procedure described in Paper II and Paper IV to calculate the remnant mass distribution. We obtain the baryonic mass of the newly formed hot NS by following the evolution of the PNS. We then use the nuclear EOS to calculate the gravitational mass of the corresponding cold NS. Finally, we compute the birth mass distribution of the compact remnants by weighting the simulated remnant mass with the Salpeter IMF for massive stars (Salpeter 1955).
First, we discuss the distribution of NSs. Figure 14 shows the IMF-weighted KDE of the mass distribution for cold NSs for all four progenitor series. For each series we have considered preexplosion masses between $11-40 M_{\odot}$. The predicted NS masses lie in the range of $1.2-1.8 M_{\odot}$.


Figure 13. Abundances of Fe-group elements for all the SFHo exploding models of the s- (blue), w- (green), u- (yellow), and z-series (red). The triangles are observationally derived abundances for the metal-poor star HD 84937.

For the low- and zero-metallicity series, most of the high ZAMS mass models do not explode and hence are not available to form higher-mass NSs. For all the four series the distributions show a single peak. For the s-series, the small bump around $1.75 M_{\odot}$ for SFHo comes from the mixed models discussed in Section 4.2. For the u-series, most of the exploding models form lower-mass NSs except for a few high-compactness models which have a lower explosion energy and make more massive NSs (u20.0, u24.0, and u30.0). These models contribute to the plateau around $1.75 M_{\odot}$. For the z-series, the slight change in shape around $1.55 M_{\odot}$ also comes from exploding models (z17.0 and z18.0) with very high compactness (see Figure 1 in Paper IV), which therefore make more massive NSs.
Comparing the results obtained with the SFHo EOS (this work) to those obtained with the DD2 EOS (Paper II and Paper IV), we find that the distribution is shifted to the left, i.e., the NSs resulting from the SFHo EOS are less massive than those from the DD2 EOS. This is consistent with the slightly


Figure 14. Gravitational birth mass kernel density estimates for cold neutron stars for the s-series, w-series, u-series, and z-series (from top to bottom). Simulations using the SFHo EOS are shown in red. Simulations using the DD2 EOS are shown in blue (data from Paper II and IV).
higher explosion energies and earlier explosions found with SFHo as compared to DD2.

Our study is based on single, nonrotating stars. As such, the results do not include the possible effects that are present in binary-star systems, like accretion or mass loss. Difficulty may
arise when we compare the theoretically predicted NS masses with the observed NS masses as the measurements of NS masses are from binary systems. However, Raithel et al. (2018) argue that we can still make such a comparison as the singlestar model can be considered as a representative of some close binary scenarios due to the uncertain nature of mass loss. Most available NS mass measurements are between 1.1-2.0 $M_{\odot}$ (Özel \& Freire 2016), which is similar to what we obtain from our simulations.
Next, we turn to the simulations that did not explode successfully and instead formed a BH. In our simulation framework, this includes models which run longer than the time when PUSH is active without exploding as well as models which exhibit a very rapid increase in the central density above nuclear saturation density, which we interpret as formation of a BH. Note that the Agile-IDSA code cannot follow the formation of the BH due to the metric used. Figure 15 shows the predicted birth mass distribution for all four progenitor series. The stellar mass at the time of collapse is determined by the star's mass-loss history. This in turn influences the mass of the BH formed as a result of a failed explosion. Other processes, like the loss of the PNS binding energy in a weak shock (Lovegrove \& Woosley 2013) or the stripping of the envelope by a binary companion before collapse, may alter the mass ultimately collapsing to a BH . We study the impact of these effects on the BH mass distribution by considering three different cases covering a range of outcomes. Our most massive estimate for the BH mass is based on a scenario where the entire stellar mass at the time of core collapse ends up in the BH . Our lightest BH mass estimate is for the case where the star is stripped of its outer layers and only the CO core collapses to a BH. In our third (intermediate) case, we follow Kochanek (2014) and assume that He-core mass sets the mass of the BH.
Generally, the low- and zero-metallicity models make more massive BHs than their solar-metallicity counterparts. This is a result of the low-metallicity progenitors experiencing less mass loss compared to the solar-metallicity ones and therefore have retained more mass at the time of collapse. In the BH distribution for the u - and z-series we see two clusters of BH masses separated by a gap. This is a reflection of the "island of nonexplodability" near $25 M_{\odot}$ (at 21-24 $M_{\odot}$ for u-series and 23-27 $M_{\odot}$ for z-series) found in our work and also in the literature (Ertl et al. 2016; Sukhbold et al. 2016; Müller et al. 2016). This gap is not visible in the BH distributions for the solar-metallicity series. The s-series has a larger number of models, whereas the w-series forms fewer BHs than the low/ zero metallicity series. Interestingly, the w-series has monotonically increasing CO-core masses with increasing ZAMS mass, whereas the s-series has a more complex trend of COcore mass as a function of the ZAMS mass (see Figures 3 and 4 in Paper II). We find that the BH mass distributions from the SFHo EOS are very similar to those obtained with the DD2 EOS. Hence, the maximum BH mass is the also the same in both cases.

A sample table of the remnant masses (NSs and BHs) from our simulations is given in Table 4 of the Appendix. The full table is available as machine-readable data.

## 8. Summary

In this paper we simulate the collapse and explosion of nonrotating massive stars at three different metallicities. We




Figure 15. Birth mass distributions of black holes (BHs) for the s-series, w -series, u -series, and z -series (from top to bottom). The different shaded bars indicate three different cases of possible BH mass distributions depending on how much of the initial stellar mass ultimately contributes to the final BH mass.
compute the resulting remnants (NSs or BHs ) and the detailed nucleosynthesis yields in a postprocessing approach. We perform two suites of simulations for this: one, a complete suite for all progenitors at all metallicities using the SFHo nuclear EOS; and the other, a suite of four progenitors ( $16 M_{\odot}$ at three metallicities and $25 M_{\odot}$ at solar metallicity) using eight different EOS: SFHo, SFHx, TM1, NL3, DD2, BHB $\lambda \phi$, LS220, and Shen.

For the first set of simulations (SFHo EOS), we find that the explosion energies are generally higher with the SFHo EOS when compared to the DD2 EOS. This is due to the higher neutrino and antineutrino luminosities for SFHo. Higher explosion energies come hand-in-hand with earlier explosions and less massive remnants. Overall, the outcome of core collapse is similar between the SFHo and DD2 EOS; however, we find that three models (s25.0, s25.2, and s39.0) with very high compactness explode with the SFHo EOS but not with the DD2 EOS. For our second set of simulations, we find that (for the three progenitors studied) the explosion energy varies by $15 \%-18 \%$ across the different EOS, but the impact on the PNS mass is minimal (about $1 \%$ ).
For the nucleosynthesis yields, we find the elements such as Fe and Ni are correlated with the explosion energy. For example, we find higher yields with the SFHo EOS, which has higher explosion energies than with DD2; however, the difference is small. Other elements, such as Mn , depend strongly on the local electron fraction; and yet, other elements (e.g., Co) are affected both by the explosion energy and the electron fraction.
For the SFHo EOS and the symmetric isotopes ${ }^{56} \mathrm{Ni}$ and ${ }^{44} \mathrm{Ti}$, we confirm the strong correlation of the final yields with the explosion energy found in our previous work and in other works. Interestingly, we find lower ${ }^{44} \mathrm{Ti}$ yields for some SFHo models despite their higher explosion energies. The nonsymmetric, neutron-rich isotopes ( ${ }^{57} \mathrm{Ni}$ and ${ }^{58} \mathrm{Ni}$ ), on the other hand, are strongly $Y_{e}$ dependent. A higher $Y_{e}$ results in overall less ${ }^{57} \mathrm{Ni}$ and ${ }^{58} \mathrm{Ni}$.
In the comparison of all the isotopic yields, we find only small differences for ${ }^{56} \mathrm{Ni}$ and ${ }^{44} \mathrm{Ti}$ across the eight EOS used. However, for ${ }^{57} \mathrm{Ni}$ and ${ }^{58} \mathrm{Ni}$ we find large differences that originate from the different $Y_{e}$ profiles for each EOS. Both the exact local value of $Y_{e}$ as well as the amount of material at that $Y_{e}$ value affect the final yields of these isotopes. All our models have some amount of neutron-rich material $\left(Y_{e} \sim 0.43\right)$ in the innermost ejecta. In these layers, isotopes up to mass number 130 are produced through a weak r-process. Our models also have proton-rich ejecta (also in the innermost ejecta, adjacent to the neutron-rich ejecta in mass coordinate). The peak $Y_{e}$ values can be as high as 0.52 . In these layers, we find the products of proton-rich and alpha-rich freeze-out.

We also compare our explosion results with observed supernovae. We find that our models are (within the $3 \sigma$ level) in agreement with the combined explosion energies and ${ }^{56} \mathrm{Ni}$ observations of local CCSNe. While we find a difference between simulations using the SFHo EOS and simulations using the DD2 EOS, they are too small to rule out one of these EOS. When comparing our predicted iron-group yields with the observationally derived abundances in a metal-poor star, we also find a general agreement, except for Mn and for Ti. This is no surprise, as Ti is traditionally underproduced in spherically symmetric simulations.

Finally, we compute the IMF-weighted distributions of NS masses and BH masses, which can be compared to the observed distributions of NSs and BHs. For the SFHo EOS, we find lower NS masses than with the DD2 EOS, which slightly shifts the NS distribution to lower masses. For the BH distribution, we find the same results as in our previous work using the DD2 EOS. The three models, which explode with SFHo and fail to explode with DD2, do not have a significant impact on the distributions.

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Software: Agile (Liebendörfer et al. 2001), CFNET (Fröhlich et al. 2006b), Matplotlib (Hunter 2007).

## Appendix <br> Machine-readable Data Table: Remnant Masses

A sample of the remnant masses from our simulations is given in Table 4.

Table 4
Remnant Masses (NSs and BHs) for Simulations with the SFHo EOS and for Simulations with the DD2 EOS

| Model | $m_{\text {ZAMS }}$ <br> $\left(M_{\odot}\right)$ | EOS <br> $\left(M_{\odot}\right)$ | $m_{\mathrm{NS}}$ | $m_{\mathrm{BH}}^{\text {CO-core }}$ <br> $\left(\boldsymbol{M}_{\odot}\right)$ | $m_{\mathrm{BH}}^{\text {He-core }}$ <br> $\left(\boldsymbol{M}_{\odot}\right)$ | $m_{\mathrm{BH}}^{\text {colapse }}$ <br> $\left(\boldsymbol{M}_{\odot}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| s10.8 | 10.8 | SFHo | 1.49 | $\ldots$ | $\ldots$ | $\ldots$ |
| s11.0 | 11.0 | SFHo | 1.41 | $\ldots$ | $\ldots$ | $\ldots$ |
| s40.0 | 40.0 | SFHo | 1.81 | $\ldots$ | $\ldots$ | $\ldots$ |
| u11.0 | 11.0 | SFHo | 1.49 | $\ldots$ | $\ldots$ | $\ldots$ |
| u40.0 | 40.0 | SFHo | $\ldots$ | 13.36 | 15.29 | 39.96 |
| z11.0 | 11.0 | SFHo | 1.49 | $\ldots$ | $\ldots$ | $\ldots$ |
| z40.0 | 40.0 | SFHo | $\ldots$ | 13.85 | 16.51 | 40.00 |
| s10.8 | 10.8 | DD2 | 1.50 | $\ldots$ | $\ldots$ | $\ldots$ |
| s40.0 | 40.0 | DD2 | 1.82 | $\ldots$ | $\ldots$ | - |
| u11.0 | 11.0 | DD2 | 1.50 | $\ldots$ | $\ldots$ | $\ldots$ |
| u40.0 | 40.0 | DD2 | $\ldots$ | 13.36 | 15.29 | 39.96 |
| z11.0 | 11.0 | DD2 | 1.49 | $\ldots$ | $\ldots$ | $\ldots$ |
| z40.0 | 40.0 | DD2 | $\ldots$ | 13.85 | 16.51 | 40.00 |

Note. For models with successful explosions, the mass of the resulting neutron star is listed. For models which failed to explode, the mass of the black hole for all three cases is given. The results with the SFHo EOS are from this work. The results with the DD2 EOS model are taken from Paper II and Paper IV.
(This table is available in its entirety in machine-readable form.)

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