# Observation, Modern Light-curve Analysis, and $\mathbf{8 9} \mathbf{y r}$ Period Study of the Short-period Algol, AE Cassiopeia 

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#### Abstract

AE Cas was observed some 40 yr ago by Srivastava \& Kandpal and was analyzed by Kopal's Fourier frequency -domain technique. No further precision observations have taken place until the present study, which represents the first modern synthetic analysis of light curves using the 2016 version of the Wilson-Devinney (W-D) Program. It was observed in 2015 October 2, 3 and 23, inclusive, at Dark Sky Observatory in North Carolina with the 0.81 m reflector of Appalachian State University and the 0.9 m reflector at Kitt Peak National Observatory remotely through the Southeastern Association for Research in Astronomy (SARA) consortia. $V, R_{\mathrm{c}}, I_{\mathrm{c}}$ observations were taken. Five times of minimum light were determined from our present observations, which include three primary eclipses and two secondary eclipses. In addition, eight observations at minima were introduced as low weighted times of minimum light from archived All-Sky Automated Survey for Supernovae Variable Star Catalog (ASAS) data and 74 times of minimum light from the literature, some of which were from visual observations. This period study covers an interval of some 89 yr . The period was found to be decaying at a constant rate with a high level of confidence. A $V R_{\mathrm{c}} I_{\mathrm{c}}$ simultaneous W-D Program solution indicates that the system has a mass ratio somewhat less than unity ( $q=0.856 \pm 0.001$ ), and a component temperature difference of $\sim 2060 \mathrm{~K}$. A $q$-search was performed and the mass ratio minimized at the above value. The large temperature difference in the components verifies that the binary is not yet in contact. No spots were needed for the solution. The fill-out of our model is $83.2 \%$ for the primary component (smaller radius) and $99.1 \%$ for the secondary component. So, it is near a classical Algol configuration.


Unified Astronomy Thesaurus concepts: Detached binary stars (375); Stellar evolution (1599); Interacting binary stars (801); Eclipsing binary stars (444); Algol variable stars (24); Contact binary stars (297)
Supporting material: machine-readable tables

## 1. Introduction

Early analyses of eclipsing binaries prior to the mid 1960s relied on many techniques that were not adequate to physically analyze interacting binaries (Wilson 1994). These included graphical techniques like the Russell Merrill rectified method (Russell \& Merrill 1952) and others using spherical and ellipsoidal geometries (i.e., Wood 1971). Many of these early models avoided the physical processes of gravitation and centrifugal force. Kopal's methods (Kopal 1982) included a Fourier analysis frequency-domain approach to the analysis of light curves. Later the potential energy-based methods of modern light-curve analysis were developed, spearheaded by R. E. Wilson \& Devinney (Wilson 1994).

Here we present precision photometry and the first modern light-curve analysis of the near-contact system, AE CAS. The first report of these observations was recently given as a poster paper at the American Astronomical Society Meeting \#234 (Chamberlain et al. 2019).

## 2. History

AE Cas was discovered as an Algol by Hoffmeister (1928). Wood \& Forbes (1963) presented an ephemeris of

$$
\begin{equation*}
\mathrm{HJD}=2433282.83348 \mathrm{~d}+0.75911650 \mathrm{E} \tag{1}
\end{equation*}
$$

the Two Micron All Sky Survey (2MASS) gives a $J-K$ of $0.320 \pm 0.053 \mathrm{mag}$, and the AAVSO Photometric All-Sky Survey, first release (APASS-DR1), gives $B-V=0.53$. Srivastava \& Kandpal (1984) presented $U B V$ photoelectric observations and
analyzed it by a Fourier frequency-domain technique. Three times of minima were presented. The Fourier fit yielded the approximate values, mass ratio $(q)=0.7$, and inclination $(i)=80^{\circ} 4$. In the Catalog and AtLas of Eclipsing Binaries (CALEB) database, ${ }^{4}$ David Bradstreet gave a binary maker potential-based (uses blackbody atmospheres) fit to these light curves. The results were a semi-detached Algol-type solution which included $\Omega_{1,2}$ (gravitational potentials $)=4.3811$ and 3.5856 , fill-out ${ }_{1,2}=81 \%$ and $100 \%, i=76^{\circ}$, and $q=0.9$. Shaw's near-contact binary site ${ }^{5}$ gives a magnitude of $V=12.421$, and the ephemeris

$$
\text { JD Hel Min I }=2451339.6385 d+0.759135 \mathrm{E} .
$$

as well as a light curve (shown in Figure 1).
This system was observed as a part of our student/ professional collaborative studies of interacting binaries using data taken from Dark Sky Observatory (DSO) observations. The observations were taken by R. Samec, D. Caton, and D. Faulkner. Reduction and analyses were done by R. Samec. A survey light curve was taken by the All-Sky Automated Survey for Supernovae (ASAS-SN) ${ }^{6}$ Variable Stars Database (The ASAS-SN Catalog of Variable Stars: II; Shappee et al. 2014 and Kochanek et al. 2017) with a $J-K=0.32$, an ephemeris of

$$
\begin{equation*}
\text { JD Hel MIN I }=2457362.89544+0.7591156 \mathrm{E}, \tag{2}
\end{equation*}
$$

[^0]

Figure 1. Data from J.S. Shaw's near-contact binaries (http://www.physast uga.edu/~jss/ncb/LC/lc00349697.pdf).


Figure 2. $V$ light curves of AE CAS (https://asas-sn.osu.edu/).


Figure 3. $R_{\mathrm{c}}, I_{\mathrm{c}}$, and $R_{\mathrm{c}}-I_{\mathrm{c}}$ color curves on the night of 2016 October 22.
and catalog name ASASSN-V J012700.39+700738.1. It is given as Figure 2.

## 3. $2017 \operatorname{VR}_{\mathbf{c}} I_{\mathbf{c}}$ Photometry

The present observations were taken with the DSO 0.81 m reflector at Philips Gap, North Carolina, on 2016 October 2, 3 and 23 (3.7-11.1 UT), inclusive, with a thermoelectrically


Figure 4. $R_{\mathrm{c}}, I_{\mathrm{c}}$, and $R_{\mathrm{c}}-I_{\mathrm{c}}$ color curves on the night of 2016 October 23.


Figure 5. Finder chart; AE CAS (V), comparison star (C), and check (K).
cooled $\left(-40^{\circ} \mathrm{C}\right) 2 \mathrm{KX} 2 \mathrm{~K}$ Apogee Alta by D. Caton with standard $V R_{\mathrm{c}} I_{\mathrm{c}}$ filters and on October 23 (1.5-11.7 UT) with the 0.9 m reflector at Kitt Peak National Observatory (KPNO) remotely through the The Southeastern Association for Research in Astronomy (SARA) consortia with the liquid nitrogen (LN) cooled ( $-84.6^{\circ} \mathrm{C}$ ) 2KX2K ARC-E2V42-40 chip camera by R. Samec.
Individual observations included 570 in $V, 559$ in $R_{\mathrm{c}}$, and 531 in $I_{\mathrm{c}}$. The probable error of a single observation was 9.9 mmag in $V, 8.5$ in $R_{\mathrm{c}}$, and 9.6 in $I_{\mathrm{c}}$. The nightly $C-K$ values stayed constant throughout the observing run with a precision less than $1 \%$. Exposure times varied from 20 to 80 s in Vand $10-32 \mathrm{~s}$ in Rand I. Figures 3 and 4 show light curves taken from 2016 October 22 and 23. Photometric targets are given in Table 1.

The variable (denoted as $V$ ), also designated TYC 43011388 1 , NSVS 240090, has a position of $\left[\alpha(2000)=01^{\mathrm{h}} 27^{\mathrm{m}} 00.3467\right.$, $\delta(2000)=+82^{\circ} 03^{\prime} 44!^{\prime \prime} 4$ UCAC3: the USNO CCD Astrograph Catalog], $\quad V=12.70-13.50$ (2MASS), a parallax of $1.37 \pm$

Table 1
Photometric Targets

| Star | Label | Name | $V$ |
| :--- | :---: | :---: | :---: | :---: |
| Variable | V | AE CAS, TYC, 4301 1388 1, NSVS 240090 | $0.0(2 \mathrm{MASS})$ |
| Comparison | C | GSC 4301 1907, 3UC321-010572 | $12.70-13.50$ |
| Check | K | GSC 4301 1549, 3UC345-013313 | 12.68 |

Table 2
Photometric Observations of AE CAS

| $\Delta V$ | VHJD <br> $2457660+$ | $\Delta R_{\mathrm{c}}$ | RcHJD <br> $2457660+$ | $\Delta I_{\mathrm{c}}$ | IcHJD <br> $2457660+$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| 0.214 | 3.4915 | 0.214 | 3.4915 | 0.199 | 3.4919 |
| 0.291 | 3.4961 | 0.291 | 3.4961 | 0.295 | 3.5017 |
| 0.311 | 3.5014 | 0.311 | 3.5014 | 0.321 | 3.5036 |
| 0.336 | 3.5034 | 0.336 | 3.5034 | 0.335 | 3.5056 |
| 0.345 | 3.5053 | 0.345 | 3.5053 | 0.318 | 3.5077 |
| 0.334 | 3.5074 | 0.334 | 3.5074 | 0.302 | 3.5119 |
| 0.318 | 3.5116 | 0.318 | 3.5116 | 0.259 | 3.5138 |
| 0.291 | 3.5136 | 0.291 | 3.5136 | 0.231 | 3.5158 |
| 0.275 | 3.5155 | 0.275 | 3.5155 | 0.179 | 3.5201 |

(This table is available in its entirety in machine-readable form.)


Figure 6. The period study of 89 yr indicates a continuous period decrease.
0.05 mas, and a distance of $730 \pm 20 \mathrm{pc}$ (Gaia; Lindegren et al. 2018). The comparison star was denoted as C, and designated GSC 43011907 and 3UC321-010572 with a position of $\quad\left[\alpha(2000)=01^{\mathrm{h}} 27^{\mathrm{m}} 25^{\mathrm{s}} .1189, \quad \delta(2000)=+70^{\circ} 08^{\prime} 44^{\prime \prime} 861\right.$ UCAC3]. The check star (denoted as K ) is also designated as GSC 43011549 and has a position of $\left[\alpha(2000)=01^{\mathrm{h}} 27^{\mathrm{m}}\right.$ $36.11475, \delta(2000)=70^{\circ} 09^{\prime} 66^{\prime \prime} 494$, UCAC3], $V=11.880$, and a distance of 649 pc (2MASS).

The finder chart is given as Figure 5 with the variable star (V), comparison star (C), and check star (K) shown. Our observations are listed in Table 2, with differences in magnitude by filters $\Delta V, \Delta R_{\mathrm{c}}$, and $\Delta I_{\mathrm{c}}$ (variable star minus comparison star in each filter).

## 4. 89 yr Orbital Period Study

A total of 88 times of minimum light were used in our period study beginning with 14 timings by Hoffmeister (1940). Many of the subsequent timings were taken by the noted observer, Kurt


Figure 7. (a) $V, R_{\mathrm{c}}$ light curves and $V-R$ color curves (variable comparison) with magnitudes phased with Equation (3). (b) $R_{\mathrm{c}}, I_{\mathrm{c}}$ light curves and $R_{\mathrm{c}}-I_{\mathrm{c}}$ color curves (variable comparison) with magnitudes phased with Equation (3).

Locher (1989a, 1989b, 1989c, 1990a, 1990b, 1991a, 1991b, 1992a, 1992b, 1992c, 1993a, 1993b, 1994, 1995, 1997a, 1997b, 1998a, 1998b, 2000a, 2000b, 2002a, 2002b, 2005 2007). These are listed in Table 3. Five times of minimum light were determined from our present observations, which include three primary eclipses and two secondary eclipses (with errors):

HJD Min $I=2457663.5055 \pm 0.0005,2457684.76093 \pm$ $0.00005,2457684.7616 \pm 0.0001$

HJD Min II $=2457663.8843 \pm 0.0006$, and 2457664.652.
In addition, eight observations at minima were introduced as low weighted times of minimum light taken from archived AllSky Automated Survey for Supernovae Variable Star Catalog (ASAS) data and as well as a number of early visual observations (the amplitude of the primary eclipse is nearly 1 mag ). This study covers an interval of some 89 yr of observations.

Table 3
$O-C$ Residual Calculations of AE CAS

|  | $\begin{aligned} & \text { Epochs } \\ & 2400000+ \end{aligned}$ | Cycles | Linear Residuals | Quadratic Residuals | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 25411.5000 | -42514.0 | -0.0037 | 0.0071 | Hoffmeister (1940) |
| 2 | 25424.4050 | -42497.0 | -0.0037 | 0.0071 | Hoffmeister (1940) |
| 3 | 25433.5090 | -42485.0 | -0.0092 | 0.0016 | Hoffmeister (1940) |
| 4 | 25436.5540 | -42481.0 | -0.0006 | 0.0101 | Hoffmeister (1940) |
| 5 | 25439.5600 | -42477.0 | -0.0311 | -0.0204 | Hoffmeister (1940) |
| 6 | 25465.4110 | -42443.0 | 0.0098 | 0.0204 | Hoffmeister (1940) |
| 7 | 25481.3490 | -42422.0 | 0.0062 | 0.0168 | Hoffmeister (1940) |
| 8 | 25493.4590 | -42406.0 | -0.0297 | -0.0191 | Hoffmeister (1940) |
| 9 | 25503.3390 | -42393.0 | -0.0183 | -0.0077 | Hoffmeister (1940) |
| 10 | 25512.4650 | -42381.0 | -0.0017 | 0.0088 | Hoffmeister (1940) |
| 11 | 25525.3550 | -42364.0 | -0.0168 | -0.0063 | Hoffmeister (1940) |
| 12 | 25644.5300 | -42207.0 | -0.0237 | -0.0136 | Hoffmeister (1940) |
| 13 | 25650.6180 | -42199.0 | -0.0087 | 0.0015 | Hoffmeister (1940) |
| 14 | 25685.5340 | -42153.0 | -0.0123 | -0.0022 | Hoffmeister (1940) |
| 15 | 25688.5660 | -42149.0 | -0.0167 | -0.0067 | Hoffmeister (1940) |
| 16 | 26391.5390 | -41223.0 | 0.0104 | 0.0186 | Hoffmeister (1940) |
| 17 | 26769.5450 | -40725.0 | -0.0257 | -0.0185 | Hoffmeister (1940) |
| 18 | 28108.6530 | -38961.0 | -0.0067 | -0.0028 | Hoffmeister (1940) |
| 19 | 34982.4860 | -29906.0 | -0.0123 | -0.0203 | Hoffmeister (1940) |
| 20 | 33282.8335 | -32145.0 | 0.0066 | 0.0009 | Wood \& Forbes (1963) |
| 21 | 43435.3260 | -18771.0 | 0.0179 | 0.0060 | Srivastava \& Kandpal (1984) |
| 22 | 43454.3020 | -18746.0 | 0.0159 | 0.0040 | Srivastava \& Kandpal (1984) |
| 23 | 44144.3400 | -17837.0 | 0.0131 | 0.0014 | Srivastava \& Kandpal (1984) |
| 24 | 47491.2910 | -13428.0 | 0.0007 | -0.0090 | Locher (1989a) |
| 25 | 47557.3220 | -13341.0 | -0.0118 | -0.0215 | Locher (1989b) |
| 26 | 47777.4960 | -13051.0 | 0.0171 | 0.0077 | Brno 30 |
| 27 | 47777.5010 | -13051.0 | 0.0221 | 0.0127 | Brno 30 |
| 28 | 47786.6030 | -13039.0 | 0.0147 | 0.0053 | Locher (1989c) |
| 29 | 47885.2910 | -12909.0 | 0.0170 | 0.0076 | Locher (1990a) |
| 30 | 48127.4530 | -12590.0 | 0.0195 | 0.0104 | Locher (1990b) |
| 31 | 48260.3090 | -12415.0 | 0.0293 | 0.0204 | Locher (1991a) |
| 32 | 48489.5340 | -12113.0 | -0.0001 | -0.0089 | Locher (1991b) |
| 33 | 48533.5860 | -12055.0 | 0.0229 | 0.0142 | Locher (1992a) |
| 34 | 48820.5270 | -11677.0 | 0.0162 | 0.0078 | Locher (1992b) |
| 35 | 48963.2360 | -11489.0 | 0.0105 | 0.0023 | Locher (1992c) |
| 36 | 49031.5560 | -11399.0 | 0.0096 | 0.0015 | Borovic' ka (1993) |
| 37 | 49054.3250 | -11369.0 | 0.0050 | -0.0031 | Locher (1993a) |
| 38 | 49173.4890 | -11212.0 | -0.0129 | -0.0209 | Locher (1993b) |
| 39 | 49561.4220 | -10701.0 | 0.0093 | 0.0018 | Locher (1994) |
| 40 | 49948.5800 | -10191.0 | 0.0157 | 0.0087 | Locher (1995) |
| 41 | 50488.3090 | -9480.0 | 0.0099 | 0.0036 | Locher (1997a) |
| 42 | 50670.4930 | -9240.0 | 0.0049 | -0.0012 | Locher (1997b) |
| 43 | 50762.3480 | -9119.0 | 0.0063 | 0.0004 | Locher (1998a) |
| 44 | 50863.3170 | -8986.0 | 0.0122 | 0.0064 | Locher (1998b) |
| 45 | 51341.5460 | -8356.0 | -0.0049 | -0.0099 | Locher (1999) |
| 46 | 51448.6000 | -8215.0 | 0.0131 | 0.0082 | Locher (2000a) |
| 47 | 51672.5380 | -7920.0 | 0.0105 | 0.0059 | Locher (2000b) |
| 48 | 52215.2940 | -7205.0 | -0.0049 | -0.0085 | Locher (2002a) |
| 49 | 52366.3710 | -7006.0 | 0.0071 | 0.0037 | Locher (2002b) |
| 50 | 52532.6150 | -6787.0 | 0.0037 | 0.0005 | Locher (2007) |
| 51 | 52964.5600 | -6218.0 | 0.0089 | 0.0066 | Diethelm (2004) |
| 52 | 53257.5690 | -5832.0 | -0.0027 | -0.0045 | Locher (2005) |
| 53 | 53579.4470 | -5408.0 | 0.0081 | 0.0069 | Locher (2005) |
| 54 | 54031.8730 | -4812.0 | -0.0019 | -0.0022 | Nelson (2007) |
| 55 | 55894.7510 | -2358.0 | -0.0062 | -0.0027 | Diethelm (2004) |
| 56 | 57973.9820 | 381.0 | -0.0070 | 0.0016 | ASAS |
| 57 | 57696.9050 | 16.0 | -0.0049 | 0.0030 | ASAS |
| 58 | 57362.8950 | -424.0 | -0.0018 | 0.0053 | ASAS |
| 59 | 57044.8270 | -843.0 | 0.0018 | 0.0081 | ASAS |
| 60 | 57046.7180 | -840.5 | -0.0050 | 0.0013 | ASAS |
| 61 | 57619.0940 | -86.5 | -0.0061 | 0.0017 | ASAS |
| 62 | 57704.8750 | 26.5 | -0.0057 | 0.0023 | ASAS |
| 63 | 57008.7690 | -890.5 | 0.0020 | 0.0082 | ASAS |

Table 3
(Continued)

|  | $\begin{aligned} & \text { Epochs } \\ & 2400000+ \end{aligned}$ | Cycles | Linear Residuals | Quadratic Residuals | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 64 | 50708.4521 | 381.0 | -0.0070 | 0.0016 | Safar \& Zejda (2000) |
| 65 | 51423.5381 | 16.0 | -0.0049 | 0.0030 | Agerer \& Hubscher (2001) |
| 66 | 51913.9283 | -424.0 | -0.0018 | 0.0053 | Nelson (2002) |
| 67 | 51946.9524 | -843.0 | 0.0018 | 0.0081 | Nelson (2002) |
| 68 | 52041.4595 | -840.5 | -0.0050 | 0.0013 | Blaettler (2001) |
| 69 | 52585.7598 | -86.5 | -0.0061 | 0.0017 | Samolyk (2013) |
| 70 | 52230.4804 | 26.5 | -0.0057 | 0.0023 | Brát et al. (2007) |
| 71 | 53251.4967 | -890.5 | 0.0020 | 0.0082 | Hubscher et al. (2005) |
| 72 | 54017.4498 | -9190.0 | 0.0080 | 0.0020 | Hubscher \& Walter (2007) |
| 73 | 54843.3705 | -8248.0 | 0.0022 | -0.0027 | Lampens et al. (2010) |
| 74 | 54843.3719 | -7602.0 | 0.0004 | -0.0038 | Lampens et al. (2010) |
| 75 | 55060.4764 | -7558.5 | 0.0027 | -0.0014 | Hubscher et al. (2010) |
| 76 | 55073.3818 | -7434.0 | -0.0007 | -0.0047 | Hubscher et al. (2010) |
| 77 | 55473.4374 | -6717.0 | 0.0100 | 0.0070 | Hubscher (2011) |
| 78 | 55804.4133 | -7185.0 | -0.0009 | -0.0045 | Hubscher \& Lehmann (2012) |
| 79 | 55940.2959 | -5840.0 | -0.0020 | -0.0039 | Marino (2012) |
| 80 | 56274.3137 | -4831.0 | -0.0018 | -0.0022 | Hubscher (2014) |
| 81 | 56567.3344 | -3743.0 | -0.0045 | -0.0032 | Hubscher (2014) |
| 82 | 56949.5505 | -3743.0 | -0.0031 | -0.0018 | Hubscher (2015) |
| 83 | 57260.4082 | -3457.0 | -0.0071 | -0.0054 | Hubscher (2016) |
| 84 | 57663.5055 | -28.0 | -0.0031 | 0.0047 | Present Observations |
| 85 | 57663.8843 | -27.5 | -0.0039 | 0.0040 | Present Observations |
| 86 | 57664.6518 | -26.5 | 0.0045 | 0.0124 | Present Observations |
| 87 | 57684.7609 | 0.0 | -0.0031 | 0.0048 | Present Observations |
| 88 | 57684.7616 | 0.0 | -0.0024 | 0.0055 | Present Observations |

(This table is available in machine-readable form.)

## Q-Search, AE Cas



Figure 8. Mass ratio search conducted with a number of solutions which minimized at $\sim 0.86$.

The following linear and quadratic ephemerides were determined from the times of minimum light:

$$
\begin{align*}
& \text { JD Hel Min I } \\
& =2457684.7640 \pm 0.0013 \mathrm{~d}+0.75912076 \pm 0.00000008 \mathrm{E} \tag{3}
\end{align*}
$$

JD Hel Min $I=2457684.7561 \pm 0.0013 \mathrm{~d}$
$+0.75911881 \pm 0.00000022 \mathrm{E}$
$-0.000000000048 \pm 0.000000000004 \mathrm{E}^{2}$.

The $O-C$ quadratic and linear residual calculations are given in Table 3. The plot of the quadratic residuals are displayed in Figure 6. The quadratic term is statistically significant at about $\sim 11 \sigma$. This ephemeris yields a $\dot{P}=-4.62 \pm 0.014 \times 10^{-8}$ day $(\mathrm{yr})^{-1}$ or a mass exchange rate of $\frac{d M}{d t}=\frac{\dot{P} M_{1} M_{2}}{3 P\left(M_{1}-M_{2}\right)}=$ $(-1.52 \pm 0.54) \times 10^{7} \mathrm{Myr}^{-1}$ in a conservative scenario. These are typical rates of magnetic braking (Qian et al. 2017).

This 89 yr trend is probably due to magnetic braking for this solar-type binary. A continuance of this trend would lead to the formation of a W UMa binary and ultimately the system would become unstable, resulting in a red novae event and finally a single fast-rotating spectrally bluer star (Tylenda \& Kamiński 2016). Alternately, the period change could be a part of a long sinusoidal variation due to the presence of a distant third body. However, third-light iterations resulted in nonphysical, negative values in the synthetic light-curve calculation.

## 5. Light Curves

The $V R_{\mathrm{c}} I_{\mathrm{c}}$ phased light curves calculated from Equation (3) are shown in Figures 7(a) and (b). Light-curve magnitude means at quarter phases are given in Table 4. The O'Connell effect, an indicator of spot activity, is negligible. For a solartype binary such as this, that does not mean that there is no magnetic activity. Likely, the surface is saturated with magnetic activity but is averaging out in flux level, so the light curves are not a good means of detecting magnetic phenomena. The differences in minima are large, $0.67-0.86 \mathrm{mag}$ from $I_{\mathrm{c}}$ to $V$, probably indicating noncontact light curves. The amplitudes of

Table 4
Light-curve Characteristics for AE CAS

| Filter | Phase | Mag |  | Phase | Mag |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Min I |  |  | Max I |
|  | 0.0 |  |  | 0.25 |  |  |
| V |  |  | $0.279 \pm 0.018$ |  |  | $-0.739 \pm 0.016$ |
| $R$ |  |  | $0.331 \pm 0.013$ |  |  | $-0.617 \pm 0.012$ |
| I |  |  | $0.309 \pm 0.019$ |  |  | $-0.551 \pm 0.008$ |
|  |  |  | Min II |  |  | Max II |
| Filter | Phase | Mag |  | Phase | Mag |  |
|  | 0.5 |  |  | 0.75 |  |  |
| V |  |  | $-0.586 \pm 0.005$ |  |  | $-0.738 \pm 0.004$ |
| $R$ |  |  | $-0.443 \pm 0.008$ |  |  | $-0.611 \pm 0.014$ |
| I |  |  | $-0.358 \pm 0.007$ |  |  | $-0.565 \pm 0.008$ |
| Filter |  | Min I-Max I |  | Filter |  | Min I-Min II |
| V |  | $1.018 \pm 0.034$ |  | V |  | $0.865 \pm 0.023$ |
| $R$ |  | $0.947 \pm 0.025$ |  | $R$ |  | $0.773 \pm 0.020$ |
| I |  | $0.860 \pm 0.027$ |  | I |  | $0.666 \pm 0.026$ |
| Filter |  | Max I-Max II |  | Filter |  | Min II-Max I |
| V |  | $0.001 \pm 0.020$ |  | V |  | $0.153 \pm 0.021$ |
| $R$ |  | $0.006 \pm 0.026$ |  | $R$ |  | $0.174 \pm 0.020$ |
| I |  | $-0.014 \pm 0.016$ |  | I |  | $0.193 \pm 0.015$ |

the light curves are $0.86-1.02 \mathrm{mag}$ in $I_{\mathrm{c}}$ to $V$ indicating a fairly high inclination and high mass ratio for the binary. The $V-I_{\mathrm{c}}$ and $R-I_{\mathrm{c}}$ color curves fall at phase 0.0 , which is characteristic of a contact binary, however the color curves rise slightly at phase 0.5 , which indicates that the secondary component is underfilling its Roche lobe. Thus, the shape of the curves indicates a near-contact semi-detached binary coming into contact.

## 6. Temperature

2MASS gives $J-K=0.320 \pm 0.053$ for the binary. The APASS-DR9 gives $B-V=0.53$. These correspond to an $\sim$ F7 $\pm 2 \mathrm{~V}$ eclipsing binary which yields a temperature of $6250 \pm 300$ K. Fast-rotating binary stars of this type are noted for having convective atmospheres, so spots are expected.

## 7. Light-curve Solution

The $V, R_{\mathrm{c}}$, and $I_{\mathrm{c}}$ curves were pre-modeled with binary maker 3.0 (Bradstreet \& Steelman 2002) and fits were determined in the three filter bands. The result of the best hand-fit was that of a classical Algol eclipsing binary with fill outs of $85 \%$ and $100 \%$. This would indicate in themselves, that the Roche Lobes of the secondary component was filling while the primary component was underfilling its critical surface. The parameters were then averaged and input into a three-color simultaneous light-curve calculation using the 2016 WilsonDevinney (W-D) Program (Wilson \& Devinney 1971; Wilson 1990, 1994, 2008, 2012; Van Hamme \& Wilson 1998, 2007; Wilson et al. 2010; Wilson \& Van Hamme 2014). Convective parameters $g=0.32$ and $A=0.5$ were used. The solution was computed in Mode 2 in order to calculate the best configuration and it converged to a solution in a detached mode

Table 5
$V, R_{\mathrm{c}}, I_{\mathrm{c}} \mathrm{W}-\mathrm{D}$ Program Solution Parameters

| Parameters | Values |
| :--- | :--- |
| $\lambda_{\mathrm{V}}, \lambda_{\mathrm{R}}, \lambda_{\mathrm{I}}(\mathrm{nm})$ | $550,640,790$ |
| $g_{1}, g_{2}$ | 0.32 |
| $A_{1}, A_{2}$ | 0.5 |
| Inclination $\left(^{\circ}\right.$ ) | $75.88 \pm 0.03$ |
| $T_{1}, T_{2}(\mathrm{~K})$ | $6250,4189 \pm 1$ |
| $\Omega_{1}, \Omega_{2}$ | $4.2186 \pm 0.0026,3.5435 \pm 0.0020$ |
| $q\left(m_{2} / m_{1}\right)$ | $0.8560 \pm 0.0005$ |
| Fill outs: $F_{1}, F_{2}(\%)$ | $83.1969 \pm 0.0005,99.0737 \pm 0.0006$ |
| $L_{1} /\left(L_{1}+L_{2}+L_{3}\right)_{\mathrm{I}}$ | $0.7808 \pm 0.0004$ |
| $L_{1} /\left(L_{1}+L_{2}+L_{3}\right)_{\mathrm{R}}$ | $0.8279 \pm 0.0008$ |
| $L_{1} /\left(L_{1}+L_{2}+L_{3}\right)_{\mathrm{V}}$ | $0.8789 \pm 0.0007$ |
| $\mathrm{JD} \mathrm{D}_{\mathrm{o}}($ days $)$ | $2457684.76120 \pm 0.00010$ |
| Period (days) | $0.759141 \pm 0.000008$ |
| $r_{1} / a, r_{2} / a$ (pole) | $0.2941 \pm 0.0017,0.3389 \pm 0.0016$ |
| $r_{1} / a, r_{2} / a$ (point) | $0.3180 \pm 0.0023,0.4386 \pm 0.0097$ |
| $r_{1} / a, r_{2} / a$ (side) | $0.3014 \pm 0.0018,0.3547 \pm 0.0020$ |
| $r_{1} / a, r_{2} / a$ (back) | $0.3113 \pm 0.0021,0.3840 \pm 0.0029$ |

with no indication that one should change modes (Mode 5 is the classical Algol with the primary underfilling its critical Roche lobe and the secondary filling its critical lobe. Mode 4 is opposite, with the primary underfilling and the secondary critically filling.)

The eclipses were not total, so a mass ratio search (q-search) was conducted converging on the original solution with a high mass ratio of 0.86 . The q-search is graphed in Figure 8 and the solution is given as Table 5.

This result is not definitive, but a radial velocity curve is needed for certainty. The normalized $V$ and the $R_{\mathrm{c}}, I_{\mathrm{c}}$ light


Figure 9. (a) $V, R_{\mathrm{c}}$ normalized fluxes and the $B-V$ color curves overlaid by the detached solution for AE CAS. (b) $R_{\mathrm{c}}, I_{\mathrm{c}}$ normalized fluxes and the $B-V$ color curves overlaid by the detached solution of AE CAS.
curves with the detached solution curves overlain are displayed in Figures 9(a) and (b). The Roche lobe surfaces are given in Figures 10(a)-(d).

## 8. Discussion

AE Cas is a dwarf solar-type binary in an unusual but a very nearly classical Algol-type configuration. The synthetic light curve determined fill outs of the primary and secondary components were $83 \%$ and $99 \%$, respectively. This configuration could result after a set of evolutionary mass exchanges called the Algol paradox. However, the process was evidently sped up by magnetic braking. Otherwise this process would probably take longer than the age of the universe for the formation of such a pre-W UMa binary. Its $J-K$ color index indicates a surface temperature of $\sim 6250 \mathrm{~K}$ for the primary component. The secondary component has a temperature of $\sim 4200 \mathrm{~K}$ (K6V), which means that it is over-massive as compared to a single main-sequence star of this temperature. The light-curve solution mass ratio is $\sim 0.86$ rather than the expected $\sim 0.54$. However, the Algol paradox specifies that mass exchanges have been made between components so masses should not match main-sequence counter parts. We note that the photometric $q$ determinations are only estimates of the physical mass ratio and masses obtained by a thorough radial

phase $=0.24$


$$
\text { phase }=0.50
$$



Figure 10. (a) Geometrical representation at phase 0.00 of AE CAS. (b) Geometrical representation at phase 0.25 of AE CAS. (c) Geometrical representation at phase 0.50 of AE CAS. (d) Geometrical representation at phase 0.75 of AE CAS.
velocity study. The inclination is $76^{\circ}$ so the eclipses are partial. No spots (asymmetries) were discernible.

## 9. Conclusion

The period study of this pre-contact W UMa binary has an 89 yr time duration. The period is found to be continually
decreasing at a high level of confidence. This is expected for a solar-type binary undergoing magnetic braking. This could be also due to a mass transfer from the primary component onto the secondary, which seems untenable for the configuration. The magnetic braking scenario will result in contact and then overcontact into an A-type W UMa binary. Continued magnetic braking will cause the system to slowly coalesce. This is due to loses in angular momentum from ion winds moving radially outward on stiff magnetic field lines rotating with the binary (out to the Alfvén radius). Ultimately, one would expect that the binary will become a rather normal, fast-rotating single A7Vtype field star after a red novae coalescence event (with a $\sim 5 \%$ mass loss; Tylenda \& Kamiński 2016). Of course, radial velocity curves are needed to confirm this proposed scenario and to obtain absolute (not relative) system parameters.

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## References

Agerer, F., \& Hubscher, J. B. 2001, IBVS, 5016, 2
Blaettler, E. 2001, BBSAG, 125, 3
Borovic'ka, J. 1993, IBVS, 3877, 3
Brát, L., Zejda, M., \& Svoboda, P. 2007, OEJV, 0074, 1
Bradstreet, D. H., \& Steelman, D. P. 2002, BAAS, 34, 1224
Chamberlain, H., Samec, R., Caton, D. B., \& Faulkner, D. R. 2019, BAAS, 51, 4
Diethelm, R. 2004, IBVS, 5543, 3
Hoffmeister, C. 1928, AN, 234, 33
Hoffmeister, C. 1940, KVeBB, 5, 3.1
Hubscher, J. 2011, IBVS, 5984, 3
Hubscher, J. 2014, IBVS, 6118, 4
Hubscher, J. 2015, IBVS, 6152, 3
Hubscher, J. 2016, IBVS, 6157, 3
Hubscher, J., \& Lehmann, P. B. 2012, IBVS, 6026, 4
Hubscher, J., Lehmann, P. B., Monninger, G., Steinbach, H.-M., \& Walter, F. 2010, IBVS, 5941, 2
Hubscher, J., Paschke, A., \& Walter, F. 2005, IBVS, 5657, 4

Hubscher, J., \& Walter, F. 2007, IBVS, 5761, 2
Kochanek, C. S., Shappee, B. J., Stanek, K. Z., et al. 2017, PASP, 129, 104502
Kopal, Z. 1982, Ap\&SS, 81, 123
Lampens, P., Kleidis, S., Van Cauteren, P., et al. 2010, IBVS, 5933, 2
Lindegren, L., Hernández, J., Bombrun, A., et al. 2018, A\&A, 616A, 2
Locher, K. 1989a, BBSAG, 90, 3
Locher, K. 1989b, BBSAG, 91, 4
Locher, K. 1989c, BBSAG, 93, 3
Locher, K. 1990a, BBSAG, 93, 3
Locher, K. 1990b, BBSAG, 96, 2
Locher, K. 1991a, BBSAG, 97, 4
Locher, K. 1991b, BBSAG, 98, 3
Locher, K. 1992a, BBSAG, 99, 3
Locher, K. 1992b, BBSAG, 101, 3
Locher, K. 1992c, BBSAG, 102, 3
Locher, K. 1993a, BBSAG, 103, 2
Locher, K. 1993b, BBSAG, 104, 2
Locher, K. 1994, BBSAG, 107, 3
Locher, K. 1995, BBSAG, 110, 5
Locher, K. 1997a, BBSAG, 114, 5
Locher, K. 1997b, BBSAG, 115b, 2
Locher, K. 1998a, BBSAG, 116, 6
Locher, K. 1998b, BBSAG, 117, 4
Locher, K. 1999, BBSAG, 121, 4
Locher, K. 2000a, BBSAG, 121, 4
Locher, K. 2000b, BBSAG, 121, 2
Locher, K. 2002a, BBSAG, 127, 2
Locher, K. 2002b, BBSAG, 128, 2
Locher, K. 2005, OEJV, 3, 1
Locher, K. 2007, IBVS, 5438, 4
Marino, G. 2012, IBVS, 6033, 3, https://konkoly.hu/pub/ibvs/6001/ 6033.pdf

Nelson, R. H. 2002, IBVS, 5224, 1
Nelson, R. H. 2007, IBVS, 5701, 2
Qian, S.-B., He, J.-J., Zhang, J., et al. 2017, RAA, 17, 087
Russell, H. N., \& Merrill, J. E. 1952, Contributions from the Princeton University Observatory (Princeton, NJ: Princeton Univ. Observatory)
Safar, J., \& Zejda, M. 2000, IBVS, 4887, 2
Samolyk, G. 2013, Javso, 41, 122
Shappee, B. J., Prieto, J. L., Grupe, D., et al. 2014, ApJ, 788, 48
Srivastava, J. B., \& Kandpal, C. D. 1984, A\&A, 34, 281
Tylenda, R., \& Kamiński, T. 2016, A\&A, 592, A134
Van Hamme, W., \& Wilson, R. E. 1998, BAAS, 30, 1402
Van Hamme, W., \& Wilson, R. E. 2007, ApJ, 661, 1129
Wilson, R. E. 1979, ApJ, 234, 1054
Wilson, R. E. 1990, ApJ, 356, 613
Wilson, R. E. 1994, PASP, 106, 921
Wilson, R. E. 2008, ApJ, 672, 575
Wilson, R. E. 2012, AJ, 144, 73
Wilson, R. E., \& Devinney, E. J. 1971, ApJ, 166, 605
Wilson, R. E., \& Van Hamme, W. 2014, ApJ, 780, 151
Wilson, R. E., Van Hamme, W., \& Terrell, D. 2010, ApJ, 723, 1469
Wood, D. B. 1971, AJ, 76, 701
Wood, D. B., \& Forbes, J. E. 1963, AJ, 68, 257


[^0]:    ${ }_{5}$ http://caleb.eastern.edu/
    5 http://www.physast.uga.edu/~jss/ncb/
    6 https://asas-sn.osu.edu/

