#### PAPER • OPEN ACCESS

# Does Pizzella's experiment violate causality?

To cite this article: Eugene V Stefanovich 2017 J. Phys.: Conf. Ser. 845 012016

View the article online for updates and enhancements.

### You may also like

- <u>Resonant gravitational wave antennas for</u> <u>stochastic background measurements</u> Pia Astone, G V Pallottino and G Pizzella
- Detection of gravitational waves L Ju, D G Blair and C Zhao
- <u>The cryogenic detector of gravitational</u> <u>waves in Frascati</u> U Giovanardi, V lafolla, P Napoleoni et al.





DISCOVER how sustainability intersects with electrochemistry & solid state science research



This content was downloaded from IP address 18.119.105.239 on 26/04/2024 at 15:26

IOP Conf. Series: Journal of Physics: Conf. Series 845 (2017) 012016

## Does Pizzella's experiment violate causality?

#### Eugene V Stefanovich

1763 Braddock Court, San Jose, CA 95125, USA

E-mail: eugene\_stefanovich@usa.net

Abstract. Recent experiments, performed by Prof. Pizzella's team with relativistic electron bunches, indicate that Coulomb field is rigidly attached to the charge's instantaneous position. Despite a widespread opinion, this fact does not violate causality in moving reference frames. To see that, one should apply the Wigner – Dirac theory of relativistic dynamics and take into account that the Lorentz boost generator depends on interaction. Then one can show that interaction remains instantaneous in all reference frames.

#### 1. Experiment at Frascati

In 2012 the team of Prof. Pizzella at the Frascati National Laboratory performed a remarkable experiment [1] that observed rigid connection between electric charge and its Coulomb field. In order to see how surprising this result is from the point of view of the traditional Maxwell-Liénard-Wiechert electrodynamics, let us turn to Fig. 1.

In three panels 1 (a) $\rightarrow$ (b) $\rightarrow$ (c) we show the sequence of events expected in the traditional theory. The snapshot 1 (a) is taken just before the electron bunch left the accelerator's pipe. In this case the bunch's field is shielded by the pipe's metal, so there is no electric field in the surrounding space.

In two frames 1 (b) - (c) the bunch has left the pipe. The emerged force field has two components. First, there is an expanding spherical electromagnetic wave (radiation field) centered at the pipe's exit. Second, there is a non-radiating bound Coulomb field, which is squeezed (or Lorentz-contracted [2]) in the direction of the bunch's motion, thus forming a narrow disk.

According to special relativity, electric field lines of the Coulomb disk cannot "leak" outside the "light cone" bounded by the expanding sphere of the electromagnetic wave. Therefore, the transverse dimension d of the disk grows with time according to formula

$$d \approx 2ct/\gamma \approx 2L/\gamma \tag{1}$$

where L is the distance traveled by the bunch from the pipe's exit and  $\gamma \equiv (1 - v^2/c^2)^{-1/2}$  is the usual relativistic factor. In the Frascati experiment, the energies of electrons in the beam were 500 MeV, which corresponded to the Lorentz contraction factor of  $\gamma \approx 1000$ . At the longest experimental travel distance of 5.5 m the expected size of the Coulomb disk was not greater than 11 mm — too small to have any effect on the field sensors placed around the beam.

In the parallel sequence of frames 1 (d) $\rightarrow$ (e) $\rightarrow$ (f) we present actual results of the Frascati experiment. In contrast to theoretical expectations, the size of the Coulomb field's disk did not

Content from this work may be used under the terms of the Creative Commons Attribution 3.0 licence. Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI. Published under licence by IOP Publishing Ltd 1



Figure 1. Time evolution of the electric field of an electron bunch (small circle) leaving the accelerator pipe (rectangle): (a) $\rightarrow$ (b) $\rightarrow$ (c) Maxwell–Liénard– Wiechert theory; (d) $\rightarrow$ (e) $\rightarrow$ (f) Frascati experiment. Broken line circle fragments show the expanding spherical electromagnetic wave. Groups of lines perpendicular to the beam's axis represent the Coulomb field disk viewed from its side.

grow in a linear fashion (1). Instead, measurements suggested that the field's disk emerged from the accelerator fully formed in the entire space (even beyond the light cone) and did not change with time, apart from the uniform movement together with the bunch.

This fact can be interpreted as an indication of an instantaneous force between charges in the bunch and in the field sensors. The idea about electromagnetic interactions being composed of both instantaneous (bound) and retarded (radiation) parts is not new. It was repeatedly expressed theoretically [3, 4, 5], and electromagnetic superluminal effects were seen in experiments as well [6, 7, 8]. However, these ideas and experiments are usually met with scepticism, because they violate the special relativistic ban on faster-than-light propagation of signals.

#### 2. Ban of superluminal signals

To understand why special relativity does not tolerate such superluminal effects, consider the time evolution of the instantaneous Coulomb field shown in three consecutive snapshots in Fig.  $2 (a) \rightarrow (b) \rightarrow (c)$ .<sup>1</sup> Frame 2 (a) is taken just before the bunch has left the accelerator's pipe, frame 2 (b) shows the exact instant of the exit, and 2 (c) is taken a moment after this event. This time, for clarity, we chose not to show the spherical electromagnetic waves, because according to the experiment [1], their signals are weaker by an order of magnitude. We also placed two electric field sensors next to the pipe's exit.

From the point of view of the observer at rest O, the field's disk forms instantaneously (panel 2 (b)), so the three events A (the bunch's exit from the pipe), B and C (clicks of the sensors) occur simultaneously, despite the fact that B and C are caused by the event A and separated from it by a considerable distance.<sup>2</sup>

In three frames 2 (d) $\rightarrow$ (e) $\rightarrow$ (f) we show how this situation looks from the point of view of an inertial observer O' moving with high velocity in the vertical direction from the bottom of the page to its top.<sup>3</sup> To draw these panels we employed Lorentz transformations of special relativity

$$t' = t \cosh \theta - (y/c) \sinh \theta \tag{2}$$

$$x' = x \tag{3}$$

$$y' = y \cosh \theta - ct \sinh \theta \tag{4}$$

$$z' = z \tag{5}$$

<sup>1</sup> they are basically the same as in Fig.  $1(d) \rightarrow (e) \rightarrow (f)$ 

 $<sup>^2\,</sup>$  from 3 cm to 55 cm in the Frascati setup

<sup>&</sup>lt;sup>3</sup> To be consistent with [1], we call it y-direction.



Figure 2. Time evolution of the bunch's instantaneous Coulomb field: (a) $\rightarrow$ (b) $\rightarrow$ (c) in the rest frame; (d) $\rightarrow$ (e) $\rightarrow$ (f) in the moving frame, as predicted by Lorentz transformations (2) - (5); (g) $\rightarrow$ (h) $\rightarrow$ (i) in the moving frame, as predicted by the Wigner-Dirac theory. Squares mark positions of electric field sensors. Filled squares indicate "clicking" sensors.

where parameter  $\theta$  was related to the observer's velocity by formula  $v = c \tanh \theta$ .

The absurdity of these drawings is clear already from the panel 2 (d), where a portion of the Coulomb field's disk has emerged even before the bunch has left the accelerator's pipe. This means that the "effect" B occurred earlier than the "cause" A in a clear violation of the principle of causality. Two other panels show the further sequence of events: the bunch leaves the accelerator 2 (e), the lower sensor clicks 2 (f).

To avoid such blatant violations of causality, special relativity forbids faster-than-light formation of the field's disk. However, in a clear disrespect of this ban, the Frascati experiment seems to show exactly such a behavior in the laboratory. We are not in a position to judge the validity of conclusions drawn by the Frascati team. Right now the most important next step would be to double check their results by repeating these remarkable measurements, preferably in a different laboratory.<sup>4</sup> Our goal here is more modest: We are going to show that there is no inherent contradiction between instantaneously propagating interactions and the principle of causality.

#### 3. Relativistic interactions between particles

Our claim is that charges in the bunch and in field sensors may, indeed, interact via an instantaneous action-at-a-distance potential. The usual attitude is that such potentials are impossible because (i) they cannot be relativistically invariant and (ii) they violate causality. We will challenge the latter statement in section 4. Here we would like to mention that the former statement is not correct as well.

First explicit construction of a relativistically invariant multiparticle model with instantaneous forces was undertaken by Bakamjian and Thomas [11]. They used the theory of unitary representations of the Poincaré group developed earlier by Wigner [12] and Dirac [13]. According to this theory [14], interactions must modify generators of the Poincaré group representation, so that the commutators of generators remain intact. The full Hamiltonian (=

<sup>4</sup> Hopefully, this will answer all outstanding questions regarding the interpretation of the Frascati experiment [9, 10].

IOP Publishing

the generator of time translations) is obtained by adding the "potential energy" operator V to the free Hamiltonian:  $H = H_0 + V$ . In Dirac's instant form of relativistic dynamics, theory is consistent with adding an interacting "potential boost" Z to the noninteracting boost generator:  $\mathbf{K} = \mathbf{K}_0 + \mathbf{Z}$ . Generators of space translations and rotations remain interaction-free:  $\mathbf{P} = \mathbf{P}_0$ ,  $\mathbf{J} = \mathbf{J}_0$ .

If this construction is performed in a two-particle system,<sup>5</sup> then the Hamiltonian H is a function of positions  $\mathbf{r}_j$  and momenta  $\mathbf{p}_j$  of both particles. Time dependencies of these observables are obtained by standard quantum mechanical formulas

$$\mathbf{r}_{j}(t) = e^{\frac{i}{\hbar} \mathrm{Ht}} \mathbf{r}_{j} e^{-\frac{i}{\hbar} \mathrm{Ht}}$$

$$\mathbf{p}_{j}(t) = e^{\frac{i}{\hbar} \mathrm{Ht}} \mathbf{p}_{j} e^{-\frac{i}{\hbar} \mathrm{Ht}}$$

$$(6)$$

where j = 1, 2 is particle label. These expressions can be viewed either as quantum mechanical time-dependent operators in the Heisenberg picture or as particle trajectories in the  $\hbar \rightarrow 0$  classical limit. In the latter case one should replace quantum commutators with classical Poisson brackets.

By its usual (non-covariant) definition, the force acting on the particle 2 is given by the time derivative of this particle's momentum

$$\mathbf{f}_{2}(t) \equiv \frac{d}{dt}\mathbf{p}_{2}(t) = -\frac{i}{\hbar} \left[\mathbf{p}_{2}(t), \mathbf{H}\right]$$

This is a function that depends on positions and momenta of both particles at the same time instant t

$$\mathbf{f}_2(t) = \mathbf{f}_2(\mathbf{r}_1(t), \mathbf{p}_1(t); \mathbf{r}_2(t), \mathbf{p}_2(t))$$
(7)

This demonstrates that interaction propagates instantaneously in the reference frame O at rest.<sup>6</sup>

#### 4. Causality

Now consider the above two-particle system from the point of view of the moving reference frame O'. Particle trajectories in this frame are<sup>7</sup>

$$\mathbf{r}_{j}(\theta, t') = e^{-\frac{ic}{\hbar} \mathbf{K}_{\mathbf{y}} \theta} e^{\frac{i}{\hbar} \mathbf{H} t'} \mathbf{r}_{j} e^{-\frac{i}{\hbar} \mathbf{H} t'} e^{\frac{ic}{\hbar} \mathbf{K}_{\mathbf{y}} \theta}$$

$$\mathbf{p}_{j}(\theta, t') = e^{-\frac{ic}{\hbar} \mathbf{K}_{\mathbf{y}} \theta} e^{\frac{i}{\hbar} \mathbf{H} t'} \mathbf{p}_{j} e^{-\frac{i}{\hbar} \mathbf{H} t'} e^{\frac{ic}{\hbar} \mathbf{K}_{\mathbf{y}} \theta}$$

$$\tag{8}$$

The Hamiltonian in the reference frame O' is  $H(\theta) = \exp\left(-\frac{ic}{\hbar}K_y\theta\right)H\exp\left(\frac{ic}{\hbar}K_y\theta\right)$ . Therefore, the force acting on the particle 2

 $^{5}$  For example, we can assume that charge 1 represents an electron in the bunch and charge 2 is a part of the electric field sensor. Of course, replacing Pizzella's experimental setup by a couple of charges requires a significant stretch of imagination, but we believe that this model captures essential features of the involved interaction.

<sup>7</sup> Here t' is time measured by the clock of the observer O'.

<sup>&</sup>lt;sup>6</sup> Indeed, in our pure 2-particle system there is no place for fields or virtual particles that could serve as "interaction carriers" and store momentum and energy travelling from one charge to the other. Thus momentum-energy lost by one charge should be immediately picked up by the other, so there can be no retardation in our model.

$$\begin{aligned} \mathbf{f}_{2}'(t') &\equiv \frac{d}{dt'}\mathbf{p}_{2}(\theta, t') = -\frac{i}{\hbar} \left[ \mathbf{p}_{2}(\theta, t'), \mathbf{H}(\theta) \right] \\ &= -\frac{i}{\hbar} \left[ e^{-\frac{ic}{\hbar}\mathbf{K}_{y}\theta} e^{\frac{i}{\hbar}\mathbf{H}t'} \mathbf{p}_{2}e^{-\frac{i}{\hbar}\mathbf{H}t'} e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta}, e^{-\frac{ic}{\hbar}\mathbf{K}_{y}c\theta} \mathbf{H}e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \right] \\ &= -\frac{i}{\hbar} e^{-\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \left[ e^{\frac{i}{\hbar}\mathbf{H}t'} \mathbf{p}_{2}e^{-\frac{i}{\hbar}\mathbf{H}t'}, \mathbf{H} \right] e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \\ &= -\frac{i}{\hbar} e^{-\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \left[ \mathbf{p}_{2}(0,t'), \mathbf{H} \right] e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \\ &= e^{-\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \mathbf{f}_{2}(0,t') e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \\ &= e^{-\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \mathbf{f}_{2}\left(\mathbf{r}_{1}(0,t'), \mathbf{p}_{1}(0,t'); \mathbf{r}_{2}(0,t'), \mathbf{p}_{2}(0,t')\right) e^{\frac{ic}{\hbar}\mathbf{K}_{y}\theta} \\ &= \mathbf{f}_{2}(\mathbf{r}_{1}(\theta,t'), \mathbf{p}_{1}(\theta,t'); \mathbf{r}_{2}(\theta,t'), \mathbf{p}_{2}(\theta,t')) \end{aligned}$$

is a function of positions and momenta of both particles at the same time instant t'. Thus, from the point of view of the moving observer O', the interaction propagates instantaneously, exactly as for the observer at rest O. Moreover, in agreement with the principle of relativity, the force function  $\mathbf{f}_2$  in (9) has the same form as in the rest frame (7).

In regard to the Frascati experiment, the above derivation means that clicks of the sensors (events B and C) in the frame O' must occur exactly at the time of the bunch's exit from the pipe (event A). This prediction of the Wigner – Dirac theory is shown in the sequence of snapshots 2  $(g) \rightarrow (h) \rightarrow (i)$ . In other words, in this theory the three events A, B, C remain simultaneous in all frames, the "effects" B and C never occur before the "cause" A, and instantaneous potentials do not violate the principle of causality.

#### 5. Discussion

The above discussion implies that in the presence of interaction  $(V \neq 0, \mathbb{Z} \neq 0)$ , particle trajectories in the moving frame (8) cannot be obtained from rest-frame trajectories (6) by applying Lorentz formulas (2) - (5). One can say that interacting Wigner – Dirac theory does not have "invariant worldlines" [15, 16]. This idea is highly controversial, and many theoreticians believe that the invariant worldline condition must be respected in all dynamical theories. Based on this belief, a multitude of approaches were formulated [17, 18, 19, 20, 21, 22, 23, 24, 25], which deviated from the relativistic Hamiltonian dynamics of Wigner and Dirac. So far, the predictive power of these approaches remains rather limited.

Another idea is that particle equations of motion (including boost transformations) should be extracted from our most successful theory – quantum electrodynamics (QED). At the first sight, it seems that Maxwell's equations, as well as Liénard–Wiechert retarded potentials, must follow from the QED field Lagrangian in the classical limit. However, this conclusion is not so obvious, because time evolution is an ill-defined concept in the theory formulated in terms of fictitious bare particles. Moreover, the Hamiltonian of QED contains divergent renormalization counterterms. These interpretational difficulties are conducive to opinions that observables (positions and momenta) of interacting particles have no meaning in QED [26] or even that "there are no particles, there are only fields" [27]. For more works on the same theme see [28, 29, 30, 31].

A somewhat different and more pragmatic attitude is taken in research programs that try to replace the field-based language of quantum field theory with ideas of physical particles interacting through effective relativistic potentials. One way to obtain such potentials is to fit them to the known and experimentally verified S-matrix of the renormalized QED. This can be done not only in the lowest second perturbation order, resulting in the classic Coulomb–Darwin– Breit potential [26, 32], but also taking into account radiative corrections [33, 34, 35, 36]. Another

way forward is to apply a unitary dressing transformation [37, 38, 39] to the QED Hamiltonian. This method has the added advantage that it explicitly preserves the relativistic invariance of the theory [40].

The resulting effective electromagnetic interactions between dressed charges separate into radiation and bound types [39]. As expected, the radiation force field (like radio signals) is transmitted by real photons and propagates with the speed of light [41, 42, 43]. However, this is not true for the bound (Coulomb and magnetic) potentials. Even in high perturbation orders they are expressed by functions that depend on instantaneous positions and momenta of the charges. These potentials are well suited to describe most experimental observations in classical electrodynamics [39], including the electron beam's field dynamics observed at Frascati. Moreover, these potentials are in full agreement with the principle of causality.

#### Acknowledgments

The author is thankful to Rainer Grobe, Guido Pizzella, and Charles Su for illuminating discussions.

#### References

- de Sangro R, Finocchiaro G, Patteri P, Piccolo M and Pizzella G 2015 Measuring propagation speed of Coulomb fields *Eur. Phys. J.* C 75 137
- [2] Jackson J D 1999 Classical Electrodynamics (New York: Wiley)
- [3] Chubykalo A E and Vlaev S J Necessity of simultaneous co-existence of instantaneous and retarded interactions in classical electrodynamics 1999 Int. J. Mod. Phys. A 14 3789
- [4] Kholmetskii A L 2006 Momentum-energy of the non-radiating electromagnetic field: open problems? Phys. Scr. 73 620
- [5] Field J H 2006 Classical electromagnetism as a consequence of Coulomb's law, special relativity and Hamilton's principle and its relationship to quantum electrodynamics Phys. Scr. 74 702
- [6] Giakos G C and Ishii T K 1991 Anomalous microwave propagation in open space Microw. Opt. Techn. Let. 4 79
- [7] Ranfagni A, Fabeni P, Pazzi G P and Mugnai D 1993 Anomalous pulse delay in microwave propagation: A plausible connection to the tunneling time *Phys. Rev.* E **48** 1453
- [8] Kholmetskii A L , Missevitch O V, Smirnov-Rueda R, Tzonchev R I, Chubykalo A E and Moreno I 2007 Experimental test on the applicability of the standard retardation condition to bound magnetic fields J. Appl. Phys. 101 023532
- [9] Shabad A 2016 A different interpretation of "Measuring propagation speed of Coulomb fields" by R. de Sangro, G. Finocchiaro, P. Patteri, M. Piccolo, G. Pizzella *Preprint* arXiv:1606.00710v1
- [10] de Sangro R, Finocchiaro G, Patteri P, Piccolo M and Pizzella G 2016 Why the interpretation of "Measuring propagation speed of Coulomb fields" stands *Preprint* arXiv:1611.06935v1
- [11] Bakamjian B and Thomas L H 1953 Relativistic particle dynamics. II Phys. Rev. 92 1300
- [12] Wigner E P 1939 On unitary representations of the inhomogeneous Lorentz group Ann. Math. 40 149
- [13] Dirac P A M 1949 Forms of relativistic dynamics *Rev. Mod. Phys.* **21** 392
- [14] Weinberg S 1995 The Quantum Theory of Fields vol. 1 (Cambridge: Cambridge University Press)
- [15] Currie D G, Jordan T F and Sudarshan E C G 1963 Relativistic invariance and Hamiltonian theories of interacting particles Rev. Mod. Phys. 35 350
- [16] Stefanovich E V 2002 Is Minkowski space-time compatible with quantum mechanics? Found. Phys. **32** 673
- [17] Van Dam H and Wigner E P 1965 Classical relativistic mechanics of interacting point particles *Phys. Rev.* B 138 1576
- [18] Van Dam H and Wigner E P 1966 Instantaneous and asymptotic conservation laws for classical relativistic mechanics of interacting point particles *Phys. Rev.* 142 838
- [19] Currie G 1966 Poincaré-invariant equations of motion for classical particles Phys. Rev. 142 817
- [20] Hill R N 1967 Instantaneous action-at-a-distance in classical relativistic mechanics J. Math. Phys. 8 201
- $[21]\,$  Komar A 1978 Interacting relativistic particles Phys. Rev. D  $\,18\,$  1887
- $[22]\,$  Crater H W and Alstine P V 1983 Two-body Dirac equations Ann. Phys.  ${\bf 148}\,$  57
- [23] Sudarshan E C G and Mukunda N 1983 Forms of relativistic dynamics and world line condition and separability Found. Phys. 13 385
- [24] Polyzou W N 1985 Manifestly covariant, Poincaré invariant quantum theories of directly interacting particles Phys. Rev. D 32 995

- [25] Sokolov S N 1997 Mechanics with retarded interactions Preprint IHEP Protvino IHEP 97-84 http://web.ihep.su/library/pubs/prep1997/ps/97-84.pdf
- [26] Berestetskii V B, Livshitz E M and Pitaevskii L P 1982 Quantum Electrodynamics (Oxford: Butterworth-Heinemann)
- [27] Hobson A 2013 There are no particles, there are only fields Am. J. Phys. 81 211
- [28] Malament D B 1996 In defence of dogma: Why there cannot be a relativistic quantum mechanics of (localizable) particles *Perspectives on Quantum Reality* ed R Clifton (Dordrecht: Springer) p 1
- [29] Wilczek F 1999 Quantum field theory Rev. Mod. Phys. 71 S58
- [30] Halvorson H and Clifton R 2002 No place for particles in relativistic quantum theories? Phil. Sci. 69 1
- [31] Strocchi F 2004 Relativistic quantum mechanics and field theory Found. Phys. 34 501
- [32] Itoh T 1965 Derivation of nonrelativistic Hamiltonian for electrons from quantum electrodynamics Rev. Mod. Phys. 37 159
- [33] Gupta S N and Radford S F 1980 Quantum field-theoretical electromagnetic and gravitational two-particle potentials Phys. Rev. D 21 2213
- [34] Feinberg G and Sucher J 1988 Two-photon-exchange force between charged systems: Spinless particles Phys. Rev. D 38 3763
- [35] Pineda A and Soto J 1998 The Lamb shift in dimensional regularization Phys. Lett. B 420 391
- [36] Holstein B R 2004 Effective interactions and the hydrogen atom Am. J. Phys. 72 333
- [37] Shebeko A V and Shirokov M I 2001 Unitary transformations in quantum field theory and bound states Phys. Part. Nucl. 32 15
- [38] Stefanovich E V 2001 Quantum field theory without infinities Ann. Phys. 292 139
- [39] Stefanovich E 2015 Relativistic Quantum Theory of Particles vol. 2 (Saarbrücken: Lambert Academic)
- [40] Shebeko A V and Shirokov M I 1998 Relativistic quantum field theory (RQFT) treatment of few-body systems Nucl. Phys. A 631 564c
- [41] Shirokov M I 1978 Signal velocity in quantum electrodynamics Sov. Phys. Usp. 21 345
- [42] Kaup D J and Rupasov V I 1996 Exactly solvable one-dimensional model of resonance energy transfer J. Phys. A: Math. Gen. 29 2149
- [43] Kaup D J and Rupasov V I 1996 Exactly solvable 3D model of resonance energy transfer J. Phys. A: Math. Gen. 29 6911