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To cite this article: Sylvain Fasel *et al* 2004 *New J. Phys.* **6** 163

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High-quality asynchronous heralded single-photon source at telecom wavelength

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New Journal of Physics **6** (2004) 163

Received 3 September 2004

Published 12 November 2004

Online at <http://www.njp.org/>

doi:10.1088/1367-2630/6/1/163

Abstract. We report on the experimental realization and characterization of an asynchronous heralded single-photon source based on spontaneous parametric down-conversion. Photons at 1550 nm are heralded as being inside a single-mode fibre with more than 60% probability, and the multi-photon emission probability is reduced by a factor of up to more than 500 compared to Poissonian light sources. These figures of merit, together with the choice of telecom wavelength for the heralded photons, are compatible with practical applications needing very efficient and robust single-photon sources.

With the present development of quantum communication and computing technologies, including quantum key distribution [1] and quantum teleportation [2], the interest for true single-photon sources is rising. Many different implementations have been investigated, using single molecule or atom excitation [3]–[6], colour centres in diamond [7, 8], quantum dots [9]–[13] and pulsed or continuous-wave parametric down-conversion sources [14, 15]. All these solutions have various advantages and tradeoffs between high purity and efficient single-photon production, repetition rate, wavelength of the photons and ease of use. The aim of this paper is to show that a spontaneous parametric down-conversion (SPDC) source made of a bulk non-linear crystal at room temperature and a simple basic optical setup can be used to herald single photons at telecom wavelength in a very efficient way (see figure 1). The photons are also directly available in a standard single-mode telecom optical fibre, making this source a good choice for quantum communication applications such as scalable quantum networks. In this context, the

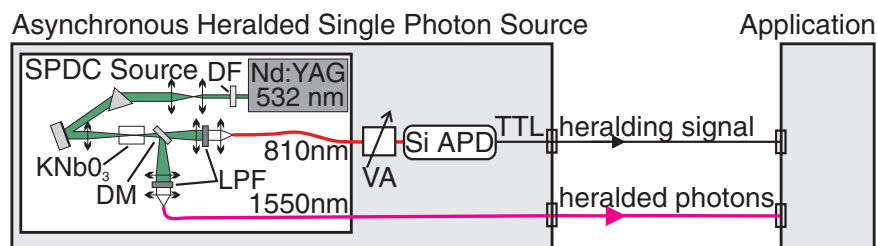


Figure 1. Schematic of the asynchronous heralded single-photon source (DM, dichroic mirror; DF, neutral density filter for pump attenuation; LPF, low-pass pump filters; VA, variable optical fibre attenuator).

term ‘heralded’ means that photons are not generated on demand, but instead electric signals announce the presence of photons in a fibre. Indeed, as photons are created in pairs, the detection of one photon can be used to announce the presence of the complementary photon [16].

The source presented in this paper is an asynchronous heralded single-photon source (AHSPS) because the heralding signals are not synchronized with a periodic clock, the SPDC pump being continuous. It exhibits a very good probability of producing one photon and a very low probability of producing more than one photon per heralding signal. The latter probability depends on the pump power applied to the crystal, and several measurements are presented to characterize this dependence.

Our AHSPS is made of two main parts, as depicted in figure 1. The first consists of the SPDC photon pair creation stage which is made of a 10-mm-long type I KNbO₃ bulk non-linear crystal pumped with a 532 nm continuous-wave laser (with maximum power of about 60 mW). On the one hand, we require our source to produce single photons for long-range telecom applications, and on the other we need the complementary photons to be passively and efficiently detected for heralding purpose. The phase-matching condition is therefore chosen to produce 1550–810 nm photon pairs, with the photons at 1550 nm featuring a 6.9 nm spectral width. A dichroic mirror is used to separate the 810 nm photons from the 1550 nm photons into two distinct beams, enabling one to couple these two wavelengths using separated optimized optics into single-mode fibres. More details about the core of this source can be found in [17, 18]. The 1550 nm single-mode fibre is the heralded single photons output port.

The second part of the AHSPS is made of an actively quenched silicon avalanche photodiode (APD) (EG&G) connected to the 810 nm single-mode fibre. The TTL detection signal from the silicon counter is the asynchronous heralding electric signal. For characterization, the optical variable attenuator in front of the silicon APD can be used to reduce the heralding signal rate without changing the heralded photons statistics. For the experiment, the pump power is varied by inserting neutral density filters in the path of the pump laser beam.

The heralded photon output port is connected to a test bench consisting of a gated detection Hanbury-Brown & Twiss type setup [19]. In order to characterize the source, the relevant parameters $P(1)$, $P(2)$ and $g^{(2)}(0)$ have indeed to be measured. $P(1)$ is the probability of having exactly 1 photon (and $P(2)$ the probability of having more than 1 photon) in the photon output port per heralding signal and during a time corresponding to the detection gate width. Note that the Hanbury-Brown & Twiss setup does not enable to discriminate between 2 and more photons events. By convention, we thus have $P(0) + P(1) + P(2) = 1$, where $P(0)$ is the probability of having no photon at all per heralding signal. Finally, $g^{(2)}(0)$ is the standard second-order autocorrelation function at time 0 [20].

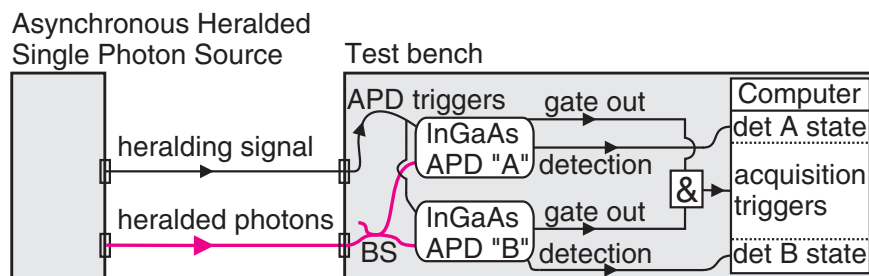


Figure 2. Schematic diagram of the test bench. The beam splitter (BS) is considered as having a perfect 50/50 separation ratio and the fibres from it to the detectors are considered as lossless. This is possible because detectors efficiency are calibrated including losses in the beam splitter and in the fibres (see text).

The setup is made of a 50/50 fibre optical beam splitter and two InGaAs APDs operated in gated mode (idQuantique). Both of these detectors are triggered with the heralding signal of the source through a TTL fan-out. The effective gate width is about 2.5 ns and is chosen with respect to the jitter of the Si APD, which is about 1 ns. A narrower gate width would not allow to detect all the heralded photons and would thus bias down the measured value for $P(1)$ and $P(2)$. The measured dark count probability per gate is $p_A^{\text{dc}} = 35.1 \pm 0.7 \times 10^{-6}$ for detector A and $p_B^{\text{dc}} = 7.4 \pm 0.3 \times 10^{-6}$ for detector B. The dark counts of the AHSPS silicon detector (about 100 Hz) artificially increase the probability of having no photons in the output port, but this effect is measured to be negligible in the present case. The detection states of both detectors are acquired using a computer by means of a digital input pc card (PCI-6533 DIO-32HS, National Instrument) and a labview software (see figure 2).

The triggering rate of the APDs is kept under 50 kHz using the optical variable attenuator of the source. Note that this does not affect the quality of the source, but has to do with the test bench we use. Indeed, this low triggering rate and a $10 \mu\text{s}$ external deadtime are used on both the InGaAs APDs to work in a regime where after-pulse counts are negligible. Because of these deadtimes, the heralding signal of the source cannot be directly used to trigger the APDs state acquisition, but one must discard the cases where one or both detectors are disabled when a new trigger arrives. If not, an artificially lowered coincidence detection rate would be measured, and the quality of the source would be overestimated. This is done by using a signal named ‘gate out’ in figure 2 which is synchronized with the effective application of bias voltage gate on a given APD, meaning that it is ready to detect heralded photons. These signals are combined with a logic AND gate to form the acquisition triggering signal. Upon reception of a trigger signal, the detection states (0 or 1) of the two APDs are acquired independently. The raw output is a binary file containing the detection state for each heralding signal effectively taken into account.

Using attenuated laser pulses, the efficiencies of both detectors under these particular working conditions are calibrated including the losses in the beam splitter and in the fibres connecting the APDs. It is thus possible to consider that the beam splitter is a perfect 50/50 separator and that the fibres are lossless. The overall detection efficiencies are measured to be $\beta_A = 8.4 \pm 0.1\%$ for detector A and $\beta_B = 9.6 \pm 0.1\%$ for detector B.

For the present set-up, one can show that the $g^{(2)}(0)$ parameter is equal to

$$g^{(2)}(0) \equiv \frac{P_{AB}}{P_A P_B} \cong \frac{2P(2)}{P(1)^2}, \quad (1)$$

Table 1. Experimental AHSPS parameters obtained with a detection gate width of 2.5 ns.

P_p (mW)	R_H (kHz)	$N_t (\times 10^7)$	T (min)	$N_A (\times 10^5)$	N_{AB}	$P(1)$	$P(2) (\times 10^{-4})$	$g^{(2)}(0) (\times 10^{-3})$
49	845	6.0	20	16	1062	0.59	41 ± 1	22.6 ± 0.5
25	403	2.8	20	7.7	255	0.61	19 ± 1	10.2 ± 0.5
13	221	1.6	20	4.1	82	0.61	10 ± 1	5.3 ± 0.5
3.3	120	1.7	12	4.6	78	0.60	8.0 ± 0.9	4.4 ± 0.5
1.6	39	1.6	40	4.2	35	0.61	2.5 ± 0.6	1.4 ± 0.3
0.9	18	1.8	85	4.4	46	0.58	3.7 ± 0.6	2.2 ± 0.4

where p_{AB} is the experimental probability of having simultaneous detections in both detectors and p_A, p_B the probabilities of having a single detection in the given detector A or B . Note that, as expected, this quantity does not depend explicitly on the detection efficiency. Refer to the appendix for details on the rightmost part of equality (1) and for details on obtaining $P(1)$ and $P(2)$ from the experimental data. p_A and p_B are obtained from the raw binary files by counting the number of registered detections for the given detector (N_A, N_B) divided by the total number of acquisition triggers (N_t). p_{AB} is obtained by counting how many times both detectors have simultaneously registered detections (N_{AB}) divided by the total number of acquisition triggers.

For the measurement, the SPDC source is first aligned without neutral density pump filters by optimizing the collection of the 810 nm photons. A second alignment is done by maximizing the ratio of detections at 1550 nm over detections at 810 nm through the adjustment of both 1550 and 810 nm photon collection. Even if the two separated collection optics are optimized for each wavelength, the spatial correlations of the 810 and 1550 nm photons cannot be perfectly matched. Therefore, the highest ratio is usually found when the 810 nm detection rate is about 90% of the maximal rate. Different neutral density pump filters are introduced one after the other in the path of the pump beam. For each filter, the pump power is measured just before the crystal, and the heralding signal rate R_H is recorded. When necessary, the variable attenuator is set to a non-zero value to keep this rate under 50 kHz for the acquisition. The results are summarized in table 1. In this table, P_p is the pump power and T is the experimental duration of the acquisition. $P(1)$, $P(2)$ and $g^{(2)}(0)$ are net (dark count subtracted values) calculated from formulas developed in the appendix. These values are obtained from the averages of the slightly different results calculated using N_A and N_B . As simultaneous detections are quite rare events, N_{AB} is small. The statistical error on this quantity is the main source of error for $P(2)$ and $g^{(2)}(0)$. It can be relatively high but it is kept under an acceptable level by acquiring for relatively long times. The error on $P(1)$ is negligible, because N_A (and N_B) is large. The slight changes for $P(1)$ values (less than 2% around the average value of 0.6) are explained by the fact that the neutral density pump filters slightly deviate the pump beam. This causes a change in the phase-matching condition and consequently a decrease in the coupling ratio from its nominal value. Moreover, as $P(1) \gg P(2)$, $P(1)$ is, to a very good approximation, the heralded photons coupling ratio, which is sometimes called the heralding efficiency H [14].

These results should be compared to a Poissonian light source featuring the same value for $P(1)$. The main observation is that the multi-photon emission probability $P(2)$ of our source is reduced by a factor $1/g^{(2)}(0)$ ranging from about 50 to more than 500, depending on the pump power. To the best of our knowledge, these are the highest factors reported so far. In fact, $g^{(2)}(0)$

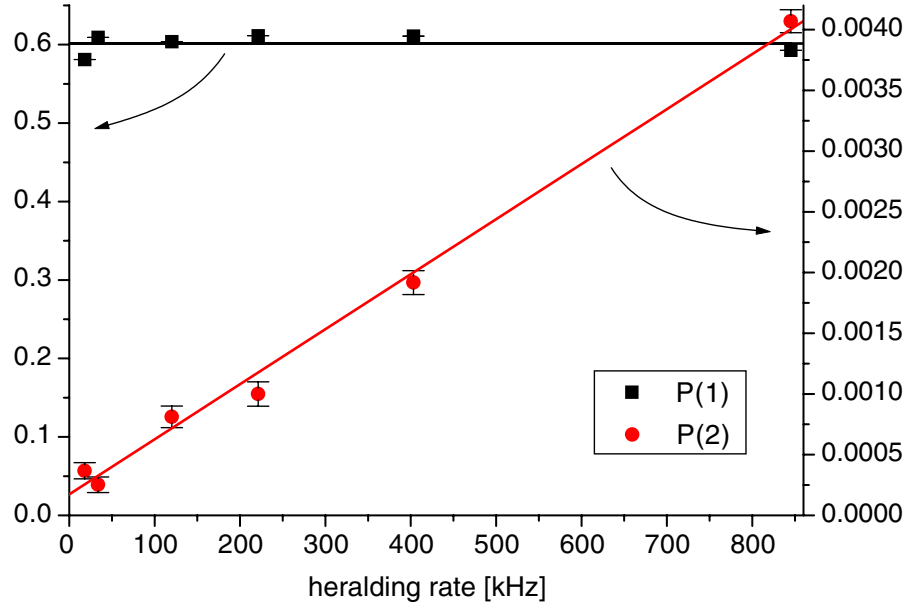


Figure 3. $P(1)$ (left scale) and $P(2)$ (right scale) displayed as function of the heralding rate. The solid lines are: average for $P(1)$ and linear fit for $P(2)$. As expected, $P(2)$ is linearly dependent on heralding rate (and hence on the pump power), while $P(1)$ remains constant.

and $P(2)$ can be arbitrarily low for low pump powers, i.e. heralding rates, as $P(2)$ is linearly dependent on the heralding rate (see figure 3). Moreover, $P(2)$ can be reduced by artificially lowering $P(1)$, i.e. by misaligning the heralded photons coupling. A better figure of merit is therefore the ratio of the heralded photons rate over $g^{(2)}(0)$:

$$F = \frac{P(1)R_H}{g^{(2)}(0)} = \frac{P(1)^3 R_H}{2P(2)}.$$

R_H and $P(2)$ are related to the physical parameters of the source as follows: R_H is the number of photon pairs created per second multiplied by the probability to detect the heralding photon. $P(2)$ is the probability to find two photon pairs in a time interval $\Delta\tau$ knowing that a trigger photon was detected, which is half of the probability that a photon pair is created during $\Delta\tau$, multiplied by the probability that two photons are coupled into the output fibre, i.e. $P(1)^2$. We find

$$R_H = q_H \eta_H \eta_S P_p, \quad P(2) = 0.5 P(1)^2 \Delta\tau \eta_S P_p,$$

where q_H is the coupling efficiency of the heralding photons, η_H the quantum efficiency of the heralding detector, η_S the pair creation efficiency of the SPDC crystal, and $\Delta\tau$ equivalent to the detection gate width of the heralded photons detection. We can now express F by

$$F = \frac{P(1)q_H\eta_H}{\Delta\tau}$$

which allows us to see which parameters should possibly be improved. We note that F does not depend on the efficiency of the SPDC crystal. Thus, using a more efficient pair generation,

e.g. by using waveguides in periodically poled crystals [15], would not impact on the quality of this single photons source. However, the source can be improved by (i) increasing $P(1)$ by using better optics, coatings or alignments [14], or using a different photon pair creation technique such as the Kerr effect inside optical fibres [21]; (ii) improving the coupling and detection efficiency of the heralding detector; (iii) reducing the timing jitter of the heralding detector which would allow to use much shorter detection gate width $\Delta\tau$ for the heralded photons.

We found it interesting to compare in a standard visual way the antibunching properties of the non-classical light coming from our source to other published results. Therefore, we devise a way to use the standard technique used in the case of synchronous single-photon source, even though our source is asynchronous. For synchronous single-photon sources, the standard way is to use detection signals coming from the Hanbury-Brown & Twiss setup as start and stop for a time to digital converter (TDC) device. Indeed, the time between successive possible creations and detections of photons is constant (fixed by a given clock signal), and such set-ups enable one to directly obtain histograms where bin n represents the probability of having two detections in different detectors, which happened at an interval of n triggers. For true single-photon sources, the central bin ($n = 0$) is of course zero while the other bins behave as for Poissonian sources. The deepness of this central dip allows one to have an intuitive information about the quality of the considered single-photon source.

For the present source, single photons are created at random times because of the continuous pumping and spontaneous non-linear process used. The elapsed time between a detection in one detector and the other is therefore completely random, and for this reason it is not possible to use a TDC. Instead, the number of triggers between detections in different detectors is computed directly from the raw binary data by a homemade software. Our reduction algorithm enables us to present standard histograms.

More precisely, the algorithm is the following: the program sequentially reads the raw data and registers in bins how many times a start and a stop were separated by n triggers (this number is called $M(n)$ in the following). As a convention, n is positive if the start was given by detector A and the stop by detector B , and negative in the opposite case. The bin $n = 0$ corresponds to the case for which two photons were detected simultaneously (i.e. for the same trigger). As for standard TDC, there could be some invalid start (another start for the same detector before a stop on the other) that will be ignored. Moreover, the search for a stop is done only within a limited range: if no stop is found before a certain number of triggers (we used 100) the search is cancelled and a new start has to be found in the subsequent data. All the processes leading to the histogram construction are summarized in figure 4. Note that this technique could be possibly applied to synchronous sources too.

The theoretical form for $M(n)$, when $n \neq 0$ is given by

$$M(n) = Cp_A(1 - p_B)^{|n|}p_B \quad (2)$$

for $n > 0$ and with p_A and p_B swapped for $n < 0$, where C is a normalization constant which depends on the total number of triggers, on the maximal n allowed and on p_A and p_B . Detections that do not occur simultaneously are indeed coming from different photon pairs and thus lead to independent detection events at detectors A and B . The probability $p(n)$ of having n triggers between a start and a stop is thus given by $p(n) = M(n)/C$. C is obtained by fitting the experimental results with the above formula for $n \neq 0$. Figure 5 shows a typical result for the whole histogram created by the algorithm described above, using 100 as range limit value.

	det A	det B	
	
no detection	0	0	$n = -1$
start at A	1	0	$n = 0$
no detection	0	0	$n = +1$
invalid start	1	0	$n = +2$
no detection	0	0	$n = +3$
stop at B	0	1	$n = +4$
	

Figure 4. Samples of raw data. Here, as an example, data reduction leads to a start and a stop separated by four triggers.

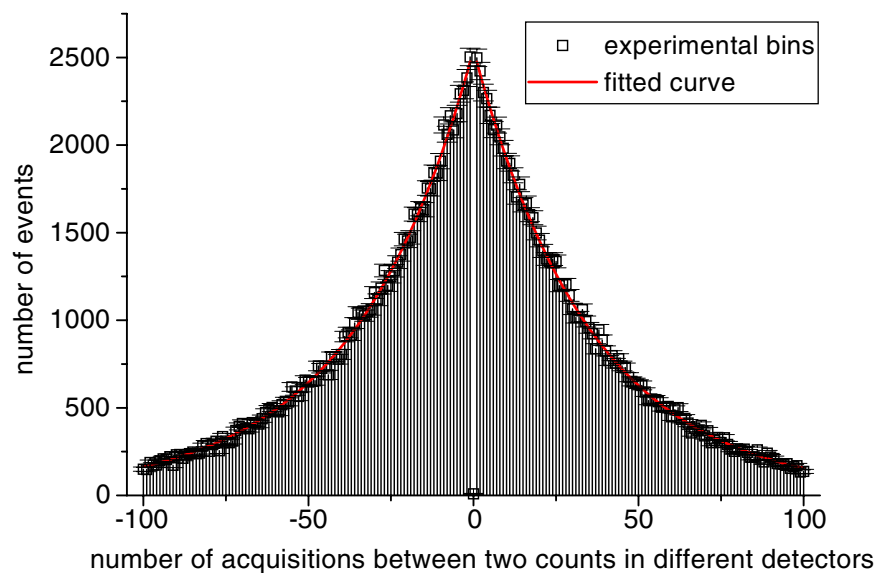


Figure 5. Typical resulting raw histogram displayed as points over the full range allowed by the algorithm. The plain curve is obtained by fitting the experimental values with formula (2) and varying C .

The central bin (corresponding to the measured value for $M(0)$) is nearly 0 indicating a very low $p(0) = M(0)/C \cong p_{AB}$. The data are in a very good agreement with formula (2) as shown by the fitted curve. The decreasing slope on both sides of the centre is related to the detection probabilities p_A and p_B . These values are quite high in our experiment compared to others. Indeed, recall that p_A and p_B describe not only the detection efficiencies but also the collection efficiencies which are rather high in our case. Consequently, the slope in figure 5 is quite steep and may look unfamiliar.

Another means of presenting these data is to restrict the display to a limited bin range around the centre, and to normalize the values in such a way that $g^{(2)}(0)$ is directly readable on the graph. This is done by dividing all experimental values by Cp_Ap_B . The height of the central bin corresponds then directly to $g^{(2)}(0)$ without dark counts subtraction (see the appendix for details on dark counts subtraction). Figure 6 shows this representation for the same data as in figure 5.

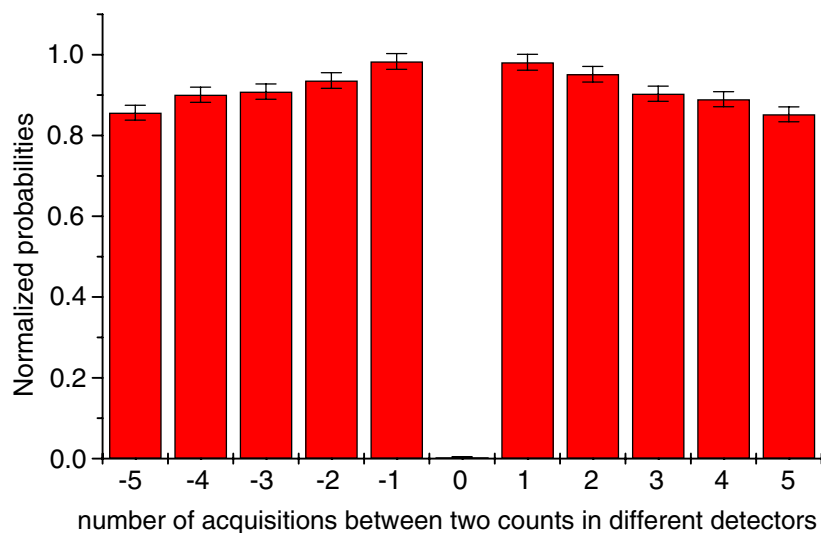


Figure 6. Typical resulting normalized histogram, restricted to small values around the centre. It is possible to infer the $g^{(2)}(0)$ values from the central bin. This histogram corresponds to acquisition made for 1.6 mW of pump. Note that the bins are made using raw values (dark counts are not subtracted) and that in this case $g^{(2)}(0) = 3 \times 10^{-3}$.

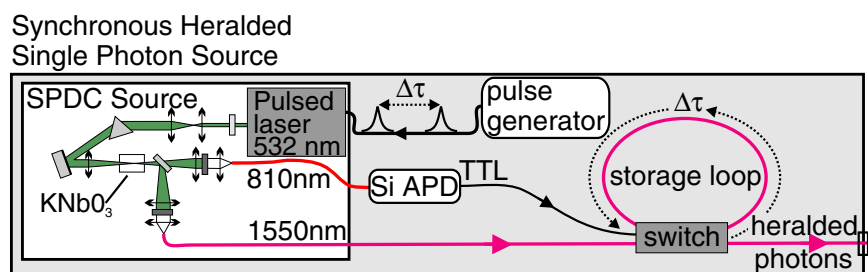


Figure 7. Schematic for using a SPDC source for high efficiency synchronous single photons production.

Note that it is in principle possible to turn our source into a synchronous one. A first step would be to use a pulsed laser to pump the non-linear crystal. A second step, following [22], would consist in a switched storage delay line (see figure 7). The latter would allow one to increase the probability of getting precisely one photon provided that the switch has a low enough insertion loss. The heralding signal is activated each time the storage loop is released (e.g. once every 10 pump pulse cycles), provided the Si-APD did register one photon.

We demonstrated that a simple and well-known SPDC set-up [17, 18] can be used to implement a very efficient high-quality single-photon source. The properties of our source for different pump powers have been investigated, showing that good tradeoffs between very low $g^{(2)}(0)$ and high enough repetition rate can be found, which are competitive with much more complex sources. Moreover, SPDC sources can be designed to produce photons at various wavelengths to match particular needs. Our source produces telecom wavelength single photons that are already in a standard single-mode telecom fibre. It is simple to operate and works at room

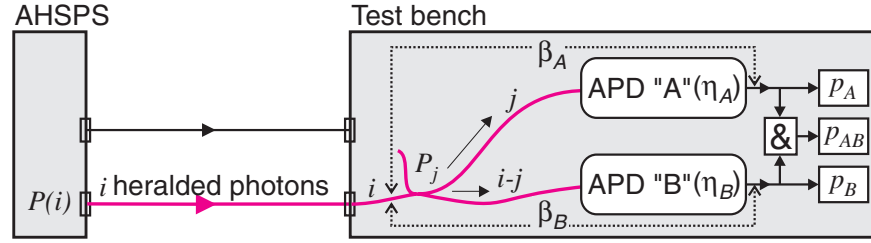


Figure A.1. Schematic of the quantities used for calculation of the source parameters.

temperature without stabilization. It is therefore a very good candidate for practical real-world telecom applications for which single photons are required.

Acknowledgments

Financial support by the Swiss NCCR Quantum Photonics is acknowledged.

Appendix

Let us elaborate on the way we obtain the relevant source parameters after subtraction of the dark counts for our set-up (see figure A.1).

The probability p^{count} for a single detector to register a count is given by

$$p^{\text{count}} = (1 - p^{\text{dc}})p^{\text{phot}} + p^{\text{dc}}(1 - p^{\text{phot}}) = p^{\text{phot}}(1 - 2p^{\text{dc}}) + p^{\text{dc}},$$

where p^{dc} is the probability for the detector to register a dark count in the absence of photons, with $p^{\text{phot}} = \sum_{j \geq 0} P_j(1 - (1 - \eta)^j)$ the probability of detecting photons. Here P_j ($\sum P_j = 1$) represents the photon numbers distribution directly at the input of the detector which features a quantum efficiency η . At the input of the test bench, the beam splitter randomly separates i incoming photons in the two arms. P_j is thus the binomial probability that, having i photons before the perfect beam splitter, j photons reach a given detector ($j \leq i$) i.e.

$$P_j = \binom{i}{j} \frac{1}{2^j} \frac{1}{2^{i-j}} = 2^{-i} \binom{i}{j}.$$

Using this P_j into the above formula for p^{phot} , and using $\sum_j \binom{i}{j} x^j = (1 + x)^i$, p^{phot} reduces to $p^{\text{phot}} = 1 - (1 - \eta/2)^i$. Therefore, whenever a heralding signal announces the presence of a multi-photon state (with probability of having i photons given by $P(i)$, $\sum P(i) = 1$) at the input of the beam splitter, p_A (the expression for p_B is similar) is expressed by

$$p_A = \sum_{i=0}^{\infty} P(i) \left\{ (1 - 2p_A^{\text{dc}}) \left(1 - \left(1 - \frac{\beta_A}{2} \right)^i \right) + p_A^{\text{dc}} \right\}. \quad (\text{A.1})$$

Here η is substituted by β_A , the overall efficiency detection including fibre losses and quantum efficiency.

In the same manner, the joint probability p_{AB} can be calculated to be

$$\begin{aligned}
 p_{AB} &= \sum_{i=0}^{\infty} P(i) \sum_{j=0}^i \binom{i}{j} \frac{1}{2^i} \{ [(1 - (1 - \beta_A)^j)(1 - 2p_A^{\text{dc}}) + p_A^{\text{dc}}] \\
 &\quad \times [(1 - (1 - \beta_B)^{(i-j)})(1 - 2p_B^{\text{dc}}) + p_B^{\text{dc}}] \} \\
 &= \sum_{i=0}^{\infty} P(i) \left\{ \left(1 - \left(1 - \frac{\beta_A}{2} \right)^i - \left(1 - \frac{\beta_B}{2} \right)^i + \left(1 - \frac{\beta_A + \beta_B}{2} \right)^i \right) (1 - 2p_A^{\text{dc}})(1 - 2p_B^{\text{dc}}) \right. \\
 &\quad \left. + \left(1 - \left(1 - \frac{\beta_A}{2} \right)^i \right) (1 - 2p_A^{\text{dc}})p_B^{\text{dc}} + \left(1 - \left(1 - \frac{\beta_B}{2} \right)^i \right) (1 - 2p_B^{\text{dc}})p_A^{\text{dc}} \right. \\
 &\quad \left. + p_A^{\text{dc}}p_B^{\text{dc}} \right\}. \tag{A.2a}
 \end{aligned}$$

$$\begin{aligned}
 &+ \left(1 - \left(1 - \frac{\beta_A}{2} \right)^i \right) (1 - 2p_A^{\text{dc}})p_B^{\text{dc}} + \left(1 - \left(1 - \frac{\beta_B}{2} \right)^i \right) (1 - 2p_B^{\text{dc}})p_A^{\text{dc}} \\
 &+ p_A^{\text{dc}}p_B^{\text{dc}} \Big\}. \tag{A.2b}
 \end{aligned}$$

$$\begin{aligned}
 &+ p_A^{\text{dc}}p_B^{\text{dc}} \Big\}. \tag{A.2c}
 \end{aligned}$$

The lines (A.2a) correspond to the cases for which at least one photon is detected simultaneously in each detector, and are consequently non-zero only for $i > 1$. The lines (A.2b) are the terms corresponding to the cases for which at least one photon is detected by one detector while the other one registers a dark count. These expression are therefore non-zero only for $i > 0$. The last line (A.2c) corresponds to the case for which both detectors register dark counts, and is of course independent of i .

Assuming $P(0) + P(1) + P(2) = 1$ in (A.1) and (A.2) (which is similar to neglecting terms for $i > 2$), and solving for $P(1)$ and $P(2)$ ($P(0) = 1 - P(1) - P(2)$), it is possible to get values for these quantities from a function of p_A^{m} , p_{AB}^{m} , $\beta_{A/B}$ and $p_{A/B}^{\text{dc}}$ (m distinguishes measured values for a parameters). $P(1)$ and $P(2)$ were also calculated from p_B^{m} and p_{AB}^{m} and the final published values are the averages. These values take directly into account the efficiencies and the dark counts and are thus as close as possible to the AHSPS parameters.

The net values for p_A , p_B and p_{AB} , denoted by net, are obtained from

$$p_A^{\text{net}} = p_A|_{p_A^{\text{dc}}=0}, \quad p_{AB}^{\text{net}} = p_{AB}|_{p_A^{\text{dc}}=p_B^{\text{dc}}=0}$$

by evaluating the right members of the equalities using the value for $P(1)$ and $P(2)$ calculated from p_A^{m} , p_{AB}^{m} , $\beta_{A/B}$ and $p_{A/B}^{\text{dc}}$ (or p_B^{m} instead of p_A^{m} for p_{AB}^{net}). These values are used to calculate the net $g^{(2)}(0)$ of table 1 using (1).

A simplified case with $P_2 \ll P_1$ and with $p_A^{\text{dc}} = p_B^{\text{dc}} = 0$ (no noise) and $\beta_A = \beta_B = \beta$ (these conditions correspond to a good approximation to our experimental results), leads to

$$p_A^{\text{m}} = p_B^{\text{m}} = P(1)\frac{\beta}{2}, \quad p_{AB}^{\text{m}} = P(2)\frac{\beta^2}{2}$$

and thus

$$P(1) = 2\frac{p_A^{\text{m}}}{\beta} = \frac{p_A^{\text{m}} + p_B^{\text{m}}}{\beta}, \quad P(2) = 2\frac{p_{AB}^{\text{m}}}{\beta^2}.$$

In this case we have

$$g^{(2)}(0) = \frac{p_{AB}^{\text{m}}}{p_A^{\text{m}}p_B^{\text{m}}} = \frac{p_{AB}^{\text{m}}}{(p_A^{\text{m}})^2} = 2\frac{P(2)}{P(1)^2}$$

and thus we obtain the well-known expression for $g^{(2)}(0)$, which enables one to compare the present source with a Poissonian source (as $g^{(2)}(0) = 1$ for such light sources).

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