# HeI VECTOR MAGNETOMETRY OF FIELD-ALIGNED SUPERPENUMBRAL FIBRILS

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### ABSTRACT

Atomic-level polarization and Zeeman effect diagnostics in the neutral helium triplet at 10830 Å in principle allow full vector magnetometry of fine-scaled chromospheric fibrils. We present high-resolution spectropolarimetric observations of superpenumbral fibrils in the HeI triplet with sufficient polarimetric sensitivity to infer their full magnetic field geometry. HeI observations from the Facility Infrared Spectropolarimeter are paired with high-resolution observations of the H $\alpha$  6563 Å and CaII 8542 Å spectral lines from the Interferometric Bidimensional Spectrometer from the Dunn Solar Telescope in New Mexico. Linear and circular polarization signatures in the HeI triplet are measured and described, as well as analyzed with the advanced inversion capability of the "Hanle and Zeeman Light" modeling code. Our analysis provides direct evidence for the often assumed field alignment of fibril structures. The projected angle of the fibrils and the inferred magnetic field geometry align within an error of  $\pm 10^\circ$ . We describe changes in the inclination angle of these features that reflect their connectivity with the photospheric magnetic field. Evidence for an accelerated flow (~40 m s<sup>-2</sup>) along an individual fibril anchored at its endpoints in the strong sunspot and weaker plage in part supports the magnetic siphon flow mechanism's role in the inverse Evershed effect. However, the connectivity of the outer endpoint of many of the fibrils cannot be established.

Key words: magnetic fields - Sun: atmosphere - Sun: chromosphere - Sun: infrared

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### 1. INTRODUCTION

Extending laterally away from magnetic field concentrations in the solar photosphere, threadlike fibrils observed in the chromosphere (e.g., Hale 1908; Veeder & Zirin 1970; Pietarila et al. 2009; Reardon et al. 2011) host a variety of dynamic behavior and have long been considered tracers of the difficult to measure chromospheric magnetic field (Smith 1968; Foukal 1971a, 1971b). Outside of sunspots, fibrils extend across internetwork cells and often, but not always, visibly suggest that their endpoints are rooted in areas of opposite polarity photospheric network flux. For this reason, fibrils are thought to be field-aligned closed magnetic loop segments. In the case of fibrils with endpoints not associated with opposite polarity network flux, Foukal (1971b) suggests that H $\alpha$  fibrils may extend over the neighboring flux and connect with regions of opposite polarity flux at a farther distance, and thus the fibrils being directed to higher heights disappear in H $\alpha$ . Contrarily, Reardon et al. (2011), using high-resolution Ca II 8542 Å narrowband images, argue that such internetwork fibrils are connected to the weak internetwork field directly below, meaning that fibrils do not contain much of the total flux of the concentrations from which they extend. The remaining flux would be directed upward into the corona, and have direct influence on dynamic heating mechanisms.

Similarly, fibrils and/or threads surrounding sunspots form what is known as the superpenumbra (Loughhead 1968). Again these fibrils are presumably magnetic loops rooted at one end in the sunspot and at the other in some opposite polarity plage. This concept is invoked by the siphon flow model to explain the apparent inward flow (i.e., the inverse Evershed effect) directed along the superpenumbral fibrils (Evershed 1909; Meyer &

<sup>4</sup> Graduate student researcher at the National Solar Observatory (NSO), operated by the Association of Universities for Research in Astronomy, Inc. (AURA), under cooperative agreement with the National Science Foundation. Schmidt 1968; Maltby 1975). Yet, characteristic shocks thought to be formed by siphon flows have not yet been definitively observed, although some evidence does exist (Uitenbroek et al. 2006; Bethge et al. 2012). Other short-lived phenomena are also witnessed in superpenumbral fibrils that are difficult to explain in terms of simple siphon flow (Vissers & Rouppe van der Voort 2012).

Until recently, our knowledge of the fine-scaled fibril magnetic field was limited to the morphological constraints placed on fine structure via comparison with photospheric field measurements. Wiegelmann et al. (2008) noted that nonlinear forcefree extrapolations of the photospheric magnetic field better account for the free-magnetic energy of the corona when the fibril direction is used as a constraint on the horizontal field direction; yet direct measurement are still lacking. Moreover, the photospheric field is a poor boundary condition since it is not strictly force-free. Lagg et al. (2009) studied two curvilinear internetwork structures observed with the He I triplet at 10830 Å and found evidence that the structures hosted a horizontal magnetic field, but the primary fibril axis was offset from the inferred magnetic field direction in one of the structures. In addition, Asensio Ramos et al. (2008, hereafter AR08) interpreted unresolved disk-center HeI internetwork spectra and found less inclined fields ( $\theta_B \approx 21^\circ$  or  $\theta_B \approx 47^\circ$  w.r.t. solar vertical). More recently, de la Cruz Rodríguez & Socas-Navarro (2011) studied the transverse Zeeman effect on the Ca II 8542 Å spectral line within superpenumbral fibrils near/above the external boundary of a photospheric penumbra and evidenced general consistency between the fibril axes and the inferred transverse magnetic field direction. However, they pointed out particular cases where the inferred field did not match the visible morphology. Furthermore, the CaII linear polarization decreased rapidly outward from the sunspot and was considered to be inconsistent with the presumed superpenumbral canopy.



**Figure 1.** NOAA active region 11408 observed by FIRS and IBIS on 2012 January 29. (a) SPECKLE reconstructed broadband images from IBIS at 20:05 UT, (b) IBIS H $\alpha$  intensity image at 6562.46 Å acquired at 20:05:16 UT, (c) IBIS Ca II intensity image at 8541.873 Å acquired at 20:04:53 UT, (d) FIRS map of the He I relative intensity (i.e.,  $I(\lambda)$  normalized to local continuum) at  $\lambda = 10829.995$  Å. The slit, oriented parallel to the solar meridian, was scanned from solar east to west at a rate of 0'.64 minute<sup>-1</sup>, (e) He I Doppler velocity corrected for orbital motions and solar rotation. Solar north is up and the *x*- and *y*-axes give helioprojective coordinates.

We address the magnetic field vector within resolved chromospheric fibrils using high-resolution observations of the He I infrared triplet. Although the utility of these three spectral lines has been long emphasized as indicators of solar and stellar activity (Zirin 1982; Kozlova & Somov 2003) and probes of the chromospheric magnetic field (Harvey & Hall 1971; Rüedi et al. 1995), only recently has the theoretical framework of its polarized spectral line formation (Trujillo Bueno & Asensio Ramos 2007; AR08) been met in maturity by instruments capable of measuring its weak polarization signals at spatial scales of interest (see, e.g., Collados et al. 2007; Jaeggli et al. 2010). Here, we discuss the polarization signatures of the HeI triplet observed within an active region (AR) superpenumbra observed with multi-channel instrumentation at the Dunn Solar Telescope (DST; Sections 2 and 3). A heuristic description of the mechanisms inducing He I polarization is given in Section 4 to explain the macroscopic structure seen in polarized maps of the AR. Section 5 outlines our methods used to model the visible fibril morphology as well as the inversion method used to infer the magnetic field vector from the polarized spectra. A summary and discussion of the results follow.

### 2. OBSERVATIONS AND DATA REDUCTION

On 2012 January 29, NOAA AR 11408 consisted of a simple alpha-type sunspot in a bipolar configuration with trailing plage. We targeted this region at the National Solar Observatory's (NSO) DST located on Sacramento Peak in New Mexico, USA. The observations included multi-channel, imaging and slit-type, spectroscopy and spectropolarimetry using the Interferometric Bidimensional Spectrometer (IBIS; Cavallini 2006; Reardon & Cavallini 2008) and the Facility Infrared Spectropolarimeter (FIRS; Jaeggli et al. 2010). An additional camera acquired broadband images within the 4300 Å molecular spectral G band. All instruments were operated simultaneously and benefited from the facility's High Order Adaptive Optics system (Rimmele et al. 2004) during a period of good to excellent seeing.

Our focus here is on a single map of NOAA AR 11408 acquired in the He I triplet with the FIRS dual-beam slit-spectropolarimeter when the AR was located at N8W35

 $(\mu = \cos \Theta = 0.8)$ . A single slit was oriented parallel to the solar north-south axis and scanned across the region from east to west with a projected step size and slit width of 0'.'3- the DST angular resolution is limited to 0''.36 at 10830 Å by the Rayleigh criterion. Seventy-seven arcseconds were imaged along the slit. A 200 step map commenced at 19:16 UT and required 94 minutes to complete. The common IBIS and FIRS field of view (FOV) is illustrated in Figure 1. This deep FIRS scan measured the full Stokes state of the incoming light with a four-state efficiency-balanced modulation scheme with 125 ms exposures. At each step position 15 consecutive modulation sequences were co-added for a total integration time of 7.5 s per slit position. The final spatial sampling after reduction (described below) is  $0''.3 \times 0''.3$ . Spectral sampling is 38.6803 mÅ pixel<sup>-1</sup> over a 35.74 Å spectral range. The mean noise level in the Stokes  $Q_{1}$ U, and V spectra is  $4.0 \times 10^{-4}$ ,  $3.7 \times 10^{-4}$ , and  $3.0 \times 10^{-4}$ , respectively, in units of continuum intensity.

In congress with FIRS, high-resolution full Stokes polarimetry was performed with IBIS, a dual Fabry–Perot interferometer, over a 45" × 95" FOV. Full Stokes measurements were acquired in the photospheric Fe I 6173 Å spectral line at  $N_{\lambda} = 16$  distributed wavelength points across the line and continuum, as well as in the chromospheric Ca II 8542 Å line ( $N_{\lambda} = 20$ ). In addition, we performed imaging spectroscopy of the H $\alpha$  6563 Å line ( $N_{\lambda} = 22$ ). Normal reduction methods were used (see, e.g., Judge et al. 2010), and included full polarimetric calibration, FOV-dependent spectral wavelength shift correction, and spatial destretching using SPECKLE reconstructed broadband images recorded simultaneously at 6360 Å (Wöger et al. 2008). The entire observation cycle of the three channels lasted 50 s and was repeated throughout all other observations.

To verify the observational geometry needed to specify the scattering angle of the He I observations, we coaligned all observations with continuum data from the Helioseismic and Magnetic Imager (HMI; Scherrer et al. 2012) on board NASA's *Solar Dynamics Observatory* (*SDO*). We also employ *SDO*/HMI magnetograms for potential field extrapolations in Section 6.3. The standard preparation routines available for *SDO*/HMI data, including *aia\_prep* v4.13, were utilized. All observations from the DST were coregistered and cor-

rected for differential atmospheric refraction. We estimate that the coregistration error is less than 0.5. The largest error in the observed geometry of the FIRS map is the 0.8 change in the heliographic observation angle introduced by solar rotation.

## 2.1. Reduction of FIRS Spectra

The reduction of the raw FIRS spectra differs in a number of ways from previous methods (Jaeggli et al. 2012). Detector properties were calibrated via dark and bias subtraction, spectral flat fields, and a nonlinearity correction, although these observations were careful to utilize only the most linear portion of the detector response curve. Flat fields consisted of averaging quiet-Sun observations taken at disk center just after the science observations. The spectral lines are removed in the spectral flats prior to their application on the science data with Voigt profiles fit to each line. Weak lines are not well removed in this process due to large pixel-to-pixel gain variations. Deep lines, such as the Si I line at 10827.089 Å, are well calibrated. Within the HeI triplet, the flat-fielding process is quite reliable due to the very weak absorption in the quiet Sun relative to strong signals in the AR which makes its removal in the raw flat field unnecessary.

#### 2.1.1. Polarization Calibration

Polarization sensitivity and accuracy are critical to our measurements. As each optical element of the telescope and instrument can modify the state of polarization, we carefully calibrate the polarimetric response of the entire optical system. Ignoring attenuation and the effects of the detector, the measurement process used by FIRS to derive the polarization state of the incoming solar light can be written as

$$\mathbf{I}_{\text{meas}} = \mathbf{O}\mathbf{X}\mathbf{T}\mathbf{S}_{\text{in}},\tag{1}$$

where  $I_{meas}$  is a vector of four measured intensities.  $S_{in}$  is the input Stokes vector, and T is the collective Mueller matrix of the telescopic optics and is time dependent due to configuration changes of the telescope throughout the observations. X is the time-independent Mueller matrix of all the instrumental optics following the set of calibration optics that are inserted near the prime telescope focus during calibration. X includes the effects of the adaptive optics system, beam splitters, and the FIRS instrument. O is the modulation matrix describing the polarimeter modulation scheme.

**T** is determined via the sub-aperture polarization calibration scheme described by Socas-Navarro et al. (2011). As in Beck et al. (2005) and Socas-Navarro et al. (2006), a linear polarizer and wave plate are introduced into the beam to determine **X**. To combat the effects of light-level variations, we fit for the 15 elements of the *normalized* **X** Mueller matrix as in Ichimoto et al. (2008). We also determine the unknown quantities of the calibration optics, namely, the retardance and offset angle of the wave plate, through a least-squares fit to an appropriate calibration optics model. The linear polarizer is kept in the beam throughout the calibration to decouple the telescope from the downstream optics as in Beck et al. (2005); however, unlike that work, we find that the parameters of the wave plate can be found directly from a model fit.

After demodulation and the correction for X and T, small offsets of the "unpolarized" continuum from zero polarization are used to fine-tune the intensity crosstalk calibration (Sanchez Almeida & Lites 1992). The two beams of FIRS are then combined to mitigate the effects of seeing-induced crosstalk. We

analyze the residual crosstalk with the correlation method of Schlichenmaier & Collados (2002) applied to the Si I line at 10827 Å. The crosstalk coefficients  $C_{VQ}$ ,  $C_{VU}$ ,  $C_{QV}$ , and  $C_{UV}$ yield small values of 0.0198, 0.076, -0.013, and -0.039, which are implemented as a correction. For the small polarization signals examined in this data (on order of 0.1%), the small residual crosstalk coefficients translate to a small polarization error (0.076 × 0.1% = 0.0076%), smaller than the mean noise level of ~0.03%. Finally, we correct for the time-dependent parallactic angle and rotate the Stokes reference direction such that the Stokes +*Q* direction is oriented parallel to the solar east/west direction.

#### 2.1.2. Polarized Fringe Removal

Our FIRS observations contain significant polarized fringes that cannot be completely decoupled or removed from the real solar signal by flat fielding and/or Fourier filtering. Casini et al. (2012) developed a pattern-recognition-based technique using two-dimensional principal component analysis (2DPCA) to address this problem, specifically using FIRS data. We apply these techniques to our data to each beam separately just prior to combination. A key difference here is that we use the spectral flat fields to determine the projection vectors necessary to "train" the 2DPCA algorithm. In doing so, we reconstruct via the proper selection of eigenfeatures the fringe pattern in the data frames instead of the solar signal itself. The reconstructed fringes are Fourier filtered using a two-dimensional Fourier analysis, and then detrended, meaning that at each sampled wavelength, the fringe signal is fit as a smooth function of spatial position across the map. The spatially detrended, Fourierfiltered, 2DPCA reconstructed fringes are subtracted from the original data frames to recover the true solar signal. This technique achieves a large increase in the sensitivity of the measurements, suppressing the fringe signal to at or below the photon noise.

#### 2.1.3. Wavelength and Velocity Calibration

Since we are interested in the absolute velocity structure along each fibril, we establish an absolute wavelength scale for these FIRS measurements. Our observations exhibit only weak telluric absorption on this date, which disallows the use of the method used by Kuckein et al. (2012) since the two telluric lines are influenced negatively by the flat-field errors discussed above. Our wavelength calibration relies instead on the cores of the two deep photospheric SiI lines at 10827.089 Å and 10843.845 Å. The separation of these two wavelengths, which have been corrected for convective blueshift and gravitational redshift by Borrero et al. (2003), is only 1.3 mÅ different than the separation we determine from the FTS spectral atlas (Kurucz et al. 1984). Thus, we argue that this separation can reliably be used to calculate the spectral dispersion. We find a linear dispersion of 38.6803 mÅ pixel<sup>-1</sup>, which is consistent with spectral dispersions calculated during other FIRS observing campaigns when the level of telluric absorption was high enough to allow for the Kuckein et al. (2012) method.

Since the convective blueshift of the Si I line at 10827.089 Å is negligible (Kuckein et al. 2012), we utilize its observed position for the absolute wavelength calibration. We assume that the line center position of the Si I observed at disk center during the flat fields is shifted by the various orbital motions described by Martinez Pillet et al. (1997) in addition to gravitational redshift. That is, the average disk-center Doppler velocity for the Si I line after the full velocity calibration is assumed to be zero. Applying this correction to our science data at a heliographic angle of  $\approx 36^{\circ}$ , we find the observed Doppler velocities in a patch of quiet Sun to be consistent within  $\pm 250 \text{ m s}^{-1}$  with the determined orbital and gravitational effects, which we take as the error of our Doppler velocities after full correction.

## 3. MULTI-WAVELENGTH COMPARISON OF CHROMOSPHERIC FIBRILS

A particular strength of these observations is the coordinated diagnostics of H $\alpha$  6563 Å, Ca II 8542 Å, and He I 10830 Å each at sufficient resolution to individuate multiple chromospheric fibrils. The spectral line formation of each of these lines constrains the thermodynamic structure of the fibrils. While the formation and dynamics of real solar fibrils is not understood, fibril-like thermodynamic structures are seen within advanced numerical radiative-MHD simulations. Forward radiative transfer (RT) calculations through these simulations are now being used to compare real observed structures with synthetic structures. However, the complex non-LTE (NLTE) formation of chromosphere lines remains a challenge. Fibril structures have not yet been produced in forward RT calculations of the Ca II 8542 Å line. However, recent three-dimensional (3D) NLTE RT calculations for the H $\alpha$  spectral line through a 3D radiative-MHD simulation including the convective zone and lower corona do produce fibril-like phenomena. These calculations propose that  $H\alpha$  fibrils denote field-aligned ridges of increased mass density at higher average formation heights than the background plasma (Leenaarts et al. 2012).

As seen in Figure 1, the fibrils extending outward from the sunspot are remarkably spatially coherent between each spectral line despite the FIRS map being significantly non-monochronic  $(t_{\text{scan}} = 94 \text{ minutes})$  compared to the relatively quick spectral scans ( $\delta t < 30$  s) of IBIS. The three center images of Figure 1 show the spectral intensity (or relative intensity) in the blue wing of each spectral line. The fibrils directly associated with the sunspot display the greatest correspondence between the spectral lines, whereas the very fine-scaled fibril features outside of the superpenumbra (near  $\langle X, Y \rangle = \langle 570, 235 \rangle$ ) are only resolved in the IBIS images. These fibrils are likely too thin and/or too dynamic to be seen in the lower-resolution FIRS maps. Individual fibril widths in the superpenumbra (especially at (560, 230) and (565, 210) are comparable for each line, suggesting again that these spectral lines probe plasma in the same structures and/or overall topology. While the temporal stability of the superpenumbral structure as a whole has been previously observed on timescales of hours (Loughhead 1968), individual lifetimes of the fibrils are only on the order of tens of minutes (Maltby 1975). It is, however, this stability that allows us to probe these fibrils with He I 1083 spectropolarimetry since FIRS requires long integration times to achieve the necessary sensitivity in the polarized spectra.

The velocity structure in the He I triplet (Figure 1(e)) displays the familiar inverse Evershed effect with line-of-sight (LOS) velocities up to ~8–9 km s<sup>-1</sup>, which is higher than velocities reported by Penn et al. (2002) from lower-resolution observations. The fibrils themselves exhibit the inverse Evershed effect as well as the inter-fibril material which still contains significant absorption in the He I triplet. Chromospheric umbral *p*-mode oscillations can be seen both in the velocity map and the quasi-monochromatic map of normalized intensity. Near the outer boundary of the superpenumbra, weak signs of oppositely directed flows, as one might expect from drainage of gas from

 Table 1

 He I Triplet Spectral Lines

Transition	Air Wavelength (Å)	$J_{ m lower}$	$J_{ m upper}$	
$2s^3S_1 - 2p^3P_0$	10829.0911	1	0	
$2s^3S_1 - 2p^3P_1$	10830.2501	1	1	
$2s^3S_1 - 2p^3P_2$	10830.3398	1	2	

fibrils, are apparent. However, we stress that this structure must be confirmed with spectral interpretation since this map results simply from locating the spectral position of greatest He I absorption and does not account for gradients along the LOS.

The absorption depth of the He I triplet primarily correlates with the He I number density and thickness of the absorbing regime, as well as with the degree of coronal illumination (Avrett et al. 1994). Photoionization of parahelium atoms and subsequent recombination is attributed to be the main driver for populating the orthohelium ground state (Centeno et al. 2008). While this study cannot constrain the relative degree of coronal illumination for each fibril, the visual correspondence of the He I absorption with the H $\alpha$  fibrils is at least consistent with fibrils being regions of increased mass density, as suggested by Leenaarts et al. (2012).

### 4. He I TRIPLET POLARIZATION SIGNATURES WITHIN THE SUPERPENUMBRAL REGION

Anisotropic radiative pumping (i.e., the quantum extension to classical scattering), the Hanle effect, and the Zeeman effect work together to induce and modify the polarization of the He I triplet. To describe and heuristically interpret the polarization signatures observed here, we summarize some key aspects of these mechanisms. (see AR08; Trujillo Bueno & Asensio Ramos 2007 and references therein for a more complete discussion)

The He<sub>1</sub> triplet consists of the three spectral lines (Table 1) formed between the  $2p^3P$  and the  $2s^3S$  terms of the He I atom. The two longer wavelength transitions form a blended "red" component at solar temperatures, whereas the 10829.0911 Å transition is referred to as the "blue" component. For each line, the Zeeman effect works as normal to split the degenerate energy transitions into  $\pi$  ( $\Delta M = 0$ ) and  $\sigma$  ( $\Delta M = \pm 1$ ) components, with their respective polarizations. Polarization is also induced (and modified via the Hanle effect) for each line by any "order" present in the magnetic substates of a given level participating in the transition. This "order," called atomic-level polarization, can be generated by "order" (i.e., anisotropy) in the incident radiation interacting with the atomic system. The decay of an excited level or absorption from a lower level harboring ordered substates *selectively* determines the polarization of the outgoing radiation. Note, however, that unlike the other levels of the He I triplet, the upper J-level (i.e., the total angular momentum) of the blue component is zero. This makes it "unpolarizable" in the sense that there are no magnetic substates for which imbalanced populations and/or coherences can be produced via anisotropic radiative pumping. Only *selective absorption* processes create net polarization in the blue transition, while *selective emission* and *selective absorption* contribute to both the total polarization of the red component. Multiterm calculations as in AR08 are necessary to determine the atomic-level polarization for each level since the "order" of a particular J-level can be transferred to other levels. In fact, this process, called *repopulation pumping*, is important in determining the polarization of the lower level of



**Figure 2.** Polarized maps of NOAA 11408 in the He t triplet at 10830 Å. The top figures give Stokes Q and U for the He t blue component while the bottom plots show the He t red component. Solar north is up and the reference direction for Stokes Q is solar east/west. The color table is saturated as the levels given in the color tables to show the polarization of the superpenumbral region. The horizontal streaks in the blue component maps arise from residual small-amplitude systematic measurement errors. The solid lines show the boundaries of the sunspot penumbra ( $r = r_{spot}$ ) and superpenumbra ( $r = 2.3r_{spot}$ ). The dashed lines correspond to  $r = 1.25r_{spot}$ .

the He I triplet. The short-lived excited states of the  $2p^3P$  term often map their "order" onto the metastable lower level.

Considering the distinctions between the blue and red He I components, we compare and describe linearly polarized maps of the observed region in each component (see Figure 2). To facilitate this description, we define a cylindrical geometry centered on the sunspot with a reference axis vertical in the solar atmosphere and a reference plane tangent to the solar surface. The reference direction of the polar axis points

toward the disk center in correspondence with the scattering event geometry defined in AR08. Thus, the ray lying in the reference plane pointing from the sunspot center toward the disk center defines where  $\theta_{spot}$  is equal to zero (see Figure 1). The center of the sunspot is defined via a fit of a circle to the *heliographic* coordinates of the external boundary of the photospheric penumbra on the north and east sides of the spot where the penumbra is most homogeneous in its radial extension. This circle defines the sunspot radius (i.e.,  $r_{spot}$ ). The superpenumbral fibrils extend mostly radially outward and have apparent endpoints within approximately 2.3 times the sunspot radius as shown in Figure 1. A second set of fibrils then extend in the same general direction from near this boundary (see Figure 1).

### 4.1. The Zeeman-effect-dominated Region

Within the sunspot radius, the Q and U polarized maps for the blue and red components of the HeI triplet display the familiar lobe structure that is commonly seen in such maps of sunspots within photospheric normal Zeeman triplets. The HeI component profiles in this region (not shown) exhibit a near symmetry about line center with the three nodes typical of the normal transverse Zeeman effect. In the photosphere, the four-lobe macroscopic structure found in Stokes Q and U maps centered on a nearly circular sunspot and viewed not too far from the disk center ( $\mu > 0.6$ ) is naturally explained by a simple model of a unipolar sunspot whose field diverges symmetrically as a function of height. The four lobes appear as a consequence of the change in the azimuthal angle of the transverse component of the magnetic field relative to the LOS (see, e.g., Schlichenmaier & Collados 2002). Such a model explains the global Q and U behavior exhibited within the sunspot radius by the HeI components in Figure 2. As these maps are produced in the line center of each component, they exhibit the polarization of the on-average unshifted  $\pi$ -component. Assuming that the radiation absorbed originates as the unpolarized photospheric continuum, the linear polarization of the  $\pi$ -component induced by the transverse Zeeman effect is aligned perpendicular to the transverse component of the magnetic field relative to the LOS. With the simple model sunspot in mind, one would expect Stokes Uto be near zero and Stokes Q to be negative along the observational reference direction for Stokes Q in a Zeemandominated region. This is consistent with the pattern shown inside the sunspot radius in Figure 2 as here the reference direction for Q is in the solar east/west direction (i.e., left/right in the figure). This region can be considered to be Zeeman-dominated, and consequently the magnetic field strengths are expected to be on the order of a kilogauss.

#### 4.2. Atomic-level Polarization in the Superpenumbral Region

Just beyond the external boundary of the sunspot penumbra (i.e.,  $r = r_{spot}$ ), the global pattern of the linear polarization markedly changes particularly in the red component. The sign of Q and U in the red component changes sign with respect to the lobe structure in the Zeeman-dominated region. This is a consequence of the atomic-level polarization beginning to dominate the polarization of the transverse Zeeman effect. To better illustrate this, we extract the observed profiles at a constant distance from sunspot center ( $r = 1.25r_{spot}$ ) and display them in Figure 3 stacked according to their angular position where  $\theta_{spot} = 0$  points toward disk center. For  $\theta_{spot}$ 



Figure 3. Angular variation of the He I Stokes profiles around the sunspot at a constant radius of 1.25 times the sunspot radius. The vertical dashed lines indicate the rest wavelengths of the three He I triplet transitions. Only weak traces of the transverse Zeeman effect are noticeable in the linearly polarized Q and U profiles. Rather, the mostly single-peaked, nearly Gaussian, characteristics of the Q and U profiles along with the opposite signed polarization in the blue and red components offer clear evidence for the prevalence of scattering polarization induced in the superpenumbra.

greater than 90° and less than 250°, Stokes Q and U show profiles clearly influenced by atomic-level polarization which can be distinguished despite the high level of noise in Stokes Q. The only traces of a Zeeman-induced  $\pi$ -component situated between  $\sigma$  components of opposite sign are recognizable in the He I red component for  $140^\circ > \theta_{spot} > 90^\circ$ . Furthermore, the red and blue components exhibit opposite signs indicating that selective absorption and emission processes are at work as discussed above. From an observer's point of view, the opposite signs of the two components gives a beneficial indication that the level of intensity crosstalk in Stokes Q and U is negligible.

Since Q and U are atomic-level polarization dominated in this region, the upper bound for magnetic field strengths is in the range of a few hundred Gauss ( $B \lesssim 500$  G). The amplitude of Stokes V sets the lower bound, indicating that field strengths are in the saturated regime of the Hanle effect. For the He I 10830 Å triplet, the onset of Hanle saturation is near 8 G and 1 G for the upper level and lower level Hanle effects, respectively (AR08). Consequently, the degree of linear polarization is not sensitive to the magnetic field strength within the superpenumbral region, but is only sensitive to the direction of the magnetic field. To constrain the full magnetic field vector of superpenumbral fibrils, we require the detection of a significant level of circular polarization (i.e., Stokes V). For this reason, an oblique observing geometry where the sunspot is not too near the disk center is preferred over a disk-center perspective since fibrils are likely to be horizontal to the solar surface.

In the saturated Hanle regime, the population imbalances induced by anisotropic radiative pumping lead to linear polarization oriented either parallel or perpendicular to the horizontal component of the magnetic field (Trujillo Bueno & Asensio Ramos 2007). Classical determinations of the scattering phase matrix (see, e.g., Section 5.8 of Landi Degl'Innocenti & Landolfi 2004) can be used to illustrate this principle for the classical analog of an "unpolarized" lower level (i.e.,  $J_l = 0$ ) and a polarizable upper level with  $J_{\mu} = 1$ , and further illuminates the so-called Van Vleck effect. Upper level population pumping favors either the  $\pi$  or the  $\sigma(\Delta M = \pm 1)$  transitions for this transition according to the Van Vleck angle  $\theta_V$  defined when the angle between the radiation symmetry axis and the magnetic field is 54°.74. For the classical analog, one would expect selective emission processes to generate linear polarization parallel to the magnetic field for inclinations  $\theta_B$  (w.r.t. to the solar vertical and the radiation symmetry axis) greater than  $\theta_V$ and less than  $(\pi - \theta_V)$ , and linear polarization perpendicular to the magnetic field otherwise. Multiterm calculations for the He I red component indicate that these expectations also apply to the collective behavior of the two red transitions. Consider once again the simple model sunspot and make the common assumption that superpenumbral fibrils are oriented mostly horizontal to the solar surface (i.e.,  $\theta_B = 90^\circ$ ) and extend radially from the sunspot. The induced atomic-level polarization for the red transitions is then expected to be parallel to the magnetic field, in fact the opposite of the polarization of the  $\pi$ -component for the Zeeman-dominated profiles discussed in the previous section. The sign change in Q and U for the red component as a function of radius observed in Figure 2 can thus be explained by and offers evidence for the near horizontal and radial orientation of superpenumbral fibrils.

Lower level *depopulation* and *repopulation* processes complicate the interpretation of the polarization of the blue He I component (see Trujillo Bueno et al. (2002) for a complete discussion of optical pumping within the He I triplet). As can be seen in Figures 2 and 3, the observed linear polarization in the blue component has the opposite orientation compared to the red component and can be seen to agree in pattern with the lobe structure of the Zeeman-dominated region. If one assumes that the decay of the polarized, short-lived upper levels accounts for the polarization of the lower level in a *repopulation* scenario,



Figure 4. Thirty-nine fibrils manually traced by inspection of the entire observed He I spectral data cube using CRISPEX. The fibrils traced constitute curvilinear features of greater absorption and account for lateral variations of the Doppler shift and width of the He I triplet. The full Stokes spectrum of the point indicated by the yellow star is given in Figure 6.

the linear polarization of the blue component should be opposite to the red component as observed in the superpenumbral region. For the He I triplet, this assumption can be validated for inclination angles away from the Van Vleck angle using the realistic multiterm calculations of AR08.

# 5. ANALYSIS METHODS

While the observed He I polarization signatures offer heuristic support for the horizontal and mostly radial orientation of fibril magnetic fields, ultimately we wish to infer through inversion the magnetic field vector within individual superpenumbral fibrils, first to compare it with the visible fibril morphology, and then to study the 3D magnetic architecture of the fibrils. This requires first an efficient approach to select and model the visual aspects of each fibril. Here, we describe our approach as well as give details of the forward model and inversion method used to infer the magnetic field parameters from the fibril spectra.

# 5.1. Fibril Tracing

In the case of high-resolution narrowband imaging, Jing et al. (2011) suggested an automated way of selecting and modeling individual fibrils. Using a threshold-based method, individual fibrils are located and fit with second-order polynomials. The orientation angle of the fibril projected in the plane of the sky (POS) is derived from the slope along this modeled curve. Unlike single-channel narrowband imaging, the FIRS data contain the full spectral information of the He I triplet over the full FOV. It is advantageous to capitalize on the additional information as the spectral features of individual fibrils often exhibit variations in their Doppler velocity and Doppler width along their axis. Narrowband imaging alone may restrict the full characterization of a fibril due to these variations.

The locations of individual fibrils in our FIRS data are found using the CRisp SPectral EXplorer (CRISPEX; Vissers & Rouppe van der Voort 2012), which is a widget-based visualization tool capable of quickly exploring spectroscopic and spectropolarimetric data cubes. A particularly useful feature of CRISPEX allows the selection of points along loop-like features. Since we can explore the spectral direction of the data cube while selecting points, we can trace fibrils exhibiting variations in Doppler velocity and/or width along their length. In this way, we locate 39 fibril features in our FIRS scan (see Figure 4).

Once the points of the individual fibrils are selected, we model their projected morphology to derive their orientation angle in the POS. As in Jing et al. (2011), we model each fibril with a simple functional fit (i.e., y = f(x)), defined in our case by an *n*th order polynomial. Most fibrils except, for example, superpenumbral whorls can be fit in this way. Sometimes we must rotate reference axes to ensure that the selected fibril locations are fit as a function of the direction along its primary axis. The derived orientation angles, which we also refer to as visible or "traced" orientation angles, can then be transformed into a common geometry.

Each fibril is fit to an appropriately ordered polynomial selected according to the Bayesian Information Criterion (Schwarz 1978; Asensio Ramos et al. 2012):

$$BIC = \chi_{\min}^2 + k \ln N, \qquad (2)$$

where  $\chi^2_{\min}$  is the normal summed squared difference between the data points and the fitted model, N is the number of data points, and k is the number of free parameters in the model (i.e., an *n*th order polynomial has k = n + 1 free parameters). The best model is selected as the one which minimizes the BIC. Of the 39 traced fibrils, 16 are best fit by a first-order linear function, 14 by a second-order, 8 by a third-order, and 1 by a fourth-order polynomial. We collect the spectra along the modeled fibril axis at points found from a parametric cubic spline interpolation with a interval distance of 0.''3. In total, 985 individual fibril Stokes spectra are selected for analysis. The projected orientation angle for each sampled location along the fibril is calculated from the first derivative of the fitted polynomial model, which for a curvilinear feature in the POS includes an intrinsic 180° ambiguity.

### 5.2. Inversions of the He I Triplet

HAZEL refers to the advanced "Hanle and Zeeman Light" forward modeling and inversion tool developed by AR08. Based on multiterm calculations (see Landi Degl'Innocenti & Landolfi 2004) of a five-term model of the orthohelium atomic system, HAZEL determines the population imbalances and quantum coherences induced by anisotropic radiative pumping using the framework of the atomic density matrix. The absorption and emission coefficients follow from the elements of the density matrix calculated via the statistical equilibrium equations subject to a limb darkened cylindrically symmetric radiation field whose symmetry axis is the solar vertical.<sup>5</sup> HAZEL also correctly accounts for the Hanle, Zeeman, and Paschen–Back effects. (see AR08 for more details).

We use the inversion capability of HAZEL to interpret the 985 observed He I Stokes spectra from the 39 selected fibrils. The equation defining the RT for each Stokes vector is an exact analytical solution of a constant-property slab model including magneto-optical terms and stimulated emission. The slab is described by the following deterministic quantities: thermal Doppler broadening  $v_{th}$ , macroscopic LOS velocity  $v_{mac}$ , optical thickness  $\Delta \tau$ , damping parameter *a*, magnetic field *B*, magnetic field inclination angle  $\theta_B$ , and magnetic field azimuthal angle  $\chi_B$  at a constant height *h*.

The oblique geometry of the observed region greatly influences the manner in which we use HAZEL. As described by AR08 and Merenda et al. (2006), He I spectropolarimetric observations at disk center and off-limb are subject to two ambiguities: (1) the Van Vleck ambiguity for some range of inclinations and (2) the familiar 180° ambiguity which introduces a 180° azimuth ambiguity at disk center and off-limb, and in addition the off-limb Stokes spectra for  $\langle B, \theta_B, \chi_B \rangle$ are  $\langle B, 180^\circ - \theta_B, -\chi_B \rangle$  are indistinguishable. According to AR08 and Trujillo Bueno (2010), an oblique scattering angle introduces a quasi-degeneracy associated with having the preferential axis of the Zeeman effect and that of the radiation symmetry be different from 0° or 90°. This degeneracy is lifted for large oblique angles such that the Zeeman effect and atomic-level polarization work to remove some ambiguities (see Landi Degl'Innocenti & Bommier 1993); however, which ambiguities remain can be difficult to determine. Moreover, observational noise can introduce ambiguities. We thus rely on the DIRECT algorithm (Jones et al. 1993) described in AR08 to search for ambiguous solutions for all possible field geometries (i.e.,  $0^{\circ} < \theta_B < 180^{\circ}, 0^{\circ} < \chi_B < 360^{\circ}$ ).

Our inversion scheme relies on the available HAZEL tools with a different implementation than AR08. We find that the thermodynamic parameters should not be fit independently with fits only to Stokes *I*. Fibril spectra near the sunspot exhibit significant Zeeman magnetic broadening. We do not single out these spectra. Rather, we create a standardized approach for all spectra. First, we remind the reader that optimizing the model solution involves minimizing the reduced  $\chi^2$  merit function (AR08):

$$\chi^2 = \frac{1}{4} \sum_{i=1}^4 w_i \chi_i^2, \tag{3}$$

where the individual contributions of the  $\chi^2$  to for each Stokes parameter is

$$\chi_i^2 = \frac{1}{N_\lambda} \sum_{j=1}^{N_\lambda} \frac{\left[S_i^{\text{syn}}(\lambda_j) - S_i^{\text{obs}}(\lambda_j)\right]^2}{\sigma_i^2(\lambda_j)} \tag{4}$$

 $\chi^2_{i=0,1,2,3} = \chi^2_{I,Q,U,V}$  and all other variables are as defined in AR08. We choose a four-step approach similar to AR08. First, the thermodynamic parameters are found via the DIRECT algorithm with the model parameters  $v_{\rm th}$ ,  $v_{\rm mac}$ ,  $\Delta \tau$ , B,  $\theta_B$ , and  $\chi_B$  free to vary within a realistic range. Such a great number of free parameters reduces the convergence efficiency of the DIRECT approach due to an increased dimensionality which must be compensated for by a greater number of function evaluations. We improve the efficiency by weighting the Stokes I  $\chi^2$  (i.e.,  $\chi^2_I$ ) greater than the others (i.e.,  $w_I = 5, w_{O,U,V} = 1$ ). Furthermore, the damping parameter, a is not a free parameter. We calculate a directly from the Doppler width,  $v_{\rm th}$ , using the Einstein coefficient of the transition, which accounts for thermal effects only. In a second step, the free parameters are fine-tuned using the Levenburg-Marquardt (LM) method of HAZEL. We find that this procedure gives much more reliable determinations of the thermodynamics parameters for all spectra.

Once the thermodynamics parameters ( $v_{\text{th}}$ ,  $v_{\text{mac}}$ , and  $\Delta \tau$ ) are determined, we locate all relevant solutions for the magnetic field strength and direction. We use the method suggested by AR08 that exploits the properties of the deterministic DIRECT searching algorithm, a key component of which is that no region of the parameter space is entirely eliminated from the search process over a great number of iterations. Ambiguous solutions are found via systematic searching of the parameter space. The number of function evaluations increases in regions of the parameter space resulting in better model fits forming clusters in maps of the searching process (see Figure 5 here and Figure 17 of AR08). We allow for a total of 3000 function evaluations by the DIRECT algorithm to locate these regions in the B,  $\theta_B, \chi_B$  hyper-volume (i.e., *n*-dimensional parameter space), during which all Stokes parameters are weighted equally in the merit function (Equation (3)). Up to three regions are then identified in the DIRECT searching maps according to two criteria: (1) the possible solutions must be separated in the  $\theta_B, \chi_B$  space (top of Figure 5) and (2) the best fit in the identified cluster must be less than  $\chi^2_{min} + \delta_{\chi}$ , where  $\chi^2_{min}$  is the minimum reduced  $\chi^2$  found by the DIRECT algorithm.

<sup>&</sup>lt;sup>5</sup> We ignore the symmetry-breaking effects of the sunspot. The degree of symmetry breaking due to a spot can be expressed as a function of its solid angle as viewed from a given point in the atmosphere (see Section 12.4 of Landi Degl'Innocenti & Landolfi 2004). A sunspot of small solid angle as viewed from the fibrils introduces a weak symmetry breaking of the impringing radiation field that weakly influences the emergent polarization of the fibrils. We are unable to discern the role of this symmetry breaking from these measurements. While the sensitivity shown here is great, we require a further reduction of the noise to evaluate this effect. We leave this for future work.



**Figure 5.** Illustration of the hyper-volume search performed by the DIRECT algorithm used to locate solution ambiguities, as in Asensio Ramos et al. (2008). Each data point represents one point (of 3000) in the hyper-volume for which DIRECT calculates the  $\chi^2$  parameter, as defined in Equation (3). The colored regions are areas where  $\chi^2 < \chi^2_{min} + 0.25$ , our prescription for regions of probable ambiguities.

We choose a value of  $\delta_{\chi}$  equal to 0.25, as this is the change in  $\chi^2_{min}$  induced by a 1 $\sigma$  error in any one of  $\chi^2_{I,Q,U,V}$ . The result of this process for the spectra from the location marked by a yellow star in Figure 4 is illustrated in Figure 5. As seen in the figure, two  $\theta_B, \chi_B$  subspaces are identified as possible solutions. The best fit in each subspace is identified and finetuned in a fourth inversion step that once again employs the LM method initialized with the identified DIRECT solutions. These determined parameters are then our best-fit determinations of the plasma thermodynamic and magnetic properties (see Figure 6).

We do not fit the height of the plasma as a free parameter. Population imbalances are a function of the anisotropic properties of the pumping radiation field. Due to geometry, the degree of anisotropy varies as a function of height, as well as the mean intensity; albeit, this dependence is weaker (AR08).<sup>6</sup> Merenda et al. (2011) used this principle to infer the height of chromospheric material above an emerging flux region. AR08 noted this possibility but also described that a quasi-degeneracy between height and inclination can make it difficult to infer the height without an additional constraint on the field geometry. We elect, due to the level of noise in our observations, to keep the height as an assumed constant and then discuss the influence of this choice in Section 6.5. The NLTE calculations of Centeno et al. (2008) indicate a large range of heights contributing to He I absorption. For the one-dimensional FAL-C atmospheric model (Fontenla et al. 1993), the range of He I formation is between 1 and 2.2 Mm above the solar surface. This is consistent with the correspondence between He I, H $\alpha$ , and Ca II described

<sup>6</sup> A pitfall we discovered here is that this mean intensity change also affects the determination of  $\Delta \tau$  via the emission coefficient  $\epsilon_{I}$ .  $\Delta \tau$  then is a weak function of height and influences the goodness of fit, meaning  $\Delta \tau$  needs to be a free parameter investigated alongside the height dependence of the polarized spectra.



**Figure 6.** Observed He triplet Stokes spectrum taken from a superpenumbral fibril (open circles) and fit with HAZEL inversions. Two solutions are found with similarly good fits and correspond to the two regions identified in Figure 5. The blue solid line corresponds to the best-fit magnetic field vector of B = 262 G,  $\theta_B = 101^\circ$ , and  $\chi_B = 40^\circ$ , with  $\chi^2_{Q,U,V} = \{1.23847, 1.12328, 1.51492\}$ . The yellow dot-dashed line corresponds to the slightly poorer fit using B = 139 G,  $\theta_B = 34^\circ$ , and  $\chi_B = 100^\circ$ , which yields  $\chi^2_{Q,U,V} = \{1.26013, 1.62421, 1.50613\}$ . (A color version of this figure is available in the online journal.)



**Figure 7.** Comparison of all determinations of the projected angle of the inferred magnetic field vector (i.e., the line-of-sight azimuthal angle,  $\chi_B$ ) and the visible projected angle of the observed fibrils,  $\chi_{\rm fib}$ . For each inverted spectrum, all the inferred solutions found via the HAZEL inversions are plotted vs. the two values of the visible projected azimuth, which has an inherent 180° ambiguity. The blue circles, black squares, and orange triangles, respectively, correspond to the first, second, and third best solution for any single HAZEL inversion. The open and closed data points distinguish between the two ambiguous visible directions.

in Section 3. The primary contribution to the He I absorption is consequently thought to be within a fibril's depth of the contribution peak of the H $\alpha$  and Ca II. Leenaarts et al. (2012) argue that fibrils in H $\alpha$  are formed at higher relative heights than the inter-fibril plasma and showed fibril formations ranging from 1.5 to 2.75 Mm. We fix the height used for the inversions at 1.75 Mm in accordance with these observations.

#### 6. RESULTS

In Figure 7, we plot the full results of the Section 5 analysis for every selected fibril location at which the Stokes spectrum is reasonably well fit with the HAZEL inversion method (i.e.,  $\chi^2_{L,O,U}$  < 2.5). A total of 592 (of 985) spectra meet this criteria. The figure includes the effect of all ambiguities. On the x-axis,  $\chi_{fib}$  is the projected angle of the observed "visible" fibril as manually traced in the POS with the inherent 180° ambiguity. For each value of  $\chi_{fib}$ , the y-axis reports the azimuths,  $\chi_B$ , of the inferred magnetic field solutions resulting from the inversion of the observed Stokes spectra, and transformed into the LOS geometry (i.e., the projected angle of the magnetic field transverse to the LOS). The reference direction for both  $\chi_{fib}$  and  $\chi_B$  points toward solar west. Note the already strong correlation of many of the solutions in this plot which represents the effect of all ambiguities. The ordered nature of this figure is due to the non-random influence of the Van Vleck and 180° ambiguities. When these effects are taken into account, as discussed below, this figure provides direct evidence for the field alignment of superpenumbral fibrils well outside of the penumbral boundary.

#### 6.1. Variation of the Magnetic Field Vector Along Individual Fibrils

We concentrate on four representative fibrils (fibrils 6, 16, 31, and 32 in Figure 4) and plot the full results as a function

of distance from the sunspot center in Figure 8. Two different reference systems are used here to report the inclination and azimuth of the magnetic field vector. The inclination refers to the angle between the magnetic field direction and the local solar vertical and is directly determined by HAZEL. An outward-directed radial magnetic field has  $\theta_B = 0^\circ$  and a value of 90° refers to a horizontal magnetic field. Meanwhile, to allow direct comparison, the azimuths of the magnetic field vector and the modeled fibril orientation angle are given in the LOS geometry since one cannot transform the projected angle of the traced fibril into solar coordinates. Lastly, since there is good reason to believe that the flows follow the magnetic field in this ion–neutral coupled, high electric conductivity plasma (Judge et al. 2010), we plot the magnitude of the velocity directed along the magnetic field vector according to

$$v_{\parallel B} = \frac{-v_{\rm LOS}}{\cos\theta_{B,\rm LOS}},\tag{5}$$

where  $\theta_{B,LOS}$  is the inclination of the magnetic field in the lineof-sight geometry,  $v_{LOS}$  is the velocity projected along the line of sight (negative values correspond to velocities of approach, i.e., blueshifted spectra), and  $v_{||B}$  is the velocity projected along the derived magnetic field. With the negative sign in Equation (5), we assign negative values of  $v_{||B}$  to flows that are anti-parallel to the magnetic field direction.

Let us first compare the two determinations of the azimuth in Figure 8. For each fibril, different classes of solutions are found for  $\chi_{B,LOS}$ . In the case of fibrils 6 and 16, only one of these classes (represented by filled data points in the figure) matches only one determination of the traced orientation angle. For fibrils 31 and 32, both ambiguous determinations of the projected orientation angle are matched by a class of HAZEL solutions along the fibril. This behavior can be explained by comparing the magnitudes of the LOS component of the magnetic field in each case. For all ambiguous solutions found for the same Stokes spectra, the LOS field magnitude must be nearly the same, but subject to the role of observational noise. The LOS magnitude of **B** for fibrils 6, 16, 31, and 32 are on average 81, 126, 25, and 57 G, respectively. If one compensates for the large field strengths of fibril 32 near the sunspot, a lower value would be more representative of the LOS field magnitude. Fibrils 31 and 32 show fields oriented more perpendicular to the LOS than 6 and 16, with lower values of  $|B_{LOS}|$ . This results in Stokes V signals of lower amplitude, at or close to the level of the noise. Consequently, the Stokes V spectra of fibrils 31 and 32 cannot be used to distinguish between the two azimuth solutions, whereas in fibrils 6 and 16 this ambiguity is resolved with Stokes V. Fields that are oriented nearly perpendicular to the LOS are subject to the 180° Hanle ambiguity.

Now consider the additional information of the inclination angle. It should be noted that the sunspot umbra hosts a field of inward-directed polarity (i.e.,  $\theta_B \approx 180^\circ$ ). The azimuth matched solutions of fibrils 6 and 16 are characterized by horizontal fields, and in the case of fibril 16, the inclination increases near the sunspot reflecting a downward turn into the sunspot and consistent with the polarity of the umbra. The inclinations of 31 and 32 are noisier, but the one solution found for fibril 32 within the sunspot radius,  $r_{spot}$ , is consistent with the polarity of the sunspot umbra. Furthermore, the azimuth of this solution (filled circles), when compared to the one matching solution of fibril 6, is consistent with the variation in the fibril direction around the sunspot. As there is only one solution for fibril 32 with the sunspot's radius, we have an unambiguous determination of the



Figure 8. Derived magnetic field parameters along fibrils 6, 16, 31, and 32 identified in Figure 4. All found solutions are represented, with blue circles denoting the best-fit solution. The filled data points correspond to the solutions matching the visible azimuth determined via tracing the fibril (solid lines). See the text for details.  $r_{spot} \approx 8.7 \text{ Mm}$ .

fibril magnetic field and it is directed along the fibril axis. For each fibril, the classes of solutions which do not match any traced fibril direction are characterized by inclinations near the sunspot below the Van Vleck angle and are discontinuous with the polarity of the sunspot. These solutions are consistent with the influence of the Van Vleck effect on the inversion process and are ruled unphysical since the magnetic field is expected to be continuous along the fibril. The picture of fibrils rooted in the sunspot that become nearly horizontal away from the sunspot is thus supported by these measurements.

We characterize all 39 analyzed fibrils in the same manner as above and detail these results in Table 2. The average values of the fibril orientation angles ( $\bar{\chi}_{fib}$ ) and the inferred LOS azimuth of the magnetic field  $(\bar{\chi}_B)$  are given only for the solutions not classified as Van Vleck ambiguities. The deviation  $(\Delta \bar{\chi}_n)$ between the average orientation angle and the average LOS azimuth is recorded as a factor of the standard deviation  $(\sigma_n)$  of the LOS magnetic field azimuths, which represent the dominate source of error. Only for fibrils 15, 21, and 22 do the inferred azimuths of the magnetic field  $(\bar{\chi}_B)$  deviate more than  $3\sigma$  from the traced orientation angle  $(\bar{\chi}_{\rm fib})$ . These fibrils correspond to short fibrils selected in a complex area of the observed region far from the sunspot. We expect that improper selection or modeling explains their  $>3\sigma$  deviation in azimuth rather than a real misalignment of the field and fibril. This table also reiterates that fields with a direction primarily transverse to the LOS introduces

a  $180^{\circ}$  ambiguity in the azimuth. This affects those fibrils on the southwest side of the sunspot (Nos. 19–35). The fibrils on the northwest side (Nos. 1–18, expect 12) all have one single inverted solution for the magnetic field azimuth that matches the azimuthal direction of the traced fibrils. The spectra of fibrils 36–39 are not well fit with a one component HAZEL model.

### 6.2. Correlation of Visible and Inferred Azimuths

Figure 9 illustrates the results found in Table 2 and is akin to Figure 7 without the Van Vleck induced solutions. The filled data points correspond to fibrils with only one matching azimuth, while the open circles are plotted for the pair of solutions for the fibrils with a  $180^{\circ}$  ambiguity in their azimuth. These different situations are classified according to their azimuth angle. A Spearman ranking test of these solutions gives a correlation coefficient of 0.935. We consider this the best proof to date that fibrils are visual markers for the magnetic field.

# 6.3. Maps of Fibril Quantities

We investigate the spatial variation of the fibril magnetic field vector with spatial maps of the field parameters (see Figure 10). Although the parameter errors are not well known,<sup>7</sup> spatial

<sup>&</sup>lt;sup>7</sup> Formal errors in a spectropolarimetric inversion is a matter of current research. The Bayesian framework in Asensio Ramos et al. (2007) seems best-suited to define confidence intervals of the returned parameters but is for now too computationally intensive to implement here.

Table	2
Comparison of Visible and Inferred	Azimuthal Direction of Fibrils

Fibril No.	$\bar{\chi}_{\rm fib}({\rm visible})^{\rm a}$	$\bar{\chi}_B$ (inferred) <sup>b</sup>	$\Delta \bar{\chi}_n / {\sigma_n}^c$	$ \bar{B}_{LOS} $ (inferred)	Comments
1	77.921	62.590	-1.641	39.0	One additional Van Vleck induced solution
2	63.862	54.857	-0.933	86.5	One additional Van Vleck induced solution
3	59.239	74.640	2.057	25.0	One additional Van Vleck induced solution
4	58.852	51.105	-0.607	79.9	One additional Van Vleck induced solution
5	57.214	54.102	-0.263	21.8	One additional Van Vleck induced solution
6	48.909	58.194	1.077	81.4	One additional Van Vleck induced solution
7	50.074	58.482	1.161	109.5	One additional Van Vleck induced solution
8	48.968	43.365	-0.258	28.0	One additional Van Vleck induced solution
9	46.801	48.367	0.174	122.3	One dominant matching solution
10	44.002	47.319	0.252	51.8	One additional Van Vleck induced solution
11	43.622	53.649	1.014	113.3	One additional Van Vleck induced solution
12	9.004, 188.567	54.124, 155.680	2.803, -3.912	79.2	Two inconsistent solutions
13	26.623	49.956	1.693	154.7	One additional Van Vleck induced solution
14	9.662	29.578	0.854	110.9	Noisy spread in two Van Vleck induced solutions
15	122.277	160.680	3.731	43.8	Two additional Van Vleck induced solutions
16	0.312	10.120	0.460	126.1	Noisy spread in two Van Vleck induced solutions
17	6.394	13.633	0.391	160.1	Two additional Van Vleck induced solutions
18	-40.317	-5.052	2.831	66.2	One additional Van Vleck induced solution
19	-64.574, 112.216	-21.747, 140.917	1.785, 13.528	69.4	One additional Van Vleck induced solution
20	-24.941, 162.636	-19.952, 137.908	0.367, -2.392	53.0	One additional Van Vleck induced solution
21	-63.104, -63.104	-12.864, -109.765	4.143, -6.463	25.6	Two inconsistent solutions
22	-50.687, 123.633	-23.109, 143.933	2.732, 7.529	54.7	One additional Van Vleck induced solution
23	-33.498, 146.502	-12.147, 153.163	1.436, 0.456	30.9	One additional Van Vleck induced solution
24	-35.495	-17.558	1.660	34.3	One additional Van Vleck induced solution
25	-37.024, 141.248	-23.240, 160.169	1.355, 1.911	41.2	One additional Van Vleck induced solution
26	-41.884	-29.319	2.585	33.7	One additional Van Vleck induced solution
27	-50.588, 129.491	-40.223, 140.274	0.382, 0.600	33.5	One additional Van Vleck induced solution
28	-50.297, 130.065	-34.746, 139.278	1.745, 0.542	91.0	Two dominant solutions, minor Van Vleck influence
29	-45.863, 134.719	-40.235, 129.986	0.133, -0.242	16.5	One additional Van Vleck induced solution
30	-49.705, 130.312	-51.324, 127.301	-0.088, -0.198	16.1	One additional Van Vleck induced solution
31	-54.316, 125.811	-43.265, 136.224	0.752, 0.962	24.9	One additional Van Vleck induced solution
32	-61.479, 116.690	-45.945, 142.609	0.545, 2.486	56.6	Two additional Van Vleck induced solutions
33	-53.871, 126.138	-32.228, 137.541	2.439, 1.177	21.9	One additional Van Vleck induced solution
34	-59.724, 120.274	-50.920, 128.125	1.151, 1.125	17.5	One additional Van Vleck induced solution
35	-54.248, 126.856	-41.159, 112.941	1.382, -0.392	306.0	Two dominant solutions, minor Van Vleck influence

Notes.

<sup>a</sup> The average visible (i.e., traced) azimuth direction of each fibril has a 180° ambiguity.

<sup>b</sup> Average, disambiguated azimuths inferred via HAZEL inversion are given in the line-of-sight geometry with a reference direction consistent with the azimuths found via tracing and modeling the fibril morphology.

<sup>c</sup> Total azimuthal angle error estimated to be approximately 20° per spatial pixel.

trends can be indicative of real changes. Field inclinations and azimuths are given here in the same local solar geometry whose reference axis is the solar vertical and polar axis (azimuth reference direction) points toward disk center. For the fibrils exhibiting a  $180^{\circ}$  ambiguity, we only display the solution that best matches the field direction at a height of 1.75 Mm within a current-free extrapolation of the photospheric magnetic field. This extrapolation is computed from a  $300'' \times 300''$  subregion of the full-disk *SDO*/HMI magnetogram centered on the AR and is based on the equations of Alissandrakis (1981) and Gary (1989). At this point, we use this only as an approximation as other means of disambiguating this  $180^{\circ}$  Hanle ambiguity should be explored. Of course, observations with better signal to noise will eliminate this ambiguity in some cases.

The fibril magnetic field strengths show a gradient toward lower field strengths outward from the sunspot down to 50 to 100 G from 600 to 800 G above the penumbra (magnetic field color table of Figure 10 saturates at 600 G). Inclinations of all fibril endpoints terminating within the sunspot show an increase in inclination consistent with a magnetic field turning downward into the negative polarity sunspot. These sunspotrooted fibrils all display a mostly horizontal field outside of the outer penumbral boundary. The outer endpoint of these fibrils does not show a common pattern. Fibrils 32, 27, and 16 exhibit a turnover toward lower inclinations ( $\theta_B < 90^\circ$ ) at their outer endpoints giving the impression that these fibrils are anchored field loops rooted at one end in the sunspot and at the other in the nearby photosphere (see next section). Fibrils numbered 2, 6, 7, 9, and 11, however, remain mostly horizontal at their outer endpoints, with little indications of whether the fields at this point turn upward or downward. Fibril 1 shows increases in inclinations with distance from the spot, but the inner endpoint is primarily horizontal and located outside the penumbral boundary.

## 6.4. The Underlying Photospheric Magnetic Field

By comparing the fibril magnetic field vector and the photospheric vector magnetic field, we gain a more complete picture of the how chromospheric fibrils might be anchored at lower heights. The Si I absorption line measured by FIRS at 10827.089 Å ( $g_{eff} = 1.5$ ) provides a good diagnostic of the



**Figure 9.** Comparison of the average visible projected angle of the fibrils and the inferred, disambiguated average azimuthal direction of the magnetic field. The visible azimuths have an inherent  $180^{\circ}$  ambiguity and that all values are given in the line-of-sight geometry in which a vector with an azimuthal angle of zero points toward solar east. The values are given along with the individual fibril numbers in Table 2.

photospheric magnetic field due to the Zeeman effect. Furthermore, the Si I spectra are acquired strictly simultaneously with the He I triplet at 10830 Å for each spatial pixel in the FIRS scan. As in Bethge et al. (2012), we use the Milne–Eddington (ME) inversion scheme implemented in the HELIx<sup>+</sup> inversion code (Lagg et al. 2004, 2007) to derive the vector magnetic field from the Si I line averaged over its formation height, which, according to Bard & Carlsson (2008), is between 300 and 550 km above the solar surface for umbral-type and quiet solar atmospheres, respectively. The derived azimuths include a 180° ambiguity inherent in the transverse Zeeman effect. To resolve this ambiguity prior to transforming the magnetic field vector into local solar coordinates, we make use of the automated ambiguityresolution code developed by Leka et al. (2009), which is based on the Minimum Energy Algorithm by Metcalf (1994).

The disambiguated, transformed vector magnetic field resultant from inversions of the Si I 10827.089 Å line is presented in Figure 11 in the same geometry as Figure 10. Contours are given for the solar inclination of this photospheric field at values of  $135^{\circ}$  (dotted),  $90^{\circ}$  (dot-dashed), and  $65^{\circ}$  (solid) and are plotted also in the maps of Figure 10. Azimuths in the chromospheric fibrils show general consistency with the azimuths of the penumbral filaments below. Additionally, we plot the variation of the photospheric magnetic field and field-projected velocity (see Equation (5)) directly below our representative fibrils in Figure 12, except for fibril 31 which is above a region of the photospheric field not well represented by the combination of disambiguation and coordinate transformation.

As described in Section 3, the sunspot is trailed by opposite polarity plage. Ahead (i.e., solar west) of the spot is a large area of plage matching the polarity of the sunspot. Just south of the sunspot is a close-proximity area of flux with polarity opposite of the sunspot. It is in this region that the outer endpoint of fibril 32 terminates providing evidence that the fibril is a closed field loop rooted in the sunspot on one end and in the opposite polarity flux on the other. Fibril 16 also shows this behavior. The arrows in Figures 10 and 11 indicate areas of significant opposite signed flux. Fibril 15 exhibits behavior consistent with its one endpoint (close to the spot) rooted in this opposite polarity flux. Fibrils numbered 2, 6, 7, 9, and 11, discussed above, do not clearly terminate above opposite flux (see fibril 6 in Figure 12). The most prominent flux concentrations in this region are the leading plage with the same polarity as the sunspot. Are these fibrils directed over the plage? Or are they connected to unresolved footpoint fields below? This becomes the same question as for internetwork flux discussed in Section 1.

### 6.5. The Influence of Height of Inversion

Our inversions do not take into account differences in the height of formation along individual fibrils or between multiple fibrils. Rather, all inversions are carried out with the same assumed height of 1.75 Mm. Ideally, one could use the spectra themselves to estimate the fibril heights either by letting height be a free parameter in addition to the magnetic field parameters (Merenda et al. 2011), or by constraining the field direction ( $\theta_B$ or  $\chi_B$ ) by some other means (AR08), such as by using the fibril direction itself. Due to the influence of noise in our observations, we are unable to constrain the height in either of these ways. As can be seen in Figures 8 and 12, significant scatter exists in the determined field parameters along each fibril. This scatter is used to estimate the error in the average fibril azimuths in Table 2. Prohibitive as this scatter can be, we are confident that within the error, the fibrils are aligned with the magnetic field using the assumed height of 1.75 Mm. In Figure 13, we show the median field parameters of fibril 6, tracking as it were the solution we found at a height of 1.75 Mm for all heights between 0 and 15 Mm. This range extends well beyond what can be considered reasonable heights for fibril formation yet the change in the average inclination is only 20°. Figure 18 of AR08 shows a similar dependence of the returned inclination with height. Between 0 and 5 Mm, the variation in the inverted azimuthal angle is only 10°. Unfortunately, we cannot use this height influence to estimate the fibril formation height since the range in Figure 13 is on the order of the error in the field parameters inferred at 1.75 Mm. Thus, while we cannot further constrain the height, the influence of the height does not affect our primary results.

# 7. DISCUSSION

## 7.1. Relation of Fibrils to the Magnetic Field

This paper has described the first vector magnetic field determinations within resolved superpenumbral fibrils. Unlike observations in the Ca II 8542 Å spectral line (de la Cruz Rodríguez & Socas-Navarro 2011), we find strong HeI linear polarization signatures originating from the superpenumbral canopy. A heuristic interpretation of these polarized spectra alongside advanced inversions from HAZEL lends support for field-aligned fibrils that are primarily horizontal  $(\pm 20^{\circ})$  with respect to the solar surface. We find little evidence for any misalignment of the thermal and magnetic structure of these fibrils and thus support extrapolation methods such as Wiegelmann et al. (2008) and Yamamoto & Kusano (2012), which use the fibril direction to constrain the horizontal magnetic field direction in the chromosphere. Yet, further comparisons must be made between these extrapolations and actual measurements of the magnetic field strength and inclination, in particular due to the limitations of the force-free assumption in these extrapolations.

A recent observation of a kink wave in an AR dynamic fibril (Pietarila et al. 2011) under assumptions regarding the unknown plasma density provided estimates of the fibril field strengths between 100 and 350 G. We find magnetic field strengths less than 300 G throughout the superpenumbra exterior to the



**Figure 10.** Spatial maps of the magnetic field vector of superpenumbral fibrils inferred from the He I triplet. The black data points indicate locations for which the goodness of fit to the observed spectra is poor. The contours of the photospheric magnetic field inclination are also given for values of  $135^{\circ}$  (dotted),  $90^{\circ}$  (dot-dashed), and  $65^{\circ}$  (solid). The inclination and azimuth values are given in the local solar reference frame. The vector directions of many fibrils suffer from a  $180^{\circ}$  Hanle ambiguity, which is here resolved with a potential field extrapolation of the photospheric magnetic field. The black arrows indicate regions of plage with a polarity opposite w.r.t. the spot. See the text for more details.



Figure 11. Photospheric magnetic field vector in local solar coordinates for the entire FIRS field of view derived from a Milne–Eddington analysis of the Si I 10827.089 Å spectral line. The contours of the inclination angle are overplotted for the inclination plot at the same values as in Figure 10. The selected fibrils are also overplotted. The arrows denote the locations of the photospheric magnetic field with opposite polarity w.r.t. the sunspot umbra.

penumbral boundary. The fibrils that extend into the sunspot penumbra exhibit a rise in field strengths. Future time resolved measurement in He I may grant a diagnostic of the unknown density when pairing field estimates with wave observations.

# 7.2. Endpoint Connectivity of Fibrils

Spatial trends in the inferred magnetic field inclination in both the chromosphere and photosphere are used here to study the 3D nature of superpenumbral fibrils. We find evidence that most superpenumbral fibrils are rooted in the sunspot, as expected, and magnetic fields that are more vertically directed at that endpoint. These fibrils become more horizontal with increased distance from the sunspot, especially as the fibrils cross the outer penumbral boundary. A few of these fibrils turn over once again to connect in regions of oppositely directed flux in the photosphere. Others do not show this behavior and remain nearly horizontal at their outer endpoints, which are located near plage of the same polarity as the sunspot. In Foukal's (1971b) picture, these fibrils might turn upward into the upper atmosphere and connect with flux elsewhere. We see no evidence for this in the fibril inclinations. Furthermore, unlike H $\alpha$  and Ca II, He I can still sense cooler material at greater heights, suggesting that the fibrils may be further extended in He I than in H $\alpha$  if they indeed turn upward. The observations in Figure 1 give little indication that this is happening; however, these He I maps suffer from poor temporal resolution due to the slit-scanning time.



**Figure 12.** Photospheric vector magnetic field resultant from a Milne–Eddington analysis of the Si I 10827.089 Å spectral line shown for points directly below selected fibrils along the line of sight. The magnetic field vector within the fibrils is overplotted. The far right panel displays the component of the photospheric flow velocity along the photospheric magnetic field vector.



**Figure 13.** Influence of the assumed height on the inversions of the He I spectra within the superpenumbral fibrils. The median magnetic field vector components of fibril 6 is shown as a function of the height of inversion.

It is not understood why we do not see a change in inclination at the outer endpoint of some fibrils. We suggest that projection effects may play a role and/or limited opacity of He I at lower heights for some fibrils. The latter argument would require a thermodynamic difference between those fibrils with and without outer endpoint inclination changes. Thus, we cannot conclude at this time that all the fibril material represents closed field loops rooted just below both their endpoints, as argued by Reardon et al. (2011) via visible constraints on the loop trajectory. A way forward may be the study of the three-dimensional velocity field in H $\alpha$  of CaII from IBIS, as in Judge et al. (2010). Ji et al. (2012) established for an arcade of low coronal loops a connectivity of finescaled neutral helium channels within intergranular lanes, as observed in very high resolution narrowband images of the HeI triplet at 10830 Å. These methods, in addition to further spectropolarimetric measurements, may aid in addressing the connectivity of fine-scaled internetwork and superpenumbral fibrils.

Nevertheless, the fibrils seen here to turn over at both ends correspond with an outer endpoint of stronger fields relative to the surrounding areas. Fibril 32, for example, is rooted at one endpoint in the strong sunspot and in  $\sim$ 375 G plage at the outer endpoint. If the fibrils that exhibit no turn over (fibrils 2, 6, 7, 9, and 11) are in reality connected below, it must be within weaker flux elements (B < 200 G) or fine-scaled flux elements below the resolution of the observations.

### 7.3. Relation of Superpenumbral Flows to Magnetic Architecture

Each observed fibril displays significant motion along its axis as measured with the He I Doppler shift. The direction of the observed flow is consistent with inward-directed inverse Evershed flow. Ultimately, we wish to study the thermo-magnetic properties of individual fibrils to understand the driving mechanisms of these flows and other observed phenomena. Unfortunately, the poor temporal resolution of these FIRS observations limits our ability to comment on the temporal evolution of these flows. However, we can comment on the magnetic architecture that hosts the flows.

In siphon flow models of the chromospheric Evershed flow (Meyer & Schmidt 1968; Maltby 1975; Cargill & Priest 1980), the driving force is a gas pressure difference along the fibril caused by off-balanced magnetic pressure at the fibril footpoints. Bethge et al. (2012) examined a cool feature, interpreted as

a loop, which displayed opposite signed LOS flows at its endpoints. The magnetic flux difference at these endpoints could explain the observed flow magnitude in a siphon flow scenario. Bethge et al. (2012) argued that the material undergoes a deceleration at its stronger magnetic footpoint according to multi-wavelength observations. Decelerated flow is a key component of siphon flow, in both the subsonic or shocked flow cases (see Cargill & Priest 1980).

In the outer footpoint, which hosts the upflow, Bethge et al. (2012) showed LOS velocities of similar magnitude for He I and Ca II H 3968.5 Å. Unfortunately, due to the geometry involved, the acceleration of the upflow is difficult to constrain without knowledge of the field geometry. A common feature of the fibrils observed here is a lateral gradient of the LOS velocity along the fibrils. Under the assumption that the flow is directed along the field, we derived the total magnitude of the flow (see Equation (5) and Figure 8). Fibrils 6 and 16 showed weakly accelerating flows at their outer footpoints. We estimate an acceleration of  $\sim 40$  m s<sup>-2</sup> for the outer end of fibril 16. However, without finer determinations of the fibril inclination, we cannot at this time distinguish whether this acceleration is siphon driven or perhaps gravitationally driven.

#### 8. CONCLUDING REMARKS

We have employed high spatial and high spectral resolution spectropolarimetry of the He I triplet at 10830 Å to probe the local magnetic field vector in individual superpenumbral fibrils. Key to this work has been the ability to achieve observations of high signal-to-noise and high polarization accuracy at high spatial resolution, which has come at the price of temporal resolution. Yet, despite this limitation, the application of the advanced forward modeling and inversion techniques of Asensio Ramos et al. (2008) yields several new inferences for the magnetic field vector within fibrils. The primary conclusions of this work are as follows:

- 1. Superpenumbral fibrils do trace the magnetic field. Despite the role of ambiguities in the determination of the magnetic field vector, He I inversions nearly always return a solution whose projected field direction is consistent (generally within  $\pm 10^{\circ}$ ) with the projected direction of the visible fibrils
- 2. The inner endpoint of superpenumbral fibrils hosts a detectable change in inclination as it turns into the sunspot where the fibrils are rooted.
- 3. Opposite signed flux roots the outer endpoint of fibrils in at least two cases, but the connectivity of most of the fibrils is hard to establish. If they are rooted below, as we suspect they are, they are connected to fine-scaled magnetic flux elements below the resolution of FIRS (0.3).

Perhaps none of these conclusions are that surprising. We confirm basic assumptions that have been made in the literature now for decades. Demonstrated here, though, is a powerful new means to measure both the macro-scaled and fine-scaled features of the chromospheric field with currently available instrumentation. Yet, the relevant temporal scales of important upper atmospheric dynamics are still out of reach for chromospheric spectropolarimetry using the existing small-aperture solar facilities. We stress the need for large-aperture facilities coupled to high-sensitivity (imaging-) spectropolarimeters both on the ground such as the Advanced Technology Solar Telescope (Rimmele & ATST Team 2008), and in new space missions, such as the Solar-C mission (Shimizu et al. 2011).

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