# THE ELM SURVEY. I. A COMPLETE SAMPLE OF EXTREMELY LOW-MASS WHITE DWARFS* 

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#### Abstract

We analyze radial velocity observations of the 12 extremely low-mass (ELM), with $\leqslant 0.25 M_{\odot}$, white dwarfs (WDs) in the MMT Hypervelocity Star Survey. Eleven of the twelve WDs are binaries with orbital periods shorter than 14 hr ; the one non-variable WD is possibly a pole-on system among our non-kinematically selected targets. Our sample is unique: it is complete in a well-defined range of apparent magnitude and color. The orbital mass functions imply that the unseen companions are most likely other WDs, although neutron star companions cannot be excluded. Six of the eleven systems with orbital solutions will merge within a Hubble time due to the loss of angular momentum through gravitational wave radiation. The quickest merger is $\mathbf{J} 0923+3028$, a $g=15.7$ ELM WD binary with a 1.08 hr orbital period and a $\leqslant 130 \mathrm{Myr}$ merger time. The chance of a supernova Ia event among our ELM WDs is only $1 \%-7 \%$, however. Three binary systems (J0755+4906, $\mathrm{J} 1233+1602$, and $\mathrm{J} 2119-0018$ ) have extreme mass ratios and will most likely form stable mass-transfer AM CVn systems. Two of these objects, SDSS J1233+1602 and J2119-0018, are the lowest surface gravity WDs ever found; both show Ca II absorption likely from accretion of circumbinary material. We predict that at least one of our WDs is an eclipsing detached double WD system, important for constraining helium core WD models.


Key words: Galaxy: stellar content - stars: individual (J211921.96-001825.8, SDSS J075552.40+490627.9, SDSS J081822.34+353618.9, SDSS J092345.60+302805.0, SDSS J123316.20+160204.6, SDSS J143948.40+100221.7, SDSS J151225.70+261538.5) - white dwarfs

Online-only material: color figures, machine-readable table

## 1. INTRODUCTION

Extremely low-mass (ELM) white dwarfs (WDs), with masses $<0.3 M_{\odot}$, are the remnants of stars that never ignited helium in their cores. The universe is not old enough to produce ELM WDs by single star evolution. Thus ELM WDs must undergo significant mass loss during their evolution. Although metal-rich red giants with strong winds may evolve in isolation into single $\simeq 0.4 M_{\odot}$ WDs (Kilic et al. 2007c), producing $\simeq 0.2$ $M_{\odot}$ ELM WDs most likely requires compact binary systems (e.g., Marsh et al. 1995). Observational data for ELM WDs are limited, however, because of their rarity. For example, among the 9316 WDs identified in the Sloan Digital Sky Survey (SDSS), fewer than $0.2 \%$ have masses below $0.3 M_{\odot}$ (Eisenstein et al. 2006; Kepler et al. 2007).
Kilic et al. $(2009,2010 b)$ have established a radial velocity program to search for companions around known ELM WDs. Of the six ELM WDs observed to date-including J0917+4638, the lowest mass WD known (Kilic et al. 2007b)—all six ELM WDs are in binaries with $\leqslant 1$ day orbital periods. Two more recently identified ELM WDs, NLTT 11748 and J1257+5428 (Kawka \& Vennes 2009; Marsh et al. 2010; Kulkarni \& van Kerkwijk 2010), are also in binaries with $<1$ day orbital periods (Steinfadt et al. 2010; Kawka et al. 2010; Kilic et al. 2010a). Three of these eight ELM WDs will merge due to gravitational wave radiation in less than 500 Myr (Mullally et al. 2009; Kilic et al. 2010b).

[^0]A larger sample of ELM WDs is required to measure the space density, period distribution, and merger rate of these systems.
Here we present 12 ELM WDs with $\leqslant 0.25 M_{\odot}$ found in the Hypervelocity Star (HVS) Survey of Brown et al. (2005, 2006a, 2006b, 2007a, 2007b, 2009a, 2009b), 10 of which are new discoveries. Our ELM WD sample is unique because it comes from a complete, non-kinematically selected survey of stars targeted in a well-defined range of apparent magnitude and color. Radial velocity follow-up reveals that 11 of the 12 ELM WDs are binaries with $<14 \mathrm{hr}$ orbital periods. Clearly, the compact binary formation scenario is the best explanation for ELM WDs.

In Section 2, we describe the survey design and the spectroscopic observations. In Section 3, we derive the physical parameters of the ELM WDs with stellar atmosphere modeling and present the radial velocity curves for each object. In Section 4, we discuss the nature of the binary systems and conclude in Section 5.

## 2. DATA

### 2.1. Survey Design

The ELM WDs reported here are found in the HVS Survey, a radial velocity survey of objects with the colors of late-B type stars. All survey targets were selected from the SDSS photometric catalog using dereddened, uber-calibrated pointspread function magnitudes (Adelman-McCarthy et al. 2008). The HVS Survey color selection is illustrated in Figure 1. Although the color selection was designed to exclude normal WDs by their $(u-g)$ color, the selection fortuitously includes low surface gravity WDs (see Figure 1).


Figure 1. Color-color diagram showing the observed distribution of ELM WDs (solid stars) and the other WDs (crosses, circles) found in the HVS Survey ( $15<g_{0}<17$, dot-dashed line; $17<g_{0}<19.5$, dashed line; $19.5<g_{0}<20.5$, dotted line) compared with our synthetic photometry of the hydrogen atmosphere WD models of D. Koester (solid lines).
(A color version of this figure is available in the online journal.)

The HVS Survey consists of three parts. The first part of the HVS Survey is defined by $15<g_{0}<17$ (dash-doted line in Figure 1) and is $100 \%$ complete over $7300 \mathrm{deg}^{2}$ of the SDSS Data Release 5 footprint Brown et al. (2007a). The second part of the HVS Survey is defined by $17<g_{0}<19.5$ (dashed line in Figure 1) and is $100 \%$ complete over the same $7300 \mathrm{deg}^{2}$ of the SDSS Data Release 5 footprint Brown et al. (2007b). The final part extends the earlier surveys over $9800 \mathrm{deg}^{2}$ of the SDSS Data Release 7 footprint and also extends the magnitude limit to $g_{0}=20.5$ (dotted line), as described in Brown et al. (2009a). The final part of the HVS Survey is currently $88 \%$ complete.

Our spectroscopy reveals that $15 \%$ of the HVS Survey targets are WDs. Two of the WDs with $\simeq 0.2 M_{\odot}$ are previously published elsewhere (Kilic et al. 2007a, 2010b). Here, we present the remaining 10 WDs with mass $\leqslant 0.25 M_{\odot}$.

### 2.2. Spectroscopic Observations

With the exception of $\mathrm{J} 0923+3028$, we obtained all observations at the 6.5 m MMT telescope using the Blue Channel Spectrograph. We operate the spectrograph with the 832 line $\mathrm{mm}^{-1}$ grating in second order, providing wavelength coverage $3650 \AA-4500 \AA$ and a spectral resolution of $1.0-1.2 \AA$, depending on the slit size used. We obtain all observations at the parallactic angle with a comparison lamp exposure paired with every observation.

We obtained spectroscopy for J0923+3028 at the Fred Lawrence Whipple Observatory 1.5 m Tillinghast telescope using the FAST spectrograph (Fabricant et al. 1998). We operate the FAST spectrograph with the 600 line $\mathrm{mm}^{-1}$ grating, providing wavelength coverage $3600 \AA-5500 \AA$ and a spectral resolution of $2.3 \AA$. All observations are paired with a comparison lamp exposure.

We process the spectra using IRAF $^{5}$ in the standard way. We flux-calibrate using blue spectrophotometric standards (Massey et al. 1988), and we measure radial velocities using the crosscorrelation package RVSAO (Kurtz \& Mink 1998).

### 2.3. Radial Velocities

It is important to maximize velocity precision in our tests for variability, and we achieve the best precision by crosscorrelating the ELM WDs with themselves. Our procedure begins by cross-correlating the observed spectra with a high signal-to-noise WD template to obtain preliminary velocities. We then shift the spectra to the rest frame and sum them together to create templates for each target. Finally, we cross-correlate the spectra with the appropriate template to obtain the final velocities for each target. The average radial velocity uncertainty of the measurements is $\pm 18 \mathrm{~km} \mathrm{~s}^{-1}$.
We check our velocities using WD model spectra with atmospheric parameters customized for each target. The results are consistent within $10 \mathrm{~km} \mathrm{~s}^{-1}$, which we take as our systematic uncertainty. Table A. 1 in the Appendix presents the full set of radial velocity measurements for the 10 newly discovered ELM WDs presented here.

## 3. RESULTS

Our time-series spectroscopy provides for robust determinations of effective temperature and surface gravity for each object as well as its binary orbital parameters. Follow-up spectroscopy of $\mathrm{J} 0917+4638$ and $\mathrm{J} 1053+5200$ is already published (Kilic et al. 2007b, 2010b), but the other ELM WDs in our sample have not been studied until now.

### 3.1. Stellar Atmosphere Parameters

We perform stellar atmosphere model fits using synthetic DA WD spectra kindly provided by D. Koester. The grid of WD model atmospheres covers effective temperatures from 6000 K to $30,000 \mathrm{~K}$ in steps of 500 K to 2000 K , and surface gravities from $\log g=5.0$ to 9.0 in steps of 0.25 dex. The model atmospheres are calculated assuming local thermodynamic equilibrium and include both convective and radiative transport (Koester 2008). We perform fits on the average composite spectra for each object and present the resulting $T_{\text {eff }}$ and $\log g$ values in Table 1. We also perform fits to the individual spectra to derive a robust statistical error estimate for each object, also presented in Table 1. Figure 2 shows the composite spectra and our model fits. The surface gravities range 5.1-6.9 dex at effective temperatures of $10,400-18,300 \mathrm{~K}$, confirming that the objects are ELM WDs.

We fit the flux-calibrated spectral continua to better measure effective temperature. The exception is J2119-0018, the one ELM WD we observed under variable conditions and at high airmass, for which we fit the continuum-corrected spectrum. If we fit only the continuum-corrected Balmer line profiles for all the ELM WDs, we obtain best-fit solutions that differ by $440 \pm 190 \mathrm{~K}$ in $T_{\text {eff }}$ and $0.04 \pm 0.04$ dex in $\log g$ from our published values. These differences reflect our systematic error, and demonstrate that our fits to the entire flux-calibrated spectra are reasonably accurate. Our fits also agree well with the SDSS photometry in all five filters, an additional demonstration

[^1]Table 1
White Dwarf Physical Parameters

| Object | $g_{0}$ <br> $(\mathrm{mag})$ | $(u-g)_{0}$ <br> $(\mathrm{mag})$ | $(g-r)_{0}$ <br> $(\mathrm{mag})$ | $T_{\text {eff }}$ <br> $(\mathrm{K})$ | $\log g$ | $M_{g}$ <br> $(\mathrm{mag})$ | $d_{\text {helio }}$ <br> $(\mathrm{kpc})$ | Mass <br> $\left(M_{\odot}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J0755+4906 | $20.095 \pm 0.023$ | $0.763 \pm 0.086$ | $-0.304 \pm 0.039$ | $13160 \pm 260$ | $5.84 \pm 0.07$ | 8.0 | 2.62 | 0.17 |
| $\mathrm{~J} 0818+3536$ | $20.484 \pm 0.030$ | $0.766 \pm 0.152$ | $-0.274 \pm 0.058$ | $10620 \pm 380$ | $5.69 \pm 0.07$ | 8.0 | 3.14 | 0.17 |
| $\mathrm{~J} 0917+4638^{\mathrm{a}}$ | $18.696 \pm 0.019$ | $0.738 \pm 0.037$ | $-0.328 \pm 0.024$ | $11850 \pm 170$ | $5.55 \pm 0.05$ | 8.0 | 1.38 | 0.17 |
| J0923+3028 | $15.628 \pm 0.018$ | $0.190 \pm 0.027$ | $-0.401 \pm 0.021$ | $18350 \pm 290$ | $6.63 \pm 0.05$ | 8.4 | 0.28 | 0.23 |
| J1053+5200 | $18.874 \pm 0.023$ | $0.395 \pm 0.049$ | $-0.358 \pm 0.045$ | $15180 \pm 600$ | $6.55 \pm 0.09$ | 8.7 | 1.08 | 0.20 |
| J1233+1602 | $19.829 \pm 0.018$ | $0.809 \pm 0.068$ | $-0.233 \pm 0.028$ | $10920 \pm 160$ | $5.12 \pm 0.07$ | 8.0 | 2.32 | 0.17 |
| J1422+4352 | $19.794 \pm 0.020$ | $0.715 \pm 0.061$ | $-0.271 \pm 0.032$ | $12690 \pm 130$ | $5.91 \pm 0.07$ | 8.0 | 2.29 | 0.17 |
| J1439+1002 | $17.812 \pm 0.016$ | $0.434 \pm 0.042$ | $-0.341 \pm 0.026$ | $14340 \pm 240$ | $6.20 \pm 0.07$ | 8.0 | 0.92 | 0.18 |
| J1448+1342 | $19.217 \pm 0.023$ | $0.581 \pm 0.047$ | $-0.286 \pm 0.033$ | $12580 \pm 230$ | $6.91 \pm 0.07$ | 9.9 | 0.73 | 0.25 |
| J1512+2615 | $19.241 \pm 0.021$ | $0.551 \pm 0.051$ | $-0.258 \pm 0.030$ | $12130 \pm 210$ | $6.62 \pm 0.07$ | 9.3 | 0.97 | 0.20 |
| J1630+2712 | $20.040 \pm 0.019$ | $0.818 \pm 0.083$ | $-0.223 \pm 0.031$ | $11200 \pm 350$ | $5.95 \pm 0.07$ | 8.0 | 2.56 | 0.17 |
| J2119-0018 | $20.000 \pm 0.021$ | $0.867 \pm 0.092$ | $-0.197 \pm 0.033$ | $10360 \pm 230$ | $5.36 \pm 0.07$ | 8.0 | 2.51 | 0.17 |

## Notes.

${ }^{\text {a }}$ Kilic et al. (2007b).
${ }^{\mathrm{b}}$ Kilic et al. (2010b).


Figure 2. Model fits (cyan lines) overplotted on the composite observed spectra (black lines). The spectral continua provide improved $T_{\text {eff }}$ determination except for the poorly fluxed-calibrated $\mathrm{J} 2119-0018$, for which we use the continuum-corrected spectrum.
(A color version of this figure is available in the online journal.)
that our temperature and surface gravity measurements are reliable.

Figure 3 compares the observed ELM WDs and other WDs in the HVS Survey with the improved Panei et al. (2007) tracks (see Kilic et al. 2010b) for He-core WDs with masses $0.16-0.45 M_{\odot}$ and the Bergeron et al. (1995) ${ }^{6}$ tracks for normal CO-core WDs with masses $0.5-1 M_{\odot}$. The gap between the

[^2]$0.17 M_{\odot}$ and $0.18 M_{\odot}$ He-core WD tracks is linked to the threshold for thermonuclear flashes in the hydrogen shell burning phase (Panei et al. 2007). Remarkably, the majority of observed ELM WDs fall in the gap of parameter space between the $0.17 M_{\odot}$ and $0.18 M_{\odot}$ models.

The inconsistency between the observations and the Hecore WD models make accurate mass and luminosity estimates difficult. Fortunately, mass and luminosity change slowly over the range of effective temperature and surface gravity sampled by our ELM WDs. We conclude that the majority of the ELM WDs have a mass of $\simeq 0.17 M_{\odot}$ and absolute magnitudes of


Figure 3. Surface gravity vs. effective temperature of the observed ELM WDs (red stars) and the other WDs (crosses, circles) found in the HVS Survey, compared with predicted tracks for He WDs with $0.16-0.45 M_{\odot}$ (blue lines; Panei et al. 2007) and CO WDs with 0.5-1.0 $M_{\odot}$ (green lines; Bergeron et al 1995; Holberg \& Bergeron 2006). Our sample of ELM WDs is defined by $m \leqslant 0.25 M_{\odot}$.
(A color version of this figure is available in the online journal.)
$M_{g} \simeq 8$; more precise estimates are possible for the $0.20-$ $0.25 M_{\odot}$ ELM WDs and are summarized in Table 1.

Using these absolute magnitude estimates, the majority of our ELM WDs are found at heliocentric distances of $1<d<$ 3 kpc . The notable exception is J $0923+3028$, a bright $g=15.7$ ELM WD approximately 280 pc distant. All of our ELM WDs are located at high Galactic latitudes $30^{\circ}<|b|<80^{\circ}$ in the SDSS imaging footprint.

The systemic velocities suggest that two objects are halo WDs: J0818+3536 and J1422+4352 that have systemic heliocentric radial velocities of $-201 \pm 4 \mathrm{~km} \mathrm{~s}^{-1}$ and $-195 \pm 8 \mathrm{~km} \mathrm{~s}^{-1}$, respectively. Kilic et al. (2010b) also identify J1053+5200 as a halo object based on its proper motion and distance estimate. Unfortunately, reliable proper motions are unavailable for our fainter $g \simeq 20$ WDs. Despite having relatively large $>1 \mathrm{kpc}$ distances above the Galactic plane, the remaining ELM WDs in our sample have systemic radial velocities consistent with a disk origin.

### 3.2. Orbital Parameters

Eleven of our twelve ELM WDs exhibit significant radial velocity variation, with peak-to-peak velocity amplitudes up to $890 \mathrm{~km} \mathrm{~s}^{-1}$. We compute orbital periods for these systems by finding the period that minimizes $\chi^{2}$ for a circular orbit. Figure 4 plots the periodograms for the 10 new ELM WDs. A few ELM WDs have multiple period solutions because of insufficient coverage, however in all cases the periods are constrained to be $<1$ day. We estimate the period error by conservatively identifying the range of periods with $\chi^{2} \leqslant 2 \chi_{\text {min }}^{2}$, where $\chi_{\text {min }}^{2}$ is the minimum $\chi^{2}$.

We compute best-fit orbital elements using the code of Kenyon \& Garcia (1986), which weights each velocity measurement by its associated error. The uncertainties in the orbital
elements are derived from the covariance matrix and $\chi^{2}$. To verify these uncertainty estimates, we perform a Monte Carlo analysis where we replace the measured radial velocity $v$ with $v+g \delta v$, where $\delta v$ is the error in $v$ and $g$ is a Gaussian deviate with zero mean and unit variance. For each of the 10,000 sets of modified radial velocities, we repeat the periodogram analysis and derive new orbital elements. We adopt the interquartile range in the period and orbital elements as the uncertainty. For binaries with multiple period aliases, both approaches yield similar uncertainties. When there are several equally plausible periods, the Monte Carlo analysis selects all possible periods and derives very large uncertainties. In these cases, we adopt errors from the covariance matrix for the lowest $\chi^{2}$ orbital period.

We present the best-fit orbital parameters in Table 2. Columns include orbital period $(P)$, radial velocity semi-amplitude $(K)$, systemic velocity ( $V_{\text {systemic }}$ ), the time of spectroscopic conjunction (the time when the object passes through $0 \mathrm{~km} \mathrm{~s}^{-1}$ as it approaches the observer), mass function (see Equation (1) below), and minimum secondary mass (assuming $i=90^{\circ}$ ). The systemic velocities in Table 2 are not corrected for the WDs, gravitational redshifts, which should be subtracted from the observed velocities to find the true systemic velocities. This correction is approximately $3 \mathrm{~km} \mathrm{~s}^{-1}$ for our targets.

We plot the best-fit orbits compared to the observed radial velocities in Figure 5, excluding the two objects previously published. Follow-up observations were typically obtained over a pair of three-day time baselines separated by one week, plus an original observation that extends the baseline up to 1488 days (not shown in the upper panel of Figure 5). The ELM WD's short orbital periods combined with our long-time baselines allow us to constrain the orbital periods accurately.

## 4. DISCUSSION

### 4.1. J0755+4906

SDSS J075552.40+490627.9 exhibits the largest radial velocity variation in our sample of ELM WDs. The WD has a best-fit amplitude of $876 \pm 10 \mathrm{~km} \mathrm{~s}^{-1}$, an orbital period of $1.512 \pm$ 0.051 hr , and a binary mass function of

$$
\begin{equation*}
\frac{M_{2}^{3} \sin ^{3} i}{\left(M_{1}+M_{2}\right)^{2}}=\frac{P K^{3}}{2 \pi G}=0.550 \pm 0.025 M_{\odot} \tag{1}
\end{equation*}
$$

where $i$ is the orbital inclination angle, $M_{1}$ is the ELM WD mass, and $M_{2}$ is the companion mass. Although the inclination is unknown, we can use the distribution of possible inclinations to constrain the companion's mass.

Given the observed orbital parameters, there is a $61 \%$ probability that J0755+4906's companion is a WD with $<1.4 M_{\odot}$ and a $20 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. The remaining probability is for a companion mass $>3 M_{\odot}$. We estimate the most probable companion mass by assuming the mean inclination angle for a random stellar sample, $i=60^{\circ}$. For J0755+4906, the most likely companion is a $1.12 M_{\odot}$ object at an orbital separation of $0.7 R_{\odot}$. Follow-up radio or X-ray observations are required to rule out a neutron star companion, but statistically the companion is most likely a massive WD.
Short-period binaries like J0755+4906 must eventually merge due to angular momentum loss to gravitational wave radiation. The merger time is

$$
\begin{equation*}
\tau=\frac{\left(M_{1}+M_{2}\right)^{1 / 3}}{M_{1} M_{2}} P^{8 / 3} \times 10^{-2} \mathrm{Gyr} \tag{2}
\end{equation*}
$$



Figure 4. Periodograms for the 10 new ELM WDs. Some objects have multiple period aliases because of insufficient coverage, however in all cases the periods are constrained to $<1$ day. J1448+1342 is formally consistent with no velocity variability.

Table 2
Binary Orbital Parameters

| Object | $\begin{gathered} P \\ \text { (days) } \\ \hline \end{gathered}$ | $\begin{gathered} K \\ \left(\mathrm{~km} \mathrm{~s}^{-1}\right) \end{gathered}$ | $\begin{aligned} & V_{\text {systemic }} \\ & \left(\mathrm{km} \mathrm{~s}^{-1}\right) \\ & \hline \end{aligned}$ | Spec. Conjunction $(\text { days }+2450000)$ | Mass Function | $\begin{gathered} M_{2} \\ \left(M_{\odot}\right) \end{gathered}$ | $\tau_{\text {merge }}$ (Gyr) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| J0755+4906 | $0.06302 \pm 0.00213$ | $438 \pm 5$ | $-51 \pm 4$ | $5150.84949 \pm 0.00010$ | $0.550 \pm 0.025$ | $\geqslant 0.81$ | $\leqslant 0.22$ |
| J0818+3536 | $0.18315 \pm 0.02110$ | $170 \pm 5$ | $-201 \pm 4$ | $5151.90466 \pm 0.00030$ | $0.094 \pm 0.014$ | $\geqslant 0.26$ | $\leqslant 8.89$ |
| J0917+4638 ${ }^{\text {a }}$ | $0.31642 \pm 0.00002$ | $145 \pm 2$ | $28 \pm 1$ | $3708.85755 \pm 0.00134$ | $0.102 \pm 0.003$ | $\geqslant 0.27$ | $\leqslant 36.8$ |
| J0923+3028 | $0.04495 \pm 0.00049$ | $296 \pm 3$ | $2 \pm 2$ | $3818.67019 \pm 0.00002$ | $0.121 \pm 0.004$ | $\geqslant 0.34$ | $\leqslant 0.13$ |
| J1053+5200 ${ }^{\text {b }}$ | $0.04256 \pm 0.00002$ | $264 \pm 2$ | $12 \pm 2$ | $3790.79731 \pm 0.00004$ | $0.081 \pm 0.002$ | $\geqslant 0.26$ | $\leqslant 0.16$ |
| J1233+1602 | $0.15090 \pm 0.00009$ | $336 \pm 4$ | $-35 \pm 3$ | $5268.84901 \pm 0.00014$ | $0.597 \pm 0.020$ | $\geqslant 0.86$ | $\leqslant 2.14$ |
| J1422+4352 | $0.37930 \pm 0.01123$ | $176 \pm 6$ | $-195 \pm 8$ | $4596.92484 \pm 0.00068$ | $0.208 \pm 0.023$ | $\geqslant 0.41$ | $\leqslant 42.9$ |
| J1439+1002 | $0.43741 \pm 0.00169$ | $174 \pm 2$ | $-55 \pm 1$ | $3882.68848 \pm 0.00079$ | $0.240 \pm 0.007$ | $\geqslant 0.46$ | $\leqslant 54.7$ |
| J1448+1342 ${ }^{\text {c }}$ |  | $35 \pm 7$ | $-28 \pm 5$ |  |  |  |  |
| J1512+2615 | $0.59999 \pm 0.02348$ | $115 \pm 4$ | $-41 \pm 4$ | $3879.48768 \pm 0.00119$ | $0.097 \pm 0.012$ | $\geqslant 0.28$ | $\leqslant 171$ |
| J1630+2712 | $0.27646 \pm 0.00002$ | $218 \pm 5$ | $-118 \pm 3$ | $5009.72779 \pm 0.00016$ | $0.295 \pm 0.018$ | $\geqslant 0.52$ | $\leqslant 15.6$ |
| J2119-0018 | $0.08677 \pm 0.00004$ | $383 \pm 4$ | $-28 \pm 4$ | $5008.88701 \pm 0.00003$ | $0.501 \pm 0.016$ | $\geqslant 0.75$ | $\leqslant 0.54$ |

Notes.
${ }^{\text {a }}$ Kilic et al. (2007b).
${ }^{\mathrm{b}}$ Kilic et al. (2010b).
${ }^{\mathrm{c}}$ The measurements are formally consistent with no variation.
where the masses are in $M_{\odot}$ and the period $P$ is in hours (Landau \& Lifshitz 1958). For a companion mass of $1.1 M_{\odot}$, J0755+4906 will merge in 170 Myr. Kilic et al. (2010b) discuss the many possible stellar evolution paths for such a merging system. For J0755+4906, there is at least a $6 \%$ likelihood that the system contains a pair of WDs whose total mass exceeds the Chandrasekhar mass and thus will explode as a Type Ia supernova. On the other hand, the extreme mass ratio $M_{1} / M_{2} \leqslant 0.21$ means that mass transfer is likely to be stable and thus this binary will probably evolve into an AM CVn system.

### 4.2. J0818+3536

The best-fit orbital period for SDSS J081822.34+353618.9 is $4.396 \pm 0.51 \mathrm{hr}$, however the limited number of follow-up observations allow for aliases at 5.4 and 8.6 hr periods. Periods longer than 14 hr are ruled out. Thus J0818+3536 is a shortperiod binary. Assuming the best-fit period, there is a $90 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $5 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. For the most probable inclination angle $i=60^{\circ}$,
the companion is a $0.33 M_{\odot}$ low-mass WD at orbital separation of $1.1 R_{\odot}$.

## 4.3. $J 0917+4638$

Previously published by Kilic et al. (2007b), SDSS J091709.55+463821.8 has a binary orbital period of $7.5936 \pm$ 0.0005 hr . Assuming an inclination angle of $60^{\circ}$, its companion is another low-mass WD with $0.35 M_{\odot}$ at an orbital separation of $1.6 R_{\odot}$.

Curiously, J0917+4638 and the two other ELM WDs with lower surface gravity in our sample (J1233+1602 and J2119-0018) all show significant CaII K absorption in their atmospheres (Figure 2). The extremely short timescale for gravitational settling of Ca in the WD photospheres means there must be an external source for the observed metals (Koester \& Wilken 2006; Kilic et al. 2007a). The ELM WDs are located far above the Galactic plane where accretion from the interstellar medium is unlikely. A plausible source of Ca is accretion from a circumbinary disk created during the mass loss phase of the
giant. Since the ELM WDs all went through a common envelope phase with a companion, a leftover circumbinary disk is possible.
4.4. J0923+3028

SDSS J092345.60+302805.0 is the brightest ELM WD in our sample, with $g=15.7$ mag and a heliocentric distance estimate of $280 \mathrm{pc} . \mathrm{J} 0923+3028$ has a binary orbital period of $1.079 \pm 0.012 \mathrm{hr}$ and a mass function of $0.121 \pm 0.004 M_{\odot}$. There is a $87 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $6 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. For the most probable inclination angle, $i=60^{\circ}$, the companion is a $0.44 M_{\odot} \mathrm{WD}$ at orbital separation of $0.5 R_{\odot}$. Thus, J0923+3028 is the second shortest period double WD system after J1053+5200 (Kilic et al. 2010b). This system will merge in less than 130 Myr .

J0923+3028 is the one ELM WD in our sample with a significant proper motion measurement, $\mu_{\alpha} \cos \delta=-4.2 \pm 3.5$ and $\mu_{\delta}=-25 \pm 3.5$ mas $^{\mathrm{yr}}{ }^{-1}$ (Munn et al. 2004). The gravitational


Figure 5. Data and best-fit orbits for the 10 new ELM WDs. Upper panels plot the heliocentric radial velocities vs. time. Lower panels plot the observations phased to the best-fit orbital solution (Table 2), and also include the observation first used to identify the ELM WD candidate. The same vertical axis is used in all 10 plots.


Figure 5. (Continued)
redshift of the WD is $\simeq 4 \mathrm{~km} \mathrm{~s}^{-1}$, thus its true systemic velocity is $-2 \pm 5 \mathrm{~km} \mathrm{~s}^{-1}$. The velocity components with respect to the local standard of rest (Schönrich et al. 2010) are $U=14 \pm 6 \mathrm{~km} \mathrm{~s}^{-1}$, $V=-20 \pm 8 \mathrm{~km} \mathrm{~s}^{-1}, W=-2 \pm 6 \mathrm{~km} \mathrm{~s}^{-1} . \mathrm{J} 0923+3028$ is clearly a disk star.
4.5. J1053+5200

Previously published by Kilic et al. (2010b), SDSS $\mathrm{J} 105353.89+520031.0$ has a binary orbital period of $1.0224 \pm$ 0.0005 hr . Assuming an inclination angle of $60^{\circ}$, the companion is another low-mass WD with $0.33 M_{\odot}$ at an orbital separation of $0.4 R_{\odot}$. This system will merge in less than 160 Myr .

### 4.6. J1233+1602

SDSS J123316.20+160204.6 is the lowest surface gravity WD known. Its surface gravity, $\log g=5.12 \pm 0.07$, is comparable to a $2.5 M_{\odot}$ main-sequence star with $\log g \simeq 4.2$ (Girardi et al. 2002, 2004). However, J1233+1602's binary orbital parameters exclude the possibility of it being a mainsequence star.
$\mathrm{J} 1233+1602$ is a binary with a $3.6216 \pm 0.0022 \mathrm{hr}$ orbital period and a mass function of $0.597 \pm 0.020 M_{\odot}$. By assuming an edge-on orbit, $i=90^{\circ}$, we can place a lower limit on the companion mass. For a $2.5 M_{\odot}$ A star primary, the star must have at least a $2.44 M_{\odot}$ companion at an orbital separation of $2.0 R_{\odot}$. However, the radius of a $2.5 M_{\odot}$ main-sequence star is $1.9 R_{\odot}$. Thus the orbital separation of two A stars in this system is less than their summed radii. Even if the companion were a $2.44 M_{\odot}$ neutron star, the system would still be in Roche lobe overflow, for which we see no evidence.

As a check, we combine the spectra near maximum blueshift and redshift into two composite spectra. If there is a contribution from the companion, it may be visible as second pair of lines or an asymmetry in the line profiles. We do not see any extra lines or asymmetries in the line profiles. We conclude J1233+1602 is $\mathrm{a} \simeq 0.17 M_{\odot}$ WD orbiting a much fainter companion.

Given the observed mass function, there is a $58 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $21 \%$ probability that the companion is a neutron star with $1.4-3.0 M_{\odot}$. Assuming the most probable orbital inclination angle of $60^{\circ}, \mathrm{J} 1233+1602$ 's companion is a 1.2 $M_{\odot}$ WD at an orbital separation of $1.3 R_{\odot}$. Follow-up radio or X-ray observations are required to rule out a neutron star companion, but statistically the companion is most likely a massive WD.

There is a 7\% likelihood that this system contains a pair of WDs whose total mass exceeds the Chandrasekhar mass and thus will explode as a Type Ia supernova. The merger time for such a system is $<2 \mathrm{Gyr}$. However, the extreme mass ratio $M_{1} / M_{2} \leqslant 0.20$ suggests that mass transfer will be stable and this binary will likely evolve into an AM CVn system.
4.7. J1422+4352

SDSS J142200.74+435253.2 has the fewest follow-up observations yet its binary orbital period is reasonably well constrained. The best-fit period is $9.10 \pm 0.27 \mathrm{hr}$, with a significant alias at 15.3 hr . Assuming the best-fit period, there is a $82 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $8 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. For the most probable inclination angle, $i=60^{\circ}$, the companion is a normal $0.55 M_{\odot} \mathrm{WD}$ at orbital separation of $2.0 R_{\odot}$.

### 4.8. J1439+1002

SDSS J143948.40+100221.7 is a binary with a best-fit period of $10.498 \pm 0.041 \mathrm{hr}$. Despite having follow-up observations on 10 nights spaced over one year (see Figure 5), there remains a significant period alias at $18.576 \pm 0.215 \mathrm{hr}$. Using the best-fit orbital solution, there is a $80 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $10 \%$ probability that the companion is a neutron star with $1.4-3.0 M_{\odot}$. For the most probable inclination angle, $i=60^{\circ}$, the companion is a normal $0.62 M_{\odot} \mathrm{WD}$ at orbital separation of $2.2 R_{\odot}$.
4.9. J1448+1342

SDSS J144801.13+134232.8 is the one ELM WD for which we detect no significant velocity variation. The best-fit orbit ( 0.5 hr period) has a reduced $\chi^{2}$ identical to a constant-velocity fit, thus this system can have a velocity semi-amplitude no larger than $K \leqslant 35 \pm 11 \mathrm{~km} \mathrm{~s}^{-1}$. By comparison, the average semiamplitude of the other eleven ELM WD binaries is $240 \mathrm{~km} \mathrm{~s}^{-1}$. The required orbital inclination for $\mathrm{J} 1448+1342$ to have the average semi-amplitude of the other ELM WD binaries is $i \leqslant 8^{\circ}$.

J1448+1342 may be either a pole-on binary system or a single star. If the orbital inclinations of our non-kinematically selected ELM WDs are randomly distributed, we expect one of the twelve ELM WDs to have $i \leqslant 23^{\circ} 5$; there is a $12 \%$ likelihood of finding one of the twelve systems with $i \leqslant 8^{\circ}$. Thus it is possible that $\mathrm{J} 1448+1342$ is a pole-on binary system. The alternative is that $\mathrm{J} 1448+1342$ is a single star. It is intriguing that $\mathrm{J} 1448+1342$ is the most massive object in our sample of 12 ELM WDs. Existing stellar evolution models, however, cannot explain 0.25 $M_{\odot}$ WDs from single star evolution, even with extreme mass loss models (Kilic et al. 2007c). Additional observations are required to determine the nature of this ELM WD.
4.10. J1512+2615

SDSS J151225.70+261538.5 is a binary with a best-fit orbital period of $14.40 \pm 0.56 \mathrm{hr}$, and a significant period alias at 17.8 hr . Assuming the best-fit period, there is an $89 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $5 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. For the most probable inclination angle $i=60^{\circ}$, the companion is a $0.36 M_{\odot}$ low-mass WD at orbital separation of $2.5 R_{\odot}$.

### 4.11. J1630+2712

SDSS J163026.09+271226.5 has a best-fit orbital period of $6.6350 \pm 0.0005 \mathrm{hr}$. The observations also allow for 5.16 and 9.17 hr periods. Assuming the best-fit period, there is a $77 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $11 \%$ probability that the companion is a neutron star with 1.4-3.0 $M_{\odot}$. For the most probable inclination angle $i=60^{\circ}$, the companion is a normal $0.70 M_{\odot} \mathrm{WD}$ at an orbital separation of $1.7 R_{\odot}$.

### 4.12. J2119-0018

SDSS J211921.96-001825.8 is the second lowest surface gravity WD known, with $\log g=5.36 \pm 0.07$. As with J1233+1602, J2119-0018's orbital parameters exclude the possibility of it being a main-sequence A star.
$\mathrm{J} 2119-0018$ is a binary with a $2.0825 \pm 0.0010 \mathrm{hr}$ orbital period and a mass function of $0.501 \pm 0.016 M_{\odot}$. If the primary is $2.5 M_{\odot}$ main-sequence star, its companion must be $\geqslant 2.2 M_{\odot}$
at an orbital separation of $1.4 R_{\odot}$. This separation is smaller than the radius of main-sequence stars. We do not see any evidence of a companion in our spectra. Thus J2119-0018 must be a $\simeq 0.17$ $M_{\odot} \mathrm{WD}$.

Given the observed orbital parameters, there is a $64 \%$ probability that the companion is a WD with $<1.4 M_{\odot}$ and a $18 \%$ probability that the companion is a neutron star with $1.4-$ $3.0 M_{\odot}$. Assuming the most probable orbital inclination angle of $60^{\circ}, \mathrm{J} 2119-0018$ 's companion is a $1.04 M_{\odot} \mathrm{WD}$ at an orbital separation of $0.9 R_{\odot}$. Follow-up radio or X-ray observations are required to rule out a neutron star companion, but the companion is most likely a massive WD.

This system will merge in less than 540 Myr. There is a 5\% likelihood that the system contains a pair of WDs whose total mass exceeds the Chandrasekhar mass and thus will explode as a Type Ia supernova. However, the extreme mass ratio $M_{1} / M_{2} \leqslant 0.23$ suggests that mass transfer will be stable and this binary will likely evolve into an AM CVn system.

## 5. CONCLUSION

We present a complete sample of 12 ELM WDs with masses $\leqslant 0.25 M_{\odot}$ in the HVS Survey. Eleven of the WDs are binary systems with orbital periods $<14 \mathrm{hr}$; J1448+1342 is the only WD for which we detect no velocity variation. Given the binary nature of the other WDs in our non-kinematically selected sample, $\mathrm{J} 1448+1342$ is quite possibly a pole-on system. Our observations demonstrate that the formation of $\leqslant 0.25 M_{\odot}$ ELM WDs requires close binary evolution (Marsh et al. 1995).

Two of our targets, J1233+1602 and J2119-0018, have surface gravities lower than the previous record holder J0917+4638 (Kilic et al. 2007a) and thus are the lowest surface gravity WDs currently known. Interestingly, all three of these low surface gravity ELM WDs exhibit strong Ca absorption in their spectra. The Ca is likely explained by on-going accretion from circumbinary disks. Other sources of accretion are much less likely, given the extremely short timescale for gravitational settling in the ELM WD photospheres and their $1-2 \mathrm{kpc}$ distances above the disk plane.

One possible source of circumbinary disk accretion is debris from former planetary systems (Dong et al. 2010). For the case of our ELM WD binaries, the systems must have had circumbinary planets that could survive the binary common envelope evolution. Common envelope evolution may also lead to "second generation" planet formation (Perets 2010), the debris of which may be accreting onto the ELM WDs. In any case, the lowest surface gravity ELM WDs are interesting targets for future infrared observations.

Six of our 12 ELM WDs (50\%) will merge within a Hubble time (we exclude J1448+1342 due to its unknown period); four of these mergers will happen in $\leqslant 600$ Myr. In all cases, the most likely binary companions are WDs, although neutron stars cannot be ruled out based on the available data. Two of the merger systems, $\mathrm{J} 0818+3536$ and $\mathrm{J} 1053+5200$, are likely to have unusually low-mass ( $<0.4 M_{\odot}$ ) WD companions and thus are possible progenitors for single helium-enriched sdO stars (Heber 2009). Four of the merger systems are likely to have C/O WD companions and thus will likely form extreme helium stars. However, three of the systems (J0755+4906, J1233+1602, and $\mathrm{J} 2119-0018$ ) have such extreme mass ratios $\leqslant 0.23$ that future mass transfer is likely to be stable and thus they will evolve into AM CVn systems.

We expect that at least one of our ELM WDs has $i>85^{\circ}$ and thus is an eclipsing system. Steinfadt et al. (2010) recently
discovered the first eclipsing detached double WD; finding eclipsing WD binaries in our sample will provide important mass-radius constraints on He core ELM WD models. The most probable eclipsing candidates in our sample are the systems with the shortest merger times, namely J0923+3028, J1053+5200, J0755+4906, and J2119-0018.

Our sample of 12 ELM WDs is unique in terms of its nonkinematic selection and its completeness. Previous discoveries of ELM WDs in the SDSS (Liebert et al. 2004; Eisenstein et al. 2006) and other surveys (Kawka et al. 2006; Kawka \& Vennes 2009) have been useful for studying the formation and future evolution of the individual systems (Kilic et al. 2010b). However, the spectroscopic selection biases present in the SDSS prohibit an accurate estimate of the space density of these objects. SDSS WDs were observed by different targeting programs selected with different color, magnitude, and photometric quality cuts as well as different sparse sampling rates that vary over the SDSS survey region (Eisenstein et al. 2006). Our sample, on the other hand, is complete in magnitude, color, and spatial coverage and enables us to estimate the space density and merger rate of ELM WDs in the Milky Way. We explore possible links to underluminous supernovae, AM CVn stars, and other phenomena in a companion paper (Brown et al. 2010).

We thank M. Alegria, J. McAfee, and A. Milone for their assistance with observations obtained at the MMT Observatory, and P. Berlind and M. Calkins for their assistance with observations obtained at the Fred Lawrence Whipple Observatory. We especially thank $P$. Challis obtaining additional observations of J2119-0018, and the referee for helpful comments. This project makes use of data products from the Sloan Digital Sky Survey, which is managed by the Astrophysical Research Consortium for the Participating Institutions. This research makes use of NASA's Astrophysics Data System Bibliographic Services. To perform the Monte Carlo analysis, we used the routine randgen.f, written by R. Chandler and P. Northrop. This work was supported in part by the Smithsonian Institution. M.K. is supported by NASA through the Spitzer Space Telescope Fellowship Program, under an award from CalTech.

Facilities: MMT (Blue Channel Spectrograph)

## APPENDIX

## DATA TABLE

Table A. 1 presents our radial velocity measurements. The table columns include object name, heliocentric Julian date, heliocentric radial velocity, and velocity error.

Table A. 1

| Radial Velocity Measurements |  |  |
| :---: | :---: | ---: |
| Object | HJD <br> +2450000 | $v_{\text {helio }}$ <br> $\left(\mathrm{km} \mathrm{s}^{-1}\right)$ |
| $\mathrm{J} 0755+4906$ | 5150.867780 | $393.5 \pm 17.5$ |
| $\ldots$ | 5267.639886 | $395.4 \pm 12.6$ |
| $\ldots$ | 5267.654862 | $27.8 \pm 11.5$ |
| $\ldots$ | 5267.668518 | $-421.8 \pm 18.0$ |
| $\ldots$ | 5268.675038 | $-363.5 \pm 23.8$ |
| $\ldots$ | 5268.685061 | $-490.9 \pm 19.5$ |
| $\ldots$ | 5268.703821 | $217.5 \pm 22.8$ |
| $\ldots$ | 5268.713913 | $384.5 \pm 22.0$ |
| $\ldots$ | 5269.617361 | $-358.8 \pm 22.0$ |
| $\ldots$ | 5269.628715 | $-386.8 \pm 31.4$ |

(This table is available in its entirety in a machine-readable form in the online journal. A portion is shown here for guidance regarding its form and content.)

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[^0]:    * Based on observations obtained at the MMT Observatory, a joint facility of the Smithsonian Institution and the University of Arizona.
    ${ }^{4}$ Spitzer Fellow.

[^1]:    5 IRAF is distributed by the National Optical Astronomy Observatory, which is operated by the Association of Universities for Research in Astronomy, Inc., under cooperative agreement with the National Science Foundation.

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