SHORT-TERM VARIABILITY AND POWER SPECTRAL DENSITY ANALYSIS OF THE RADIO-LOUD ACTIVE GALACTIC NUCLEUS 3C 390.3

MARIO GLIOZZI¹, IOSSIF E. PAPADAKIS^{2,3}, MICHAEL ERACLEOUS^{4,9}, RITA M. SAMBRUNA⁵, DAVID R. BALLANTYNE⁶,

VALENTINA BRAITO⁷, AND JAMES N. REEVES⁸

¹ George Mason University, 4400 University Drive, Fairfax, VA 22030, USA

² Physics Department, University of Crete, Greece

³ IESL, Foundation for Research and Technology, 71110 Heraklion, Greece

⁴ Department of Astronomy & Astrophysics, The Pennsylvania State University, 525 Davey Lab, University Park, PA 16802, USA

NASA's Goddard Space Flight Center, Code 661, Greenbelt, MD 20771, USA

⁶ Center for Relativistic Astrophysics, School of Physics, Georgia Institute of Technology, 837 State Street, Atlanta, GA 30032, USA

⁷ Department of Physics and Astronomy, University of Leicester, Leicester LE1 7RH, UK

⁸ Astrophysics Group, School of Physical and Geographical Sciences, Keele University, Keele, Staffordshire, UK

Received 2009 January 2; accepted 2009 August 6; published 2009 September 3

ABSTRACT

We investigate the short-term variability properties and the power spectral density (PSD) of the broad-line radio galaxy (BLRG) 3C 390.3 using observations made by XMM-Newton, RXTE, and Suzaku on several occasions between 2004 October and 2006 December. The main aim of this work is to derive model-independent constraints on the origin of the X-ray emission and on the nature of the central engine in 3C 390.3. On timescales of the order of few hours, probed by uninterrupted XMM-Newton light curves, the flux of 3C 390.3 is consistent with being constant in all energy bands. On longer timescales, probed by the 2-day RXTE and Suzaku observations, the flux variability becomes significant. The latter observation confirms that the spectral variability behavior of 3C 390.3 is consistent with the spectral evolution observed in (radio-quiet) Seyfert galaxies: the spectrum softens as the source brightens. The correlated variability between soft and hard X-rays, observed during the Suzaku exposure and between the two XMM-Newton pointings, taken 1 week apart, argues against scenarios characterized by the presence of two distinct variable components in the 0.5-10 keV X-ray band. A detailed PSD analysis carried out over five decades in frequency suggests the presence of a break at $T_{br} = 43^{+34}_{-25}$ days at a 92% confidence level. This is the second tentative detection of a PSD break in a radio-loud, non-jet dominated active galactic nucleus (AGN), after the BLRG 3C 120, and appears to be in general agreement with the relation between $T_{\rm br}$, $M_{\rm BH}$, and $L_{\rm bol}$, followed by Seyfert galaxies. Our results indicate that the X-ray variability properties of 3C 390.3 are broadly consistent with those of radio-quiet AGN, suggesting that the X-ray emission mechanism in 3C 390.3 is similar to that of nearby Seyfert galaxies without any significant contribution from a jet component.

Key words: galaxies: active - galaxies: nuclei - X-rays: galaxies

Online-only material: color figures

1. INTRODUCTION

Relativistic bipolar outflows, generally emitting most of their energy in the radio range, are one of the most dramatic manifestations of the presence of supermassive black holes in active galactic nuclei (AGNs). Although it is widely accepted that these ejections are closely related to the accretion process onto the central black hole, the details of this link are still unknown.

A promising approach for tackling this problem is to investigate the X-ray properties of AGN with jets (generally called radio-loud AGN) and carry out a systematic comparison with their radio-quiet counterparts, the Seyfert galaxies. Unlike optical and UV light, X-rays are not significantly attenuated and are less affected by dilution from the host galaxy and are thought to be produced in the inner most regions of the accretion flow, thus may provide the most direct view of the central engine.

Broad-line radio galaxies (hereafter BLRGs) are one of the best classes of radio-loud AGNs for this comparative analysis; they have optical and UV spectral properties similar to Seyfert galaxies, but they also host large-scale radio jets that are absent in their radio-quiet counterparts. Past X-ray spectroscopic studies, employing ASCA, RXTE, and BeppoSAX data, have shown that BLRGs have weak Fe K α lines and weak or absent Compton reflection humps at energies $\gtrsim 10$ keV, a hallmark of Seyfert 1 galaxies (e.g., Woźniak et al. 1998; Sambruna et al. 1999; Eracleous et al. 2000; Zdziarski & Grandi 2001; Grandi et al. 2006). These findings have been confirmed by recent studies that made use of higher quality spectra provided by *Chandra* and *XMM-Newton* (e.g., Ballantyne et al. 2004, Ballantyne 2005; Ogle et al. 2004; Lewis et al. 2005; Gliozzi et al. 2007). Indeed, the weakness of the Fe K α line and the Compton reflection continuum are very important observational clues, since they represent a major difference between radio-loud and radio-quiet AGNs. However, the origin of this difference is still debated (see Gliozzi et al. 2007 for a detailed discussion on the competing models).

The importance of temporal studies lies in that they may provide model-independent information that complements the findings from spectral studies and possibly breaks the spectral degeneracy. Indeed, the similarity of the temporal and spectral variability properties of two BLRGs (including 3C 390.3) with those of Seyfert galaxies, led us to rule out a jet origin for the bulk of X-ray flux from these BLRGs and provided tight constraints on the jet contribution (Gliozzi et al. 2003b).

Past temporal studies indicate that the flux variability of 3C 390.3 is associated with spectral variability, in the sense that

⁹ Also at Center for Gravitational Wave Physics, The Pennsylvania State University, University Park, PA 16802, USA.

the spectrum softens as the flux increases. The presence of flux and spectral variability has been separately observed in the 2-15 keV band with RXTE (Gliozzi et al. 2003b, 2006), in the 2-10 keV energy band using ASCA and Ginga (Leighly et al. 1997), as well as at softer energies (0.1–2.4 keV) with ROSAT (Leighly et al. 1997). Importantly, all the above results, are based either on long-term (months to years) monitoring campaigns or on multiple observations spanning several years, but none addresses specifically the short-term variability. Although in the literature there are several studies based on individual observations of 3C 390.3 with different X-ray satellites (e.g., EXOSAT from Inda et al. 1994; ASCA from Eracleous et al. 1996; or BeppoSAX from Grandi et al. 1999), they all are focused on the spectral analysis and the temporal analysis is generally limited to few sentences indicating that the flux appears to be constant on timescales shorter than 1 day.

The apparent absence of short-term variability in 3C 390.3 seems to be in line with scaling relations inferred from power spectral density (PSD) studies of radio-quiet AGNs (see McHardy et al. 2006 and references therein). However, the lack of short-term variability in this AGN has never been tested by a satellite with the capabilities of *XMM-Newton*, which combines a very high throughput with highly elliptical orbits. These capabilities produce high quality uninterrupted light curves that have revealed the presence of short-term variability also in unexpected AGN classes, such as LINERs or low-luminosity Seyfert galaxies (e.g., Gliozzi et al. 2003a, 2008; Papadakis et al. 2008).

Taking advantage of the unique capabilities of XMM-Newton, we perform for the first time a thorough analysis of the temporal and spectral variability of 3C 390.3 on timescales of a few hours. This study is complemented by a similar analysis on timescales of 2 days, based on high quality variability data from Suzaku and from RXTE. These data are then combined with long-term *RXTE* monitoring data to produce the first PSD of 3C 390.3. A detailed analysis of the time-averaged spectral properties is reported in a companion paper by Sambruna et al. (2009) and can be summarized as follows: (1) the broadband 0.4-100 keV continuum is well described by a power law with $\Gamma = 1.6$ and a high-energy cutoff at $E_{\text{cutoff}} = 175 \text{ keV}$; (2) reprocessing by two different "reflectors" (one neutral with R = 0.5 and the other ionized with $\xi \simeq 2700$) is required; (3) the Fe K α line profile is well fitted by a narrow component centered at 6.4 keV plus a broad component at 6.6 keV (apparently from He-like Fe).

This paper is organized as follows. In Section 2, we describe the observations and data reduction. The short timescale (from few hours to 2 days) flux and spectral variability analyses are reported in Section 3 and Section 4, respectively. In Section 5, we perform a PSD analysis combining the short timescale light curves from this paper with long timescale light curves from past RXTE monitoring campaigns. In Section 6, we discuss the main results; and finally in Section 7, we summarize the main conclusions. Hereafter, we adopt $H_0 = 71 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{\Lambda} = 0.73$, and $\Omega_{M} = 0.27$ (Bennet et al. 2003); with the assumed cosmological parameters, the luminosity distance of 3C 390.3 (z = 0.056) is 247 Mpc. For the temporal analysis, we make use of the χ^2 test to assess the significance of the variability and consider a light curve significantly variable if the probability of the null hypothesis (i.e., the source being constant) is less than 1%.

2. OBSERVATIONS AND DATA REDUCTION

We observed 3C 390.3 with *XMM-Newton* on 2004 October 10 and 17 for 50 ks and 20 ks, respectively. All of the EPIC

cameras (Strüder et al. 2001; Turner et al. 2001) were operated in small window mode to prevent photon pile-up, and with medium filters, due to the presence of bright nearby sources in the field of view. The data reduction has been performed following the standard procedure with the *XMM-Newton* Science Analysis Software (SAS) 7.1; a detailed description is given in Sambruna et al. (2009).

In order to cover the harder part of the X-ray band, up to 40 keV, 3C 390.3 was also observed by *RXTE*. Unfortunately, the *RXTE* coverage, which was intended to be simultaneous to the *XMM-Newton* observations, was carried out on 2005 January 12 and 13, i.e., nearly two months after the *XMM-Newton* observations, due to scheduling problems. Because of the well known long-term temporal and spectral variability of 3C 390.3, the *RXTE* data cannot be safely combined with the EPIC data for a broadband spectral analysis. Nevertheless, the *RXTE* observation, which has a total exposure of 80 ks spanning a 2-day interval, is useful for investigating the variability on intermediate timescales at higher energies.

The RXTE observations (both the new observations presented here and the older observations used for the PSD analysis) were carried out with the Proportional Counter Array (PCA; Jahoda et al. 1996), and the High-Energy X-Ray Timing Experiment (HEXTE; Rotschild et al. 1998) instruments. Here we will consider only PCA data, because the signal-to-noise ratio (S/N) of the HEXTE data is too low for a meaningful analysis. The PCA data were screened according to the following acceptance criteria: the satellite was out of the South Atlantic Anomaly (SAA) for at least 30 minutes, the Earth elevation angle was $\ge 10^\circ$, the offset from the nominal optical position was \leq 0.02, and the parameter ELECTRON-2 was \leq 0.1. The last criterion excludes data with high particle background rates in the Proportional Counter Units (PCUs). The PCA background light curves were determined using the L7-240 model developed at the *RXTE* Guest Observer Facility (GOF). This model is implemented by the program pcabackest v.2.1b and is applicable to "faint" sources, i.e., those with count rates $< 40 \text{ s}^{-1} \text{ PCU}^{-1}$. All the above tasks were carried out with the help of the REX script provided by the RXTE GOF, which calls the relevant programs from the FTOOLS v.6.5 software package and also produces response matrices and effective area curves for the specific time of the observation. Data were initially extracted with 16 s time resolution and then rebinned to different bin widths for different applications. The short-term temporal analysis is restricted to PCA, STANDARD-2 mode, 2-15 keV, and Layer 1 data, because that is where the PCA is best calibrated and most sensitive. For the PSD study, we restricted the analysis to the 2–10 keV energy band, since this is the common energy range for RXTE, Suzaku, and XMM-Newton. PCUs 0 and 2 were turned on throughout the monitoring campaign. However, since the propane layer on PCU0 was damaged in May 2000, causing a systematic increase of the background, we conservatively use only PCU2 for our analysis. All quoted count rates are therefore for one PCU.

Suzaku observed 3C 390.3 on 2006 December 14–16 for a total exposure time of 100 ks. We used the cleaned event files obtained from version 2 of the *Suzaku* pipeline processing, according to standard screening criteria. The XIS0, XIS1, and XIS3 source light curves were extracted from circular regions of radius 2.9 centered on the source and combined in order to increase the S/N; background light curves were extracted from four circular regions offset from the source. For the HXD-PIN data reduction and analysis, we followed the latest *Suzaku* data



Figure 1. Left: XMM-Newton EPIC pn light curves of the soft (0.5–2 keV) and hard count rate (2–10 keV) on 2004 October 10. Time bins of 1000 s have been used. Right: XMM-Newton EPIC light curves on 2004 October 17.

Table 1

(A color version of this figure is available in the online journal.)

Flux Variability Properties									
Date	Instrument (Satellite)	$F_{2-10 \text{ keV}}$	0.5–2 keV	Variability	2–10 keV Variability				
(yyyy/mm/dd)		$(\mathrm{erg}\mathrm{cm}^{-2}\mathrm{s}^{-1})$	χ^2/dof	P_{χ}^2	χ^2/dof	P_{χ}^2			
2004/10/10	EPIC pn (XMM)	3.9×10^{-11}	41.08/37	0.30	47.20/37	0.12			
2004/10/17	EPIC pn (XMM)	3.4×10^{-11}	20.01/21	0.52	19.07/21	0.58			
2005/01/12, 13	PCA (RXTE)	$5.5 imes 10^{-11}$			58.37/24	1.1×10^{-4}			
2006/12/14-16	XIS (Suzaku)	3.1×10^{-11}	105.24/29	$<1\times10^{-6}$	42.97/29	4.6×10^{-2}			

reduction guide, and used the rev2 data, which include all the four cluster units and the best background available, model D, which has a systematic uncertainty of $\pm 1.3\%$ at 1σ level.¹⁰ See Sambruna et al. (2009) for a more detailed description of the *Suzaku* data reduction.

3. SHORT TIMESCALE FLUX VARIABILITY

3.1. XMM-Newton

Figures 1(a) and (b) show the EPIC pn light curves of the soft (0.5–2 keV; top panels) and hard (2–10 keV; bottom panels) count rate on 2004 October 10 and October 17. Hereafter, for the sake of simplicity, we will refer to the two XMM-Newton pointings as observations A and B, respectively. The average 2-10 keV fluxes during these two observations were 3.9×10^{-11} and 3.4×10^{-11} erg cm⁻² s⁻¹, respectively. In order to allow a direct comparison between observations A and B, we have kept the same vertical scales in Figures 1(a) and (b). In this way, the significant decrease in count rate is easily discernible. Specifically, between the first and the second exposure, the EPIC pn average count rate decreases from $10.99 \pm 0.01 \text{ s}^{-1}$ to 9.58 ± 0.01 s⁻¹ in the 0.5–10 keV energy band. A visual inspection of Figure 1 suggests that, despite the presence of some small-amplitude variations during observation A, within each individual exposure the soft and hard count rates do not vary significantly. The lack of short-term variability is formally confirmed by a χ^2 test and by the fractional variability analysis, whose results are reported in Tables 1 and 2, respectively.

3.2. RXTE

RXTE observed 3C 390.3 on 2005, January 12 and 13, when the source was in a very high brightness state: the average 2-10 keV flux was 5.5×10^{-11} erg cm⁻² s⁻¹ with a corresponding luminosity of 4.1×10^{44} erg s⁻¹, which is slightly higher than the maximum value registered in the two-year RXTE monitoring campaign (Gliozzi et al. 2006). The left panel of Figure 2 shows the light curves in the 2–6 keV (top panel; $P_{\chi^2} = 1.5 \times 10^{-3}$), 2–10 keV (middle panel; $P_{\chi^2} = 1.1 \times 10^{-4}$), and 6–15 keV (bottom panel; $P_{y^2} = 4.9 \times 10^{-2}$) energy bands, respectively. Since the RXTE PCA is best calibrated in the 2-15 keV energy band, a direct comparison with the soft EPIC pn light curve described above cannot be performed. Nevertheless, RXTE allows a direct comparison in the 2-10 keV range and also the investigation of the harder X-rays up to 15 keV. On timescales of the order of 2 days, the source count rate is clearly variable in the 2-10 keV energy band (Table 1). The fact that the harder band is only marginally variable (it is variable at a 95% confidence level) can be ascribed to the lower data quality at higher energies.

3.3. Suzaku

Suzaku observed 3C 390.3 on 2006 December 14–16, when the source was in a brightness state similar to that observed by *XMM-Newton* two years earlier ($F_{2-10 \text{ keV}} = 3.1 \times 10^{-11}$ erg cm⁻² s⁻¹). The XIS 0.5–2 keV and 2–10 keV light curves are shown in the top and middle panels of Figure 2(b). Just as with the *RXTE* PCA light curves, both XIS light curves show significant (and correlated) variability on timescales of

¹⁰ ftp://legacy.gsfc.nasa.gov/suzaku/doc/hxd/suzakumemo-2008-03.pdf



Figure 2. Left: *RXTE* PCA light curves in the 2–6 keV, 2–10 keV, and 6–15 keV energy bands. Time bins of 5760 s ($\sim 1 RXTE$ orbit) have been used. Right: *Suzaku* XIS013 light curves in the 0.5–2 keV and 2–10 keV energy bands (top and middle panels). Time bins of 5760 s ($\sim 1 Suzaku$ orbit) have been used. The bottom panel shows the *Suzaku* PIN light curve in the 15–40 keV energy range; time bins are two satellites orbit. Given the uncertainty on the PIN background, for completeness, we have plotted both 1 σ (solid line) and 3 σ (dotted lines) error bars.

(A color version of this figure is available in the online journal.)

Spectral Variability Properties									
Date	Instrument (Satellite)	HR Varia	bility	$F_{\rm var, soft}{}^{\rm a}$	F _{var,hard} ^b				
(yyyy/mm/dd)		χ^2/dof	P_{χ}^2						
2004/10/10	EPIC pn (XMM)	38.92/37	0.38	$(3.6 \pm 4.3) \times 10^{-3}$	$(9.6 \pm 5.2) \times 10^{-3}$				
2004/10/17	EPIC pn (XMM)	21.61/21	0.42						
2005/01/12, 13	PCA (RXTE)	24.22/24	0.45	$(9.3 \pm 5.2) \times 10^{-3}$	$(8.4 \pm 5.9) \times 10^{-3}$				
2006/12/14-16	XIS (Suzaku)	37.7/29	0.13	$(1.9 \pm 0.2) \times 10^{-2}$	$(1.1 \pm 0.3) \times 10^{-2}$				

Notes.

^a The soft band is 0.5–2 keV for XMM-Newton and Suzaku, whereas for RXTE it is 2–6 keV.

^b Similarly, the hard band corresponds to 2–10 keV for XMM-Newton and Suzaku, and to 6–15 keV for RXTE.

2 days, confirmed by a χ^2 test whose results are reported in Table 1.

The HXD PIN instrument aboard *Suzaku* offers the opportunity to investigate the variability of 3C 390.3 at harder X-ray energies for the first time. Using the latest background file, we extracted light curves in the 15–40 keV and 40–70 keV ranges; no variability was detected in the harder energy band $(P_{\chi^2} = 0.47)$, while significant variability $(P_{\chi^2} = 1 \times 10^{-4})$ seems to be present in the 15–40 keV energy band, which is shown in the bottom panel of Figure 2(b). However, if we increase the PIN background level by applying systematic corrections at 1, 2, and 3σ levels, we obtain P_{χ^2} values of 1.6×10^{-2} , 0.16, and 0.52, respectively. *Suzaku* observations thus indicate that there is significant variability in the energy range 0.5–10 keV, while above 15 keV the uncertainties on the HXD background prevent us from drawing strong conclusions.

In summary, on short timescales (few hours) the flux of 3C 390.3 is consistent with the hypothesis of being constant in all

energy bands. On longer timescales (i.e., considering the two *XMM-Newton* observations together or the 2-day *RXTE* and *Suzaku* coverage), the flux variability becomes significant.

4. SHORT TIMESCALE SPECTRAL VARIABILITY

In order to study the spectral variability of 3C 390.3, we use simple methods such as the variation of the hardness ratio with time and with total count rate, and the fractional variability in different energy bands. These can provide useful information without any a priori assumption about the shape of the X-ray continuum. Thus, the results from the study of these plots can be considered as "model independent."

To investigate the presence of spectral variability, we first apply a χ^2 test to the time series of the hardness ratio HR = h/s, where h = 2-10 keV and s = 0.5-2 keV for *XMM-Newton* and *Suzaku*, whereas for *RXTE* h = 6-15 keV and s = 2-6 keV. The



Figure 3. Left: *XMM-Newton* hardness ratio (2–10 keV)/(0.5–2 keV) plotted versus the total count rate. The large black circles indicate the average values during the two observations; the error bar is smaller than the symbols. The dashed line indicates the best linear fit. Middle: *RXTE* hardness ratio (6–15 keV)/(2–6 keV) plotted versus the total count rate. The dashed line indicates the best linear fit. Right: *Suzaku* XIS03 hardness ratio (2–10 keV)/(0.5–2 keV) plotted versus the total count rate. The dashed line indicates the best linear fit. Right: *Suzaku* XIS03 hardness ratio (2–10 keV)/(0.5–2 keV) plotted versus the total count rate. To guide the eye, binned values (large black circles) have been plotted over non-binned values. The dashed line indicates the best linear fit: $y = (1.11 \pm 0.13) - (0.06 \pm 0.02)x$. (A color version of this figure is available in the online journal.)

results of this test are reported in Table 2 and suggest that there is no significant spectral variability on timescales of a few hours, while on a timescale of 2 days (*Suzaku* observation) marginally significant spectral variability seems to be present. It is worth noting that even between *XMM-Newton* observations A and B only marginally significant spectral variability seems to occur: the average *HR* increases from 0.349 ± 0.001 to 0.354 ± 0.002 , which is a 2σ effect. This is a direct consequence of the fact that the soft and hard count rates vary by the same amount: they both decrease by ~12% in one week (see Figure 1).

Spectral variability can be further investigated by plotting HR versus the total count rate. Figure 3 shows the HRcount rate plots for XMM-Newton (left panel), RXTE (middle panel), and Suzaku (right panel), respectively. The superimposed dashed lines represent the best-fitting straight lines, which were obtained using the routine fitexy (Press et al. 1997) that accounts for the errors not only on the y-axis but along the x-axis as well. Specifically, this analysis yielded: $y = (0.38 \pm$ $(0.02) - (0.003 \pm 0.002)x$ for XMM-Newton, $y = (1.23 \pm 0.41) - 0.02$ $(0.01\pm0.07)x$ for *RXTE*, and $y = (1.11\pm0.13) - (0.06\pm0.02)x$ for Suzaku, respectively. In summary, while XMM-Newton and RXTE observations show very flat negative slopes that are consistent with the hypothesis of constancy, Suzaku shows a negative trend (i.e., a steepening of the spectrum with increasing source flux) that is significant at a 3σ level. This result is confirmed by a non-parametric Spearman test that yields a rank correlation value of -0.44 and a corresponding chance probability of 1.6×10^{-2} .

Another simple way to quantify the spectral variability of 3C 390.3, without considering the time ordering of the values in the light curves, is based on the fractional variability parameter F_{var} . This is a commonly used measure of the intrinsic variability amplitude relative to the mean count rate, corrected for the effect of random errors, i.e.,

$$F_{\rm var} = \frac{(\sigma^2 - \Delta^2)^{1/2}}{\langle r \rangle},\tag{1}$$

where σ^2 is the variance, $\langle r \rangle$ the unweighted mean count rate, and Δ^2 the mean square value of the uncertainty associated with each individual count rate. The error on F_{var} , reported in Table 2, has been estimated following Vaughan et al. (2003). For all individual observations, we computed F_{var} on the soft and hard energy bands (as defined above), since the relatively short observations and the moderately low count rate do not allow this kind of analysis on multiple narrow energy bands. The results, summarized in Table 2, indicate that the variability amplitudes measured in the two energy bands are consistent with each other within the uncertainties. During the *Suzaku* observation there is marginal evidence ($\sim 2.2\sigma$) that the soft band is more variable than the hard one.

5. POWER SPECTRAL DENSITY ANALYSIS

To estimate the power spectrum of the source in the 2–10 keV energy band, we used: (1) the 1999 and 2000 *RXTE* light curve, using a 3-day bin size ("rxte-long" light curve, hereafter); (2) the 1996, two-month long, *RXTE* light curve, using a 1-day bin size ("rxte-medium" light curve, hereafter); (3) the 2005, 2-day long, *RXTE* light curve ("rxte-short" light curve, hereafter), (4) the 2006, 2-day long, *Suzaku* XIS light curve; and (5) the 2004 October 10 and 17, *XMM-Newton* EPIC pn light curves. We used a 5760 s binning for the rxte-short and XIS light curves, and a 200 s binning for the *XMM-Newton* light curves. The 2004 October 10, *XMM-Newton* light curve was split in two parts to exclude the ~ 2 hr period of enhanced background activity, which was detected ~7 hr after the start of the observation.

All light curves are evenly sampled, with a few missing points (about 5%-10% of the total number of points). These missing points are randomly distributed over each light curve, and we accounted for them using a linear interpolation between the two bins adjacent to the gaps, adding the appropriate Poisson noise in each case.

We used Equation (1) in Papadakis & Lawrence (1993) to compute the periodograms of each light curve, after normalizing them to their mean. The expected Poisson noise power level for the rxte-long and rxte-medium light curves is comparable; and for this reason, we combined their periodograms in one file and sorted them in order of decreasing frequency (the "lowfrequency" periodogram). This combined periodogram can be used for the estimation of the long and medium timescale power spectrum, from a frequency $\sim 1/(\text{few days})$, down to \sim 1/(two years). The rxte-short and XIS light curves also have comparable Poisson noise power level, and we therefore combined their periodograms forming the "medium-frequency" periodogram to estimate the power spectrum at higher frequencies of the order of $\sim 1/(a$ few hours). Finally, we also combined the XMM-Newton periodograms, in an attempt to detect a source signal at even higher frequencies (the "high frequency" periodogram).



Figure 4. Power density spectra of 3C 390.3 based on *RXTE*, *Suzaku* (open squares), and *XMM-Newton* light curves (filled triangles) described in the text. The dashed lines indicate the best power-law model fit (left panel) and the best broken power-law model fit (right panel) to the full band PSD. Solid lines indicate the best-fit models when the Poisson noise power level is also taken into account. Clearly, the intrinsic power level is very low above 10^{-4} Hz, hence the observed PSD in the *XMM* band is flat, and consistent with the predictions of a purely Poisson noise power spectrum (indicated by the solid line at the highest frequency part of the PSD). (A color version of this figure is available in the online journal.)

Following Papadakis & Lawrence (1993), we binned the three periodograms in log–log space, using bins of size 20, and their Equations (18), (19), and (20) (for the estimation of the error of the resulting binned PSD points). Our results are plotted in Figure 4. Filled triangles indicate the high frequency PSD, estimated using the high-frequency, *XMM-Newton* periodogram. The solid line indicates the expected Poisson power level. Clearly, at frequencies higher than 10^{-4} Hz, we cannot detect any intrinsic variations. The open squares in the same figure indicate the low and medium frequency PSD estimates. At low frequencies, the source PSD shows the familiar "red-noise" power spectral shape.

We fitted the low-frequency PSD with a simple power-law model of the form $P(f) \propto f^{-a}$, taking into account the different Poisson noise power levels for the medium-frequency PSD estimate (indicated by the open square around $f \sim 10^{-4.5}$ Hz) and the low-frequency PSD (open squares at frequencies lower than $f \sim 10^{-5.7}$ Hz). We have also accounted for aliasing effects, as they can be analytically estimated for any given PSD model shape, following the analytical expressions in Section 7.1.1 of Priestley (1989). The model describes reasonably well the PSD: the best-fit slope is $a = 2.2 \pm 0.2$ (errors correspond to 68% confidence limits for two interesting parameters), $\chi^2 = 12.8/6$ degrees of freedom (dof), probability of null hypothesis, P_{null} , of 4.6%. The dashed line in the left panel of Figure 4 indicates the best-fit power-law model; and the thick solid black line, the best-fit model after taking into account the different Poisson noise power levels for the lowand medium-frequency power spectra (best-fit residuals are shown in the bottom panel of the same figure). The best-fit slope is consistent with the high-frequency PSD slope detected in radio-quiet Seyfert galaxies. The steepness of the intrinsic power spectrum can explain the lack of detection of intrinsic source variations in the XMM-Newton light curves: the expected amplitude at the highest frequencies we can probe is much smaller than the amplitude caused by noise in the XMM-Newton light curves.

We also tried to fit the PSD with a broken power-law model of the form: $P(f) \propto (f/f_{\rm br})^{-b}$, where $f < f_{\rm br}$ and $P(f) \propto (f/f_{\rm br})^{-a}$, at higher frequencies; $f_{\rm br}$ is the so called "break-frequency." Such a model provides a good fit to the PSD

of many Seyfert galaxies with $a \sim 2$ and $b \sim 1$ (see, e.g., Uttley et al. 2002; Papadakis et al. 2002a; Markowitz et al. 2003). Since the 3C 390.3 PSD does not show a clear slope change at low frequencies, we kept b fixed at 1, which is the typical value found in Seyfert galaxies. Note that, in case b is left free to vary, all parameters are very poorly constrained, due to paucity of data points at low frequencies. The best-fit parameters are as follows: $a = 2.4 \pm 0.3$, $f_{\rm br} = 2.7^{+3.6}_{-1.2} \times 10^{-7}$ Hz (68% errors for three interesting parameters: high-frequency slope, break frequency, and normalization), $\chi^2 = 6.6/5$ dof, $P_{\rm null} =$ 25.2%. The resulting best-fit model is shown in the right panel of Figure 4 (the symbols are the same as in the left panel), and indicates that it fits the PSD very well. According to an *F*-test ($F_{\text{stat}} = 4.7, P_F = 0.082$), the broken power-law model provides an improvement of the goodness of fit at a confidence level of 92%, compared to the power-law model. At the same time, the PSD plotted in the right panel of Figure 4 indicates that the detection of this break frequency in the power spectrum of the source is determined mainly by the lowest frequency point in the PSD. The points indicated by the crosses in the same panel, show the lowest frequency part of the power spectrum. They correspond to the 20 lowest frequency periodogram ordinates, and were estimated using bins of size 5 and 10, for the higher frequency point. These points indicate that the low frequency end of the PSD does follow a slope which is flatter than the slope of the high frequency PSD. Nevertheless, to be conservative, we consider the detection of a break frequency in the PSD of 3C 390.3 as tentative.

6. DISCUSSION

In order to put our results in perspective and better understand their implications, it is important to have in mind the values of the fundamental parameters that characterize the accretion process in 3C 390.3, namely the black hole mass, $M_{\rm BH}$, and the accretion rate in Eddington units, \dot{m} . To be consistent with the companion paper from Sambruna et al. (2009), in the following we assume $M_{\rm BH} = (5 \pm 1) \times 10^8 M_{\odot}$, which is based on the velocity dispersion presented in Nelson et al. (2004) and is reported by Lewis & Eracleous (2006). However, for completeness and given the large uncertainties, we also consider the value obtained via reverberation mapping $M_{\rm BH} =$ $(2.87 \pm 0.64) \times 10^8 M_{\odot}$ (Peterson et al. 2004). Once $M_{\rm BH}$ is determined, \dot{m} readily follows, by determining the bolometric luminosity, L_{bol}, and dividing it by the Eddington luminosity, $L_{\rm Edd} = 1.3 \times 10^{38} \, (M_{\rm BH}/M_{\odot}) \, {\rm erg \ s^{-1}}. L_{\rm bol}$ can be obtained by integrating the broadband spectral energy distribution (SED) of 3C 390.3. A detailed compilation of broadband data of 3C 390.3 ranging from the radio to the hard X-rays has been presented by Sambruna et al. (2009), yielding a bolometric luminosity in the range $1-4 \times 10^{45}$ erg s⁻¹ (this luminosity range is a direct consequence of the long-term intrinsic variability of 3C 390.3). Combining these values with $M_{\rm BH}$, we obtained an Eddington ratio ranging between 0.01 and 0.07 (0.03-0.1 for $M_{\rm BH} = 2.87 \times 10^8 M_{\odot}$), which is consistent with the lower end of the accretion rate values typically inferred in Seyfert 1 galaxies (see Vasudevan & Fabian 2009 for a recent compilation). For a source with powerful radio jets as 3C 390.3, it is also important to know the inclination angle, since beamed emission can affect any energy band including the X-rays. Based on radio data, the jet inclination angle in 3C 390.3 lies between 30° and 35° and the estimated jet velocity is $\beta = v/c > 0.96$ (Giovannini et al. 2001). This translates into bulk Lorentz factors in the range $\Gamma = 3.6-7.1$, which in turn yield beaming factors in the range $\delta \simeq 0.7$ –1.7, implying that the jet emission can be either debeamed or beamed but in a moderate way.

The main aim of this work is to utilize the results from the short-term variability and PSD analyses to derive modelindependent constraints on the central engine of 3C 390.3 and possibly on radio-loud AGN, in general. More specifically, our findings can be used to evaluate the competing models proposed to explain the weaker X-ray reprocessing features in BLRGs, namely dilution from the base of the jet, radiatively inefficient flow (RIAF) in the central region, or the presence of a highly ionized reflector.

6.1. Flux Variability

Previous X-ray monitoring campaigns have shown that 3C 390.3 is highly variable on timescales ranging from several days to months. For example, using a nine-month light curve of 3C 390.3 from the *ROSAT* HRI (which probes the 0.1–2.4 keV energy band), Leighly & O'Brien (1997) demonstrated that the soft X-rays are highly variable, displaying large flares with quiescent periods in between, a behavior that implies a non-linear nature for the variability process. Similarly, two long-term monitoring campaigns with *RXTE*, spanning respectively three months and two years, revealed that the source is also highly variable at higher X-ray energies with F_{var} ranging between 20% and 30% (Gliozzi et al. 2003b; 2006). However, since both *ROSAT* and *RXTE* are low-Earth orbit satellites the light curves were continuously interrupted, hampering the study of variability on timescales of hours.

XMM-Newton, with its highly elliptical orbit, has allowed the study of the short-term variability of 3C 390.3 for the first time. The EPIC light curves showed a lack of any significant short-term variability, despite the fact that the source was caught in a fairly high flux state. The lack of short-term variability lends support to the scenario where the jet does not play an important role in the X-ray emission of 3C 390.3 from two different points of view. First, it confirms on firmer statistical ground that 3C 390.3 follows the scaling relations typical of radio-quiet AGN that predict the short-term variability to be negligible in AGN with large $M_{\rm BH}$. Second, it reveals a marked difference with respect to the typical behavior observed in jet-dominated

sources, which show strong variability down to timescales of few minutes (e.g., Cui 2004). According to the current blazar paradigm, the observed short-term variability at high energies is a direct consequence of the small size of the emitting region and the observed variability timescales are further shortened by beaming effects: $t_{obs} = t_{rest}/\delta$. As a consequence, the lack of short-term variability in 3C 390.3 suggests that the X-ray emitting region is extended and that the beaming effects, if present, are negligible in this energy band.

The 2-day long observations carried out with *RXTE* and *Suzaku* confirm that on timescales longer than a few hours, the X-ray emission of 3C 390.3 varies significantly. Additionally, the analysis of *Suzaku* HXD-PIN data suggests a possible detection of low-amplitude flux changes up to 40 keV. However, the current uncertainties on the HXD background prevent us from drawing strong conclusions.

Important results from the temporal study can also be derived by the PSD analysis, which is the best developed timing technique and the one commonly used for investigating the time variability properties of Galactic black hole systems (GBHs) and AGNs. Indeed, recent detailed PSD studies have been used to strengthen the link between GBHs and AGNs (e.g., Uttley et al. 2002; Markowitz et al. 2003, McHardy et al. 2004).

The comparison of the PSD frequency break $f_{\rm br}$ (indicative of a characteristic timescale of the BH system) in GBHs and AGNs has provided an alternative way to determine the BH mass in AGNs. McHardy et al. (2006) proposed that, in Seyfert galaxies, the break timescale, $T_{\rm br} = 1/f_{\rm br}$, scales with $M_{\rm BH}$ and $L_{\rm bol}$, following the relationship: $\log(T_{\rm br}) =$ 2.1 log($M_{\rm BH}$) – 0.98 log($L_{\rm bol}$) – 2.32, where $M_{\rm BH}$ is measured in units of 10⁶ M_{\odot} , and $L_{\rm bol}$ in units of 10⁴⁴ erg s⁻¹. Using in the above formula $M_{\rm BH} = 500 \times 10^6 M_{\odot}$ and $L_{\rm bol} = (10-40) \times$ 10^{44} erg s⁻¹, obtained from the direct integration of the SED, we obtain that $T_{\rm br}$ ranges between 60 and 234 days (20– 66 days for $M_{\rm BH} = 287 \times 10^6 M_{\odot}$). Interestingly, this result is consistent with the temporal break inferred from our PSD analysis: $T_{\rm br} = 43^{+34}_{-25}$ days.

McHardy and collaborators (2006) also found a tight correlation between $T_{\rm br}$ and the full width at half-maximum (FWHM) of the H_{β} line: $\log(T_{\rm br}) = 4.20^{+0.71}_{-0.56} \times \log(FWHM(H_{\beta})) - 14.43$. Taking into account the uncertainties on the slope, and using the value derived from our PSD analysis, $T_{\rm br} = 43$ days, the predicted FWHM(H_{β}) for 3C 390.3 ranges between ~2000 and 26,000 km s⁻¹, which is fully consistent with the value of 12,700 km s⁻¹ derived from a time-averaged spectrum over several years (Sergeev et al. 2002).

The agreement between the predicted and the measured value of $T_{\rm br}$ is important in two respects. First, it lends further support to the detection of the break in the PSD of 3C 390.3. We do note that, owing to the relatively short monitoring baseline of 3C 390.3 (2 years as opposed to 5-10 years used in Seyfert studies), the detection of a break is significant only at the 92% confidence level. Nevertheless, we emphasize that this is the best estimate afforded by the current data and no improvement on the break determination will be possible in the years to come, since 3C 390.3 is not monitored by any X-ray satellite. Second, and perhaps more important, it suggests that the flux variability properties of this BLRG are indistinguishable from those of radio-quiet AGNs. In contrast, PSD studies of the most prominent blazars, Mrk 421, Mrk 501, and PKS 2155-304 (i.e., jet-dominated AGNs that have been observed with RXTE in long monitoring campaigns) suggest the presence of PSD breaks at frequencies that are nearly 2 orders of magnitude higher than the

tentative break found in 3C 390.3, i.e., at $f_{br,blazar} \simeq 10^{-5}$ Hz, or $T_{br,blazar} < 1$ day (Kataoka et al. 2001). As a consequence, the variability properties of 3C 390.3 appear to be incompatible with jet emission. On the other hand, the similarity between the variability properties of Seyfert galaxies and 3C 390.3 PSDs suggests that the X-ray variability process, and by extension the X-ray emission mechanism are similar between these two classes of object.

6.2. Spectral Variability

Previous studies, based on *RXTE* monitoring campaigns over periods ranging from a few months to two years, have revealed that 3C 390.3 shows correlated flux and spectral variations: the source spectrum softens as the source becomes brighter (Gliozzi et al. 2003b, 2006), which is the typical behavior observed in Seyfert galaxies (e.g., Papadakis et al. 2002b). Since these studies were performed in the 2–15 keV energy range, only our 2005 December *RXTE* observation can be formally compared with previous results. Unfortunately, due to the short duration of that observation and the limited range of the observed flux variations (compared to the long monitoring campaigns), no significant spectral variability is detected.

Thanks to the combination of XIS0, XIS1, and XIS3 data, and their relatively low background level, the *Suzaku* light curves have higher S/N than *RXTE*; and the *HR*–count rate plot clearly indicates that 3C 390.3 is consistent with the typical Seyfertlike behavior over a time interval of 2 days. It is worth noting that, unlike *RXTE* that covers only the hard X-ray range, *Suzaku* makes it possible to probe simultaneously soft (i.e., E < 2 keV) and hard energies. This is of crucial importance for BLRGs that have generally complex X-ray spectra, which cannot be fitted with a simple power law suggesting possible contributions from different physical components (see, e.g., Sambruna et al. 2009). For example, based on spectral variability results, Kataoka et al. (2007) proposed that the soft X-ray emission of 3C120 (another archetypal BLRG) was dominated by a jet.

In this context, the fact that the *Suzaku HR–ct* results are in full agreement with those obtained from an analogous analysis of long-term 2-15 keV RXTE data suggests that at softer energies also, the emission is dominated by the same Comptonized component as in Seyfert galaxies. This conclusion is further confirmed by the fact that soft (0.5–2 keV) and hard (2–10 keV) count rates appear to vary in concert (see Figure 2; right panel). This result does not exclude the possible presence of an additional component with constant flux (such as some contribution from reflection), but it rules out the presence of a variable component, such as the beamed emission from a jet.

Further support for the latter conclusion comes from the spectral variability analysis of *XMM-Newton* data: soft and hard count rate appears to vary roughly in concert not only within each single *XMM-Newton* observation but also between the two *XMM-Newton* pointings that are separated in time by one week and in flux by 12%. At this point, one might wonder why *XMM-Newton* with its superior throughput is unable to detect a statistical significant anticorrelation in the *HR*–*ct* plot at a confidence level higher than 2σ . The reason is simply that on short timescales (individual exposures) count rate and *HR* are constant, therefore all the information from one exposure virtually collapses to a single data point. As a consequence, the search for a negative trend in the *HR*–*ct* plot is based on two data points solely.

7. SUMMARY AND CONCLUSIONS

We have studied the short-term temporal and spectral variability properties of the BLRG 3C 390.3 using *XMM-Newton*, *RXTE*, and *Suzaku* observations carried out between 2004 October and 2006 December. Our new data were then combined with older *RXTE* data obtained from long-term monitoring campaigns to investigate the PSD in detail. The main findings of our analysis can be summarized as follows:

- 1. On short timescales (i.e., few hours, probed by uninterrupted *XMM-Newton* observations), the flux of 3C 390.3 in all energy bands is consistent with the hypothesis of being constant. On longer timescales (i.e., considering the two *XMM-Newton* observations together or the 2-day *RXTE* and *Suzaku* coverage), the flux variability becomes significant.
- 2. A detailed PSD analysis carried out over five decades in frequency suggests the presence of a break at $T_{\rm br} = 43^{+34}_{-25}$ days at a 92% confidence level. This is the second tentative detection of a PSD break in a radio-loud, non-jet dominated AGN, after the recent results of the BLRG 3C 120 from Marshall et al. (2009). Importantly, the timescale corresponding to the break frequency is in agreement with the relation between $T_{\rm br}$, $M_{\rm BH}$, and $L_{\rm bol}$ as well as with the $T_{\rm br}$ -FWHM(H_{β}) relationship, both of which are valid for Seyfert galaxies. Note that, while the relative brevity of the long-term *RXTE* campaign hampers the significance of the break detection around 40 days, the quality of the data is sufficient to rule out the presence of a break at shorter timescales, which is typically detected in PSDs of jet-dominated sources.
- 3. The 2-day long *Suzaku* observation indicates that 3C 390.3 shows the typical spectral evolution of Seyfert galaxies in the 0.5–10 keV energy range (the spectrum becomes softer as the source brightens). This confirms previous results, based on long *RXTE* monitoring campaigns, and expands them to different energy bands and to much shorter timescales.
- 4. The broadly coordinated variability in soft and hard X-rays during the 2-day *Suzaku* observation and between the two *XMM-Newton* pointings, taken one week apart, suggests a common physical origin for both energy bands, arguing against the presence of an additional variable component (i.e., a jet) emerging at softer energies.
- 5. The lack of short-term flux variability, the frequency break of the PSD, and the Seyfert-like spectral variability consistently argue against a scenario where a jet plays a significant role in the X-ray regime, confirming the results from the time-averaged spectral analysis (Sambruna et al. 2009).

In conclusion, all our results indicate that the flux variability properties of 3C 390.3 are broadly consistent with those of radioquiet AGNs, suggesting that the X-ray variability process and, by extension, the emission mechanism in 3C 390.3 is similar to that of Seyfert galaxies. This, in turn, suggests that the weaker reflection features observed in the X-ray spectrum of 3C 390.3 are not a result of dilution by jet emission, which is in agreement with the conclusions of the spectral analysis of Sambruna et al. (2009). If variability studies of other BLRGs show similar results, then jet dilution will be disfavored as a general explanation of the weak reflection features in all BLRGs as a class. Of course, the jet can still influence the observed X-ray properties of BLRGs by obscuring the central regions of the accretion disk or by beaming radiation away from the disk surface. The obscuration scenario has been suggested by Sambruna et al. (2009) and Larsson et al. (2008) to account for the lack of reflection from the inner accretion disk in 3C 390.3 and 4C+74.26, respectively. Unfortunately, this scenario would also block from view the region of the accretion flow where the jet is formed. Significant progress can be made by deep broadband observations of a large number of BLRGs so as to sample a wide variety of accretion disk geometries. The variability analysis presented here shows that, as long as the jet angle to line of sight is large enough, such an investigation will not be subject to the effects of jet dilution.

We acknowledge support from NASA through the *Suzaku* and *XMM-Newton* programs. I.E.P. acknowledges support by the EU grant MTKD-CT-2006-039965.

REFERENCES

- Ballantyne, D. R. 2005, MNRAS, 362, 1183
- Ballantyne, D. R., Fabian, A. C., & Iwasawa, K. 2004, MNRAS, 354, 839
- Bennet, C. L., et al. 2003, ApJS, 148, 1
- Cui, W. 2004, ApJ, 605, 662
- Eracleous, M., Halpern, J. P., & Livio, M. 1996, ApJ, 459, 89
- Eracleous, M., Sambrunna, R., & Mushotzky, R. F. 2000, ApJ, 537, 654
- Giovannini, G., Cotton, W. D., Feretti, L., Lara, L., & Venturi, T. 2001, ApJ, 552, 508
- Gliozzi, M., Foschini, L., Sambruna, R. M., & Tavecchio, F. 2008, A&A, 478, 723
- Gliozzi, M., Papadakis, I. E., & Raeth, C. 2006, A&A, 449, 969
- Gliozzi, M., Sambruna, R. M., & Brandt, W. N. 2003a, A&A, 408, 949
- Gliozzi, M., Sambruna, R. M., & Eracleous, M. 2003b, ApJ, 584, 176
- Gliozzi, M., et al. 2007, ApJ, 664, 88
- Grandi, P., Malaguti, G., & Fiocchi, M. 2006, ApJ, 642, 113
- Grandi, P., et al. 1999, A&A, 343, 33
- Inda, M., et al. 1994, ApJ, 420, 143

- Jahoda, K., et al. 1996, Proc. SPIE, 2808, 59
- Kataoka, J., et al. 2001, ApJ, 560, 659
- Kataoka, J., et al. 2007, PASJ, 59, 279
- Larsson, J., Fabian, A. C., Ballantyne, D. R., & Miniutti, G. 2008, MNRAS, 388, 1037
- Leighly, K. M., & O'Brien, P. T. 1997, ApJ, 481, L15
- Leighly, K. M., et al. 1997, ApJ, 483, 767
- Lewis, K. T., & Eracleous, M. 2006, ApJ, 642, 711
- Lewis, K. T., et al. 2005, ApJ, 622, 816 Markowitz, A., et al. 2003, ApJ, 593, 96
- Marshall, K., et al. 2009, ApJ, 696, 601
- McHardy, I., et al. 2009, MNRAS, 348, 783
- McHardy, I., et al. 2006, Nature, 444, 730
- Nelson, C. H., Green, R. F., Bower, G., Gebhardt, K., & Weistrop, D. 2004, ApJ, 615, 652
- Ogle, P. M., et al. 2004, ApJ, 618, 139
- Papadakis, I. E., Ioannou, Z., Brinkmann, W., & Xilouris, E. M. 2008, A&A, 490, 995
- Papadakis, I. E., & Lawrence, A. 1993, MNRAS, 261, 612
- Papadakis, I. E., et al. 2002a, A&A, 382, L1
- Papadakis, I. E., et al. 2002b, ApJ, 573, 92
- Peterson, B. M., et al. 2004, ApJ, 613, 682
- Press, W. H., Teukolsky, S. A., Vetterling, W. T., & Flannery, B. P. 1997, Numerical Recipes (Cambridge: Cambridge Univ. Press)
- Priestley, M. B. 1989, Spectral Analysis and Time Series (London: Academic Press)
- Rotschild, R. E., et al. 1998, ApJ, 496, 538
- Sambruna, R. M., Eracleous, M., & Mushotzky, R. 1999, ApJ, 526, 60
- Sambruna, R. M., et al. 2009, ApJ, 700, 1473
- Sergeev, S. G., Pronik, V. I., Peterson, B. M., Sergeeva, E. A., & Zheng, W. 2002, ApJ, 576, 660
- Strüder, L., et al. 2001, A&A, 365, L18
- Turner, M. J., et al. 2001, A&A, 365, L27
- Uttley, P., McHardy, I., & Papadakis, I. E. 2002, MNRAS, 332, 231
- Vasudevan, R. V., & Fabian, A. C. 2009, MNRAS, 392, 1124
- Vaughan, S., Edelson, R., Warwick, R. S., & Uttley, P. 2003, MNRAS, 345, 1271
- Woźniak, P. R., Zdziarski, A. A., Smith, D., Madejski, G. M., & Johnson, W. N. 1998, MNRAS, 299, 449
- Zdziarski, A. A., & Grandi, P. 2001, ApJ, 551, 186