POLLUTION OF SINGLE WHITE DWARFS BY ACCRETION OF MANY SMALL ASTEROIDS

M Jura

Department of Physics and Astronomy and Center for Astrobiology, University of California, Los Angeles, CA 90095-1562, USA; jura@astro.ucla.edu Received 2007 November 19; accepted 2008 February 20; published 2008 April 7

ABSTRACT

Extrapolating from the solar system's asteroid belt, we propose that externally contaminated white dwarfs without an infrared excess may be experiencing continuous accretion of gas-phase material that is ultimately derived from the tidal destruction of multiple small asteroids. If this scenario is correct, then observations of metal-polluted white dwarfs may lead to determination of the bulk elemental compositions of ensembles of extrasolar minor planets. *Key words:* planetary systems – white dwarfs

1. INTRODUCTION

An indirect but potentially powerful method to determine the elemental abundances of extrasolar minor bodies and planets is to measure the photospheric compositions of stars they pollute. Such studies in main-sequence stars are challenging because the host star's photosphere possesses intrinsic metals, making it difficult to determine the amount, if any, of contamination (see Gonzalez 2006). In contrast, heavy elements rapidly settle out of the atmospheres of white dwarfs cooler than 20,000 K (Koester & Wilken 2006), so that photospheric metals have an external source. We hope to identify which metal-possessing cool white dwarfs have accreted circumstellar rather than interstellar material in order to use these white dwarf atmospheres to measure the bulk elemental composition of extrasolar minor planets.

There are strong arguments that the approximately ten single white dwarfs known to have an infrared excess (Kilic et al. 2006a, 2006b; Kilic & Redfield 2007; Mullally et al. 2007; Jura et al. 2007a; von Hippel et al. 2007; Farihi et al. 2008; J. Farihi et al. 2008, in preparation) are accreting tidally disrupted asteroids. (1) The near-infrared excess discovered around G29-38 (Zuckerman & Becklin 1987) was shown to be produced by dust (Graham et al. 1990) that likely resulted from an orbitally perturbed minor planet (Debes & Sigurdsson 2002) that passed within the tidal radius of the host star (Jura 2003). For other white dwarfs, the infrared excess is usually well modeled with a geometrically flat dust disk that lies within the tidal radius of the star (Jura et al. 2007a). (2) The infrared spectrum of G29-38 displays strong 10 μ m silicate emission with a spectral shape that resembles dust emission from the zodiacal light rather than interstellar silicates (Reach et al. 2005). GD 362, the second white dwarf discovered to have a nearinfrared excess (Becklin et al. 2005; Kilic et al. 2005), also displays a 10 μ m silicate feature characteristic of asteroidal rather than interstellar dust (Jura et al. 2007b). (3) The white dwarfs with an infrared excess generally show when measured that $F_{\nu}(24 \ \mu \text{m}) \ll F_{\nu}(8 \ \mu \text{m})$ (Reach et al. 2005; Jura et al. 2007a). There is no evidence for relatively cold dust grains outside the tidal radius (Jura et al. 2007a). (4) The atmospheric composition of GD 362 is refractory-rich and volatile-poor (Zuckerman et al. 2007), reminiscent of material in the inner solar system and unlike the interstellar medium. While not as comprehensively studied as GD 362, there are at least three other white dwarfs which are markedly deficient in carbon relative to iron as is characteristic of asteroids and very unlike the Sun or interstellar matter (Jura 2006). (5) Asteroid belts similar to the solar system's can supply the required pollution masses (Jura 2006).

Only about 1/7 of all contaminated white dwarfs display an infrared excess (Kilic & Redfield 2007); the origin of the pollution of the more numerous contaminated white dwarfs without an infrared excess is uncertain. Although interstellar accretion could supply the metals in the atmospheres of contaminated white dwarfs (see, for example, Dupuis et al. 1993; Koester & Wilken 2006; Zuckerman et al. 2003; Dufour et al. 2007), there are difficulties with this model. First, at least for helium-rich stars, the accretion of hydrogen relative to calcium must be suppressed by at least a factor of 100 (Dufour et al. 2007). None of the suggested mechanisms such as magnetic shielding that preferentially exclude hydrogen from the star has yet received any observational support (Friedrich et al. 2004). Furthermore, there is no correlation between metal contamination and the star's space motion as would be expected from Bondi-Hoyle accretion theory (Zuckerman et al. 2003; Koester & Wilken 2006). Finally, using a very simple model of grain inspiral because of Poynting-Robertson drag, Jura et al. (2007b) showed that the predicted fluxes at 24 μ m for Bondi– Hoyle accretion can be more than 100 times greater than the observed upper limits. In view of these difficulties, the alternative of accretion of circumstellar matter merits consideration.

Gaensicke et al. (2006, 2007) have identified two metalcontaminated single white dwarfs with gaseous dust disks that are likely the result of tidal disruption of a large parent body such as an asteroid. It is possible that in many cases, the dust orbiting a white dwarf is destroyed and therefore stars without an infrared excess may still experience accretion from tidally disrupted minor bodies. In this paper, we elaborate upon this possibility.

In contrast to hydrogen-rich white dwarfs where the gravitational settling time of metals is typically less than 100 years (see von Hippel & Thompson 2007), in helium-rich white dwarfs cooler than 20,000 K, the gravitational settling time may be considerably longer than 10^5 yr (Paquette et al. 1986; Dupuis et al. 1993). Although very uncertain, we suggest below that the lifetime of a dusty disk around a white dwarf might be $\sim 10^5$ yr. Therefore, at least for the helium-rich white dwarfs, the absence of an infrared excess might simply be a situation where a single tidally disrupted asteroid has been fully accreted and the disk has dissipated but the contamination still lingers in the star's atmosphere.

In Section 2 we present a qualitative overview of our proposed model where we suggest that contaminated white dwarfs without an infrared excess accrete from a gaseous disk created by the accumulation from many small asteroids. This contrasts with our model for the white dwarfs with an infrared excess which we expect to be the result of the destruction of a single large asteroid. In Section 3 we argue that asteroids larger than 1-10 km in radius are likely to survive the star's evolution through the asymptotic giant branch (AGB) phase. In Section 4 we describe in somewhat more detail our model of white dwarf contamination by multiple tidal disruptions of small asteroids. In Section 5 we discuss observational assessment of this scenario. In Section 6 we discuss implications of this model and in Section 7 we present our conclusions.

2. OVERVIEW

Very little is known about extrasolar asteroid belts. Even the presence of warm dust at a few AU from the star does not tightly constrain the parent-body populations (see Wyatt et al. 2007). Here, assuming that many other main-sequence stars possess an asteroid belt similar to the solar system's, we present a single illustrative model to account for the white dwarf data. There are many unknown parameters; our calculations aim to establish that there is at least one plausible scenario where multiple small asteroids can explain the presence of metals in white dwarf photospheres. If detailed abundance studies of polluted white dwarfs without an infrared excess were shown to be consistent with this hypothesis, then a more comprehensive investigation would be warranted.

In our illustrative model, we suggest that the total mass of the asteroid belt when the star becomes a white dwarf is 10^{25} g, somewhat larger than the solar system's asteroid belt current mass of 1.8×10^{24} g (Binzel et al. 2000). We assume that there is a steeply rising number of lower-mass asteroids, and we then compute that asteroids larger than $\sim 1-10$ km in radius plausibly survive the star's evolution through the AGB. Although we do not compute detailed models, we propose that the orbits of these asteroids are occasionally perturbed on a timescale of ~ 1 Gyr into orbits which lead them within the tidal radius of the white dwarf (see Debes & Sigurdsson 2002; Duncan & Lissauer 1998) where the asteroid is rapidly shredded into smaller rocks and dust debris.

Small asteroids are sufficiently common, such that perhaps one is perturbed into an orbit where it is tidally disrupted every 300 years. We argue that the accretion time on the white dwarf is long compared to this arrival time, so that white dwarfs with surviving asteroid belts inevitably possess a low-mass disk composed of disintegrated larger bodies. It is likely that newly perturbed asteroids arrive at a random nonzero inclination relative to the pre-existing disk. As the asteroid passes through the disk, solid material is rapidly sputtered into the gas phase and a small asteroid is effectively vaporized. The matter gained by the disk from disrupted asteroids is lost by accretion into the atmosphere of the white dwarf, thus explaining the star's external pollution. In these systems, there is little dust and a negligible infrared excess.

More rarely, a large asteroid is perturbed into an orbit where it is tidally disrupted. If sufficiently large, the destroyed asteroid dominates over the pre-existing gaseous disk. In these systems, a dust ring is formed and survives for perhaps 10⁵ yr; during this phase there is an infrared excess.

3. ASTEROID SURVIVAL DURING THE STAR'S AGB PHASE

Asteroids must survive the AGB phase if they are to pollute the star as a white dwarf. Rybicki & Denis (2001) discuss three processes that can lead to terrestrial planet destruction during the AGB phase. A planet can induce a tidal bulge in its host star which can then interact with the planet to drag it inwards. However, asteroids have such small masses that this effect is not important. Below, we consider two other routes for asteroid destruction.

3.1. Asteroid Destruction by Wind Drag

Asteroids may spiral into the host star under the action of gas drag as they orbit through the wind of the AGB star. We assume that an asteroid is destroyed if it encounters its own mass in the wind. This destruction occurs because of hydrodynamic friction rather than sputtering which is negligible since the colliding gas atoms have kinetic energies of only a few eV (see Tielens et al. 1994). At distance D from the star in a spherically symmetric wind of mass loss rate \dot{M}_* with outflow speed, $V_{\rm wind}$, the gas density, $\rho_{\rm wind}$, is

$$\rho_{\rm wind} = \frac{M_*}{4\pi D^2 V_{\rm wind}}.\tag{1}$$

As long as gravitational focusing is negligible, the rate of encountering mass, \dot{M}_{enc} , by the asteroid is

$$\dot{M}_{\rm enc} = \pi R_{\rm ast}^2 \rho_{\rm wind} V_{\rm ast},$$
 (2)

where the asteroid of radius R_{ast} has orbital speed V_{ast} . For this evaluation, we assume that the asteroid's radius and mass are constant during the AGB phase. For circular motion,

$$V_{\rm ast} = \left(\frac{GM_*}{D}\right)^{1/2}.$$
 (3)

If the timescale for mass loss is slow compared to the asteroid's orbital period, then the specific angular momentum of the asteroid is approximately conserved and

$$DM_* = D_i M_i \tag{4}$$

for an initial distance, D_i , from a star of initial mass, M_i . As the star loses mass and M_* diminishes, then the asteroid's orbit expands. Combining Equations (1)–(4), during the star's AGB phase, the total encountered mass, M_{enc} is

$$M_{\rm enc} = \int \dot{M}_{\rm enc} dt \approx \frac{R_{\rm ast}^2 G^{1/2} M_i^{3/2}}{16 V_{\rm wind} D_i^{5/2}}.$$
 (5)

In arriving at the last expression in Equation (5), a simplified and slightly altered version of Equation (3) of Duncan & Lissauer (1998), we assume $M_i \gg M_f$ where M_f is the final mass of the star (see, for example, Weidemann 2000).

If ρ_{ast} is the density of the asteroid whose mass is $(4\pi\rho_{ast}R_{ast}^3)/3$, then Equation (5) leads to the condition that the minimum radius of a surviving asteroid, R_{min} , is

$$R_{\min} = \frac{3M_i^{3/2}G^{1/2}}{64\pi D_i^{5/2}\rho_{\rm ast}V_{\rm wind}}.$$
(6)

We only consider asteroids with initial distances from the host star greater than 2 AU because interior to this region, there may be a quasi-static region around the AGB star with a density much greater than that given by Equation (1) (Reid & Menten 1997). Beyond 2 AU, we assume an outflow velocity of 2 km s^{-1} (Keady et al. 1988), a speed that is appreciably smaller than the typical wind terminal speed of 15 km s⁻¹ (Zuckerman 1980).



Figure 1. Minimum surviving asteroid radius versus initial distance from the star for stellar wind drag from Equation (6). The solid, dotted, and dashed lines are plotted for stars of initial masses of 1.5 M_{\odot} , 3.0 M_{\odot} , and 5.0 M_{\odot} , respectively.

We adopt $\rho_{ast} = 2.1 \text{ g cm}^{-3}$, as inferred for Ceres (Michalak 2000).

We show in Figure 1 the results for R_{\min} as a function of D_i for initial stellar masses of 1.5 M_{\odot} , 3 M_{\odot} , and 5 M_{\odot} . As can be seen from Equation (6), the value of R_{\min} diminishes rapidly as D_i increases since less mass is encountered in the wind. Also, R_{\min} increases with the initial mass of the star since the star ejects more mass for the asteroid to encounter. Depending upon the initial distance from the host star and its mass, we find that asteroids larger than 1–10 km in radius are likely to survive the drag induced by the AGB wind.

3.2. Asteroid Destruction by Thermal Sublimation

Subjected to the star's high AGB luminosity, an asteroid might thermally sublimate, and we now estimate the minimum size asteroid that survives this process. If the star's high-luminosity phase has duration, t_{AGB} , then the minimum size of a surviving asteroid is

$$R_{\rm min} = \frac{dR_{\rm ast}}{dt} t_{\rm AGB}.$$
 (7)

 $dR_{\rm ast}/dt$ is the rate at which an asteroid's radius shrinks because of sublimation:

$$\frac{dR_{\rm ast}}{dt} = \frac{\sigma(T)}{\rho_{\rm ast}},\tag{8}$$

where $\dot{\sigma}(T)$ denotes the mass production rate from the dust per unit area (g cm⁻² s⁻¹) as a function of the asteroid temperature, *T*. Assuming pure olivine,

$$\dot{\sigma}(T) = \dot{\sigma}_0 \sqrt{\frac{T_0}{T}} e^{-T_0/T} \tag{9}$$

where, converted to cgs units, $\dot{\sigma}_0 = 1.5 \times 10^9$ g cm⁻² s⁻¹ and $T_0 = 65,300$ K (Kimura et al. 2002). Different materials may have different sublimation rates, so our results are sensitive to the



Figure 2. Minimum surviving asteroid radius versus distance from the star for olivine sublimation (Section 3.2). The solid line and dashed line are for stars with luminosities of $1.0 \times 10^4 L_{\odot}$ and $2.0 \times 10^4 L_{\odot}$, respectively.

presumed asteroid composition. We adopt olivine as this appears to be the most likely carrier of the 10 μ m silicate emission seen in G29-38 (Reach et al. 2005) and GD 362 (Jura et al. 2007b) as well as being common in the solar system. Assuming that the asteroids have a negligible albedo, we write that

$$T = \left(\frac{L_*}{16\pi\sigma_{\rm SB}D^2}\right)^{1/4},$$
 (10)

where L is the luminosity of the star and $\sigma_{\rm SB}$ is the Stefan–Boltzmann constant. While on the AGB, we assume that the star has a luminosity near 10⁴ L_{\odot} or larger for $t_{\rm AGB} = 2 \times 10^5$ yr (Jura & Kleinmann 1992).

Using Equations (8)–(10), we show in Figure 2 the minimum size asteroid from Equation (7) for stellar luminosities of $1 \times 10^4 L_{\odot}$ and $2 \times 10^4 L_{\odot}$ as a function of the asteroid's distance from the star. We neglect the orbital drift of the asteroid discussed above. Because the thermal sublimation rate is temperature sensitive, asteroid survival decreases rapidly as the star's luminosity increases or for asteroids that orbit relatively close to the star. We see from Figure 2 that depending upon the luminosity of the star, asteroids with radii between 1 and 10 km are likely to survive if they orbit beyond 3 or 4 AU.

4. ACCRETION OF MANY SMALL ASTEROIDS

Eventually, those asteroids that survive a star's AGB evolution may have their orbits perturbed so that they come within the tidal radius of the white dwarf (Duncan & Lissauer 1998; Debes & Sigurdsson 2002). When this occurs, the asteroid is shredded into dust. If the asteroid is relatively small and if there is a preexisting disk from destruction of previous asteroids, then the shredded debris of the new asteroid is destroyed by sputtering in the pre-existing disk, and the circumstellar matter is largely gaseous. If, instead, the asteroid is more massive than the preexisting disk, there is not enough gas to sputter the debris from the asteroid, and a disk with a large amount of dust at the inclination angle of the large asteroid is created. This more massive disk subsumes the low-mass pre-existing gaseous disk. Eventually, however, this large disk is accreted onto the star and the system relaxes to its steady-state configuration of a largely gaseous disk.

We denote the total asteroid belt's total mass as $M_{\text{belt}}(t)$, where t denotes the cooling time of the white dwarf. Let t_{orbit} be the mean lifetime of an asteroid before it is perturbed into the tidal radius of the star. Assuming that all of the shredded asteroid is ultimately accreted, the average metal-accretion rate, $\langle \dot{M}_{\text{metal}} \rangle$, is

$$\langle \dot{M}_{\text{metal}} \rangle = \frac{M_{\text{belt}}(t)}{t_{\text{orbit}}}.$$
 (11)

JURA

If the circumstellar gaseous disk around a white dwarf has a lifetime, t_{gas} , then the mass of a typical disk, M_{disk} , is

$$M_{\rm disk} = \langle M_{\rm metal} \rangle t_{\rm gas}.$$
 (12)

We propose that if an asteroid has a mass larger than $M_{\rm disk}$, then a single event dominates the circumstellar environment and the star exhibits an infrared excess. If, however, an asteroid arrives with a mass lower than $M_{\rm disk}$, then this newly-shredded asteroid's dust debris is rapidly vaporized and the disk remains gaseous.

We picture that all polluted white dwarfs possess in a steady state a gaseous disk and, occasionally, a massive dusty disk. It is likely that a white dwarf takes relatively little time to enter its "normal" steady state with a gaseous disk. The first tidally disrupted asteroid is shredded into dust which can persist for a long time since there is not likely to be much viscosity in the dust particles. The second tidally disrupted asteroid is also shredded into dust, but its orbital inclination is likely to be different from that of the first asteroid. Consequently, there will be grain–grain collisions approaching 1000 km s⁻¹ within the tidal radius. These collisions are very destructive and large amounts of gas will be released. Eventually, as described below, the disk will evolve into a large gaseous system.

4.1. Duration of Gaseous Disks: tgas

To progress further, we now estimate the lifetime of a white dwarf's circumstellar disk which we presume is controlled by viscous dissipation. We could extrapolate from cataclysmic variables to single white dwarfs. However, disks derived from destroyed asteroids probably have little hydrogen, and their compositions are very different from those of the disks in cataclysmic variables. For a gaseous circumstellar disk, the time for viscous dissipation is (King et al. 2007)

$$t_{\rm gas} \sim D \frac{V_{\rm ast}}{\alpha V_{\rm th}^2},$$
 (13)

where α is the usual dimensionless parameter and V_{th}^2 is $\sim k_{\text{B}}T/m_{\text{ast}}$, where k_{B} is the Boltzmann constant, *T* the temperature and m_{ast} the mean atomic weight of the asteroidal matter. The most uncertain factor is α . As discussed by King et al. (2007), empirical estimates of α for thin, fully ionized disks are between 0.1 and 0.4, but theoretical simulations yield values of α that are at least an order of magnitude lower. In FU Ori stars, values of α as low as 0.001 are inferred. The viscosity also may be a function of the gas ionization and decrease as the gas becomes more neutral. Here, because the disks around single white dwarfs may be long-lived, we assume that α is 0.001, but this value is extremely uncertain. We use models of the infrared

Vol. 135

emission from disks (Jura et al. 2007a) to adopt a characteristic disk size, D, of 3×10^{10} cm. At this distance from the star, $V_{\rm ast} = 5 \times 10^7$ cm s⁻¹, and at least for dusty disks, a representative temperature is 300 K (Jura 2003). If $m_{\rm ast}$ equals that of silicon, then $t_{\rm gas} \approx 5 \times 10^4$ yr. Although this estimate of the timescale is very uncertain, it is long compared to the time between arrivals of small asteroids within the tidal zone (see Section 5).

4.2. Destruction Timescale of Small Asteroids in a Gaseous Disk

We now show that if a relatively small asteroid impacts a gaseous disk, then the resulting infrared excess from dust debris has a short duration compared to the characteristic disk lifetime. In the solar system, asteroids in the main belt have a mean inclination, *i*, of 7.9° (Binzel et al. 2000), and in white dwarf systems, it is unlikely that a newly tidally disrupted asteroid has exactly the same orbital inclination as the pre-existing gaseous disk. As a result, as the debris from the asteroid orbits through the disk, it is eroded by sputtering.

Let Σ_{disk} (g cm⁻²) denote the mean disk surface density:

$$\Sigma_{\rm disk} = \frac{M_{\rm disk}}{\pi D^2}.$$
 (14)

If spherical grains of radius a move with speed v through a disk with number density, n, then the mass loss from sputtering is

$$\frac{d}{dt}\left(\frac{4\pi\rho_{\rm ast}a^3}{3m_{\rm ast}}\right) = -y(\pi a^2 nv),\tag{15}$$

where y is the sputtering yield. If the grains and the disk have the same composition since they are both derived from asteroids, then each passage through the disk erodes a layer of thickness, Δa_{pass} , where

$$\Delta a_{\text{pass}} = \frac{y \Sigma_{\text{disk}}}{4\rho_{\text{ast}} \sin i}.$$
 (16)

With two passages per orbit, in time t with $t \gg P$, where P denotes the asteroid's orbital period, the minimum radius of a grain that survives, a_{\min} is

$$a_{\min} = 2\Delta a_{\text{pass}} \frac{t}{P}.$$
 (17)

The infrared excess from a disk depends upon its optical depth which we now show rapidly becomes optically thin. Let χ denote the opacity of the dust. Assuming that the grain optical cross section is given by its geometric cross section and making the conservative assumption that all dust particles have size a_{\min} , then

$$\chi = \frac{3}{4\rho_{\rm ast}a_{\rm min}}.$$
 (18)

If the mass of the asteroid is less than the mass of the disk, then the vertical optical depth through the disk, τ_z , is bounded so that

$$\tau_z \leqslant \chi \Sigma_{\text{disk}}.$$
 (19)

Using Equations (16)–(19),

$$\tau_z \leqslant \frac{3\sin i}{2y} \frac{P}{t}.$$
 (20)

Light from the star of radius R_* illuminates the disk at a slant angle of R_*/D , and the optical depth in the disk, τ_{disk} , to light at this angle is

$$\tau_{\rm disk} \approx \tau_z \frac{D}{R_*} = \frac{3D \sin i}{2R_* y} \frac{P}{t}.$$
 (21)

From Equation (21), τ_{disk} diminishes with time as grains are destroyed. We now assume that the typical atom in the disk is silicon. The orbital speed at the disk is near 500 km s⁻¹ and with an inclination angle of 7.9°, the characteristic speed and kinetic energy of a silicon atom impacting a grain are ~ 70 km s⁻¹ and \sim 700 eV, respectively. Using the models of Tielens et al. (1994), we adopt $y \approx 0.1$. For $D/R_* = 30$, as representative of a disk within the tidal zone of the star, Equation (21) shows that $\tau_{\rm disk}$ becomes less than unity within ~60 orbital times. Since the orbital time of an asteroid might be ~ 10 yr, this implies that there is appreciable infrared emission from the system for at most ~ 600 yr. The true duration of an excess is probably much shorter since, for example, most incoming asteroids have masses appreciably smaller than those of the disk so that the bound given in Equation (19) is conservative. Also, we have probably substantially overestimated the opacity of the dust debris by assuming that all the particles have the minimum size.

4.3. Duration of Dust Disks

We propose that when a massive asteroid's orbit is perturbed so it is tidally destroyed, then a dust disk results. If analogous to Saturn's rings, this might only take ~ 100 orbital times or \sim 1000 yr for the disk to form (Dones 1991). The subsequent evolution of the dust disk depends upon its viscosity which is highly uncertain. If the disk were composed purely of dust grains, then, like the rings of Saturn, the duration of the disk could be comparable to or longer than 10⁸ yr. However, we anticipate that the dust disk is bombarded by orbitally perturbed small asteroids and the resulting grain-grain collisions produce gas in the disk. For a mass distribution of asteroids given by Equation (23), the median mass of a large asteroid that creates a dust disk is $2M_{\text{disk}}$. A dust disk derived from the median-sized large asteroid accumulates by further collisions of small asteroids, its own mass in gas in a timescale of $2t_{gas}$. Furthermore, the asteroid may have had a substantial amount of internal water which can be released into the gas phase as the asteroid is destroyed. Estimates for the percentage by mass of internal water in Ceres range between 0.17 and 0.27 (McCord & Sotin 2005; Thomas et al. 2005). If the viscous time scales inversely as the fraction of matter that is gaseous, then in the absence of adding any additional gas from small asteroids, t_{dust} would be between a factor of 4 and 6 longer than t_{gas} . Although extremely uncertain, we adopt on average that $t_{dust} \sim 3t_{gas}$ or perhaps 1.5×10^5 yr.

5. MODEL ASSESSMENT

We now evaluate the model that asteroids are the main source of contamination of many externally polluted white dwarfs. In our "standard model" the mass of the asteroid belt, $M_{belt}(t)$, is taken to equal 10^{25} g at the onset of the white dwarf phase when t = 0. We assume that there is a characteristic time, t_{orbit} , to perturb an asteroid into a tidally disrupted orbit. Therefore,

$$M_{\text{belt}} = M_{\text{belt}}(0)e^{-t/t_{\text{orbit}}}.$$
(22)

This expression for an exponential decay of the asteroid belt is at best a rough approximation; other models are discussed by Wyatt et al. (2007) and Dobrovolskis et al. (2007).

A critical parameter in our analysis is t_{orbit} . To date, simulations for the evolution of asteroid belts around white dwarfs have been somewhat limited, although Duncan & Lissauer (1998) and Debes & Sigurdsson (2002) computed various scenarios. For the future evolution of the solar system, Duncan & Lissauer (1998) followed the orbits of five asteroids, and found that one was always unstable. In two out of their four simulations, a second asteroid, Pallas, became unstable in 5×10^8 yr. To reproduce the data, we adopt values of t_{orbit} near 1 Gyr. However, more simulations for the asteroid belt evolution during the white dwarf phase are needed.

We assume that the asteroid belt has a mass distribution, n(M)dM, given by a power law so that

$$n(M)dM = AM^{-2}dM, (23)$$

where the constant A is derived by the normalization condition. This power-law variation of M^{-2} is slightly steeper than the "classical" estimate for the solar system that n(M) varies as $M^{-1.83}$ (O'Brien & Greenberg 2005), but it is computationally convenient and adequate for systems about which we know very little. If the mass of the largest and smallest asteroids are M_{max} and M_{min} , respectively, then

$$A = M_{\text{belt}} \left(\ln \left[\frac{M_{\text{max}}}{M_{\text{min}}} \right] \right)^{-1}.$$
 (24)

As in the solar system, we assume that the largest asteroid has an appreciable fraction of the total mass of the entire system, and we adopt $M_{\text{max}}(t) = 0.2M_{\text{belt}}(t)$. Thus, initially, the largest asteroid has a mass of 2×10^{24} g, somewhat larger than the mass of Ceres which is 9.4×10^{23} g (Michalak 2000). We assume that M_{min} is independent of time and equals 2×10^{17} g, the mass of an asteroid with radius 3 km and density 2.1 g cm⁻³. In this model, the total number of asteroids initially is 3×10^{6} . With $t_{\text{orbit}} = 1$ Gyr, this would result in an asteroid being tidally disrupted every 300 yr.

5.1. Which Contaminated White Dwarfs have an Infrared Excess?

In the context of our model, we now compute which white dwarfs may have an infrared excess. This requires estimating $\langle \dot{M}_{metal} \rangle$ which we take as

$$\langle \dot{M}_{\text{metal}} \rangle = \frac{M_{\text{belt}}(0)}{t_{\text{orbit}}} e^{-t/t \text{orbit}}.$$
 (25)

To compare this quantity with observables, we estimate the white dwarf's cooling time from its effective temperature. We interpolate from the calculations of Winget et al. (1987) and Hansen (2004) and take for white dwarfs with masses near $0.6 M_{\odot}$

$$t_9 = 0.38 \left(\frac{12000}{T_{\rm eff}}\right)^3,$$
 (26)

where t_9 denotes the cooling time (Gyr). This approach neglects the variation in stellar radii and masses. If a white dwarf exhibits an accretion rate above $\langle \dot{M}_{metal} \rangle$, then, according to our model, it experiences accretion from a single large asteroid and should possess an infrared excess. We show in Figure 3 a plot of



Figure 3. Metal accretion rates versus stellar effective temperature. The filled circles represent stars with an infrared excess while the open triangles represent stars without an infrared excess. The data are taken from Farihi et al. (2008) and Jura et al. (2007b); the metal accretion rates are taken from Koester & Wilken (2006) and scaled according to the procedure in Jura et al. (2007b). The lines represent $\langle \dot{M}_{metal} \rangle$ as a function of the star's effective temperature from Section 5.1. We assume initial asteroid belt masses of 10^{25} g and the dotted, solid, and dashed lines represent values of t_{orbit} of 0.5 Gyr, 1.0 Gyr, and 2.0 Gyr, respectively. The solid circles are expected to lie above the curves, while the open triangles are predicted to lie below the curves.

accretion rate versus stellar effective temperature for externally polluted hydrogen-rich white dwarfs where the accretion rate can be reliably estimated. In this plot, we also show the value of $\langle \dot{M}_{metal} \rangle$ for $M_{belt}(0) = 10^{25}$ g and t_{orbit} varying from 0.5 Gyr to 2.0 Gyr. The model and the data are consistent for most but not all stars. The adopted estimated mass in the asteroid belts of 10^{25} g is larger than that in the solar system; this point is discussed in Section 6.

While the data points in Figure 3 mostly obey the predicted relationship, there are exceptions. The most deviant point is for WD 1633+433 with $\dot{M}_{\rm metal} = 4 \times 10^8$ g s⁻¹ and $T_{\rm eff} = 6600$ K (Koester & Wilken 2006). Perhaps this star has a particularly long-lived and massive asteroid belt.

5.2. Relative Numbers of Contaminated White Dwarfs with and without an Infrared Excess

Any model to explain the contamination of white dwarfs should account for the relative numbers of stars with and without an infrared excess. We hypothesize in Section 4 that an infrared excess occurs when a tidally disrupted asteroid is more massive than the ambient gaseous disk. From Equation (23), the number of such asteroids, $N(M > M_{disk})$, is

$$N(M > M_{\rm disk}) \approx \frac{A}{M_{\rm disk}}.$$
 (27)

The total rate at which these asteroids are perturbed into orbits where they are tidally destroyed is $N(M > M_{disk})/t_{orbit}$. Therefore, if t_{dust} is the duration of a dust disk, the fraction of time, f_{IR} , that the white dwarf exhibits an infrared excess is

$$f_{\rm IR} = N(M > M_{\rm disk}) \frac{t_{\rm dust}}{t_{\rm orbit}}.$$
 (28)

Using Equations (11), (12), (24), (27) and (28), this expression becomes

$$f_{\rm IR} = \left(\frac{t_{\rm dust}}{t_{\rm gas}}\right) \left(\ln \frac{M_{\rm max}}{M_{\rm min}}\right)^{-1}.$$
 (29)

Evaluation of expression (29) is insensitive to the exact values of M_{max} and M_{min} . From our estimates given above, we find that $f_{\text{IR}} = 0.062$ ($t_{\text{dust}}/t_{\text{disk}}$). In Section 4.3, we argued that $t_{\text{dust}} \sim 3t_{\text{disk}}$. Although extremely uncertain, the prediction from Equation (29) is therefore that $f_{\text{IR}} \sim 0.19$, consistent with the observational constraint determined by Kilic & Redfield (2007) that at least 14% of externally polluted hydrogen-rich white dwarfs possess an infrared excess.

5.3. Composition of Accreted Material

One motivation for studying the composition of contaminated white dwarfs is that it enables the measurement of the bulk elemental composition of extrasolar minor planets. For example, the photosphere of the white dwarf GD 362 was found to be markedly deficient in volatiles such as carbon and sodium relative to refractories such as calcium and iron (Zuckerman et al. 2007), a pattern reminiscent of the inner solar system where the Earth and asteroids are also very volatile deficient.

Wolff et al. (2002) reported relative abundances of iron, magnesium, silicon, calcium, and carbon in ten helium-rich white dwarfs. Although in many cases the uncertainties are very large, three of these stars exhibit a carbon abundance less than that of iron and therefore a value of n(C)/n(Fe) that is at least a factor of 10 smaller than solar. The ratio of these metals in the photospheres of these stars is very approximately similar to that of the Earth or chondrites; they do not appear to have accreted interstellar matter (Jura 2006). One of these three stars, GD 40, also displays an infrared excess (Jura et al. 2007a), consistent with the hypothesis that it is accreting chondritic material. However, the other two stars do not display an infrared excess (J. Farihi et al., 2008, in preparation) which, however, as discussed below, does not preclude the asteroid accretion scenario.

Desharnais et al. (2008) report *Far Ultraviolet Spectroscopic Explorer (FUSE)* data for five helium-rich white dwarfs. Of these five stars, GD 378 has n(C)/n(Fe) = 2.5, within the errors not grossly different from the solar value of 8.3 (Lodders 2003). There are mostly only upper limits to the abundances for GD 233, a second star in this sample. However, G270-124, GD 61, and GD 408 all have values of n(C)/n(Fe) less than 0.3. These three stars are therefore candidates for having accreted chondritic material. G270-124 does not display an infrared excess shortward of 8 μ m (Mullally et al. 2007). As far as we know, GD 61 has not been observed for an infrared excess. There is a hint of an excess at 7.9 μ m for GD 408 (Mullally et al. 2007), but the signal to noise was not good enough for a definitive conclusion.

Not all contaminated white dwarfs appear to have accreted chondritic material. G238-44 has been found to display n(C)/n(Fe) near 2.5 (Dupuis et al. 2007); this star does not display any infrared excess (Mullally et al. 2007). As with GD 378, the source of the external matter is unknown.

There are at least two possible explanations for the absence of a near-infrared excess around externally polluted helium-rich white dwarfs. First, as discussed above, the circumstellar disk could be largely gaseous. Second, the disk may have dissipated before the contaminants have settled out of the star's atmosphere. The settling time of heavy metals



Figure 4. Comparison of data showing 1σ error bars (Farihi et al. 2008) with the predicted stellar and disk emission for G166-58. The model fluxes from the star, the disk and the total are represented by the dotted, dashed, and solid lines respectively. For clarity, the lower panel re-displays the dotted rectangle in the upper panel.

in the atmospheres of these stars with effective temperatures between 15,000 K and 21,000 K ranges from $\sim 3 \times 10^4$ yr to $\sim 5 \times 10^5$ yr (Dupuis et al. 1993), comparable to or longer than our very rough estimate of the duration of a dust disk of 1.5×10^5 yr.

5.4. Infrared Excess from a Largely Gaseous Disk?

Above, we have adopted the view that a disk is either essentially all dust or all gas. However, it is possible that some dust survives in disks that are bombarded by numerous small asteroids. Consider the case where the interior of the disk is gaseous yet the outer portion remains dusty, and thus the disk distribution may have an especially large central hole. All but one of the ten white dwarfs currently known to have an infrared excess has dust as warm as 1000 K (see Jura et al. 2007a). This innermost temperature may be determined by the location where grain sublimation becomes rapid. However, G166-58 (also known as LHS 3007 or WD 1455+298), a metal-polluted white dwarf with a metal accretion rate of 3×10^7 g s⁻¹ (Koester & Wilken 2006), was found by Farihi et al. (2008) to have an excess at 5.7 μ m and 7.9 μ m, but not at shorter wavelengths. Following Jura et al. (2007b), we compute a model with a flat disk to reproduce the data. We adopt a stellar temperature of 7390 K and a ratio of the star's radius (9.1 \times 10⁸ cm) to the star's distance from the Sun (\approx 30 pc), R_*/D , of 1.0×10^{-11} . We fit the infrared data with an inner disk temperature of 400 K (corresponding to a physical distance from the star of 30 R_* , Jura 2003), an outer disk temperature of 300 K (corresponding to a physical distance from the star of 43 R_*), and $\cos i = 0.4$. This model disk lies well within the tidal zone which extends to $\sim 100 R_*$ (Davidsson 1999). The comparison between observations and the model is shown in Figure 4; the fit is good enough that this model is a serious contender for explaining the data. Thus, this system may be in an intermediate phase of its disk evolution where the dust disk has a usually large hole because bombardment destroyed dust in the inner disk.

5.5. Detectability of Line Emission from Gaseous Disks?

Gaensicke et al. (2006, 2007) report emission lines from two disks; most polluted white dwarfs do not display emission lines even though we postulate the presence of a circumstellar reservoir from which they accrete. We suggest that the systems with detected emission are unusual because the gas has an unusually high excitation temperature, T_{ex} . If the star has effective temperature, T_* , and subtends solid angle, Ω_* , while the disk subtends solid angle, Ω_{disk} , then an opaque line is seen in emission if

$$B_{\nu}(T_{\rm ex})\Omega_{\rm disk} \sim B_{\nu}(T_*)\Omega_*.$$
 (30)

For SDSS 1228+1040, the analysis of Gaensicke et al. (2006) yields $\Omega_{\text{disk}}/\Omega_* = 1.2 \times 10^4$. Since $T_* = 22,020$ K, then for the calcium lines near 8500 Å, the above criterion requires $T_{\text{ex}} > 1800$ K. This temperature is much greater than expected for a passively heated disk material lying at 100 stellar radii (see Jura 2003), and some additional heating of the gas must be occurring. Gaensicke et al. (2006) show that the calcium lines are asymmetric and they explain this as the consequence of our viewing an eccentric disk. Because the orbits should circularize by mutual collisions, it is plausible that the eccentricity is being driven by some external unseen planet. If so, this material would also be heated. Other disks may not be subjected to such extreme heating, and their circumstellar gas would be too cool to be detected.

6. DISCUSSION

There are a number of similarities between the asteroid belt in the solar system and the proposed asteroid belts around white dwarfs. We invoke asteroid belt masses of 10^{25} g at the time the star enters its white dwarf phase; this mass is about a factor of 6 larger than the mass of the asteroid belt in the solar system. However, if stars form with a Salpeter mass function, $n(M_*)dM_*$, that varies as $M_*^{-2.35}$ and if the lowest mass star that is currently dying has a mass of 0.9 M_{\odot} , then the median main sequence mass of a dying star is $\sim 1.5 M_{\odot}$. There may be a linear scaling between the mass of a star's asteroid belt and its main-sequence mass. Furthermore, 1.5 M_{\odot} stars spend only ~ 3 Gyr on the main sequence before becoming white dwarfs, significantly less than the current age of the solar system of 4.6 Gyr. Thus, when a 1.5 M_{\odot} star becomes a white dwarf, a simple linear extrapolation from the solar system suggests that its asteroid belt would possess 4×10^{24} g, and thus approximately resemble the solar system's asteroid belt.

A minimum mass of an extrasolar asteroid can be estimated from the mass of contaminants in the atmosphere of a contaminated helium-rich white dwarf. Since calculations for the mass in the outer mixing zone differ by as much as a factor of 10 (Dupuis et al. 1993, MacDonald et al. 1998), these estimates are uncertain. At the moment, the He-rich white dwarf with the most massive pollution is HS 2253+8023 (Wolff et al. 2002), and the inferred mass of its accreted asteroid is $\sim 10^{24}$ g (Jura 2006), comparable to the mass of Ceres.

The relative numbers of polluted white dwarfs with and without an infrared excess are explained by a mass distribution of extrasolar asteroids that varies as M^{-2} , approximately what

is observed in the solar system. Thus, extrasolar asteroid belts may possess a size distribution similar to that of asteroids in the solar system.

Remarkably, in marked contrast to the solar composition, carbon appears to be less abundant by number than iron or silicon in at least a few extrasolar asteroids. Similarly, as measured from chondrites (Lodders 2003), asteroids in the solar system have a similarly low carbon-to-iron abundance ratio. As argued previously (Jura 2006), determinations of the abundances in the atmospheres of white dwarfs can serve both to evaluate the model of interstellar accretion and, at least in some cases, to measure the composition of extrasolar asteroids.

7. CONCLUSIONS

We suggest that the contamination of many externally polluted white dwarfs without an infrared excess results from tidal disruptions of numerous small asteroids. This scenario is consistent with the hypothesis that the masses, size distributions, and compositions of extrasolar asteroids are similar to those of the solar system's asteroids.

This work has been partly supported by NASA.

REFERENCES

- Becklin, E. E., Farihi, J., Jura, M., Song, I., Weinberger, A. J., & Zuckerman, B. 2005, ApJ, 632, L119
- Binzel, R. P., Hanner, M. S., & Steel, D. I. 2000, in Allen's Astrophysical Quantitiies, ed. A. N. Cox (New York: Springer), 315
- Davidsson, B. J. R. 1999, Icarus, 142, 525
- Debes, J. H., & Sigurdsson, S. 2002, ApJ, 572, 556
- Desharnais, S., Wesemael, F., Chayer, P., Kruk, J. W., & Saffer, R. A. 2008, ApJ, 672, 540
- Dobrovolskis, A. R., Alvarellos, J. L., & Lissauer, J. J. 2007, Icarus, 188, 481 Dones, L. 1991, Icarus, 92, 194

Dufour, P., et al. 2007, ApJ, 663, 1291

- Duncan, M. J., & Lissauer, J. J. 1998, Icarus, 134, 303
- Dupuis, J., Bouabid, M.-P., Wesemael, F., & Chayer, P. 2007, in ASP Conf. Ser., 372, 15th European Workshop on White Dwarfs, ed. R. Napiwotzki, & M. R. Burleigh (San Francisco, CA: ASP), 261
- Dupuis, J., Fontaine, G., Pelletier, C., & Wesemael, F. 1993, ApJS, 84, 73
- Farihi, J., Zuckerman, B., & Becklin, E. E. 2008, ApJ, 674, 431
- Friedrich, S., Jordan, S., & Koester, D. 2004, A&A, 424, 665
- Gaensicke, B. T., Marsh, T. R., & Southworth, J. 2007, MNRAS, 380, L35
- Gaensicke, B. T., Marsh, T. R., Southworth, J., & Rebassa-Mansergas, A. 2006, Science, 314, 1908

- Gonzalez, G. 2006, PASP, 118, 1494
- Graham, J. R., Matthews, K., Neugebauer, G., & Soifer, B. T. 1990, ApJ, 357, 216
- Hansen, B. M. S. 2004, Phys. Rep., 399, 1
- Jura, M. 2003, ApJ, 584, L91
- Jura, M. 2006, ApJ, 653, 613
- Jura, M., Farihi, J., & Zuckerman, B. 2007a, ApJ, 663, 1285
- Jura, M., Farihi, J., Zuckerman, B., & Becklin, E. E. 2007b, AJ, 133, 1927
- Jura, M., & Kleinmann, S. G. 1992, ApJS, 79, 105
- Keady, J. J., Hall, D. N. B., & Ridgway, S. T. 1988, ApJ, 326, 832
- Kilic, M., & Redfield, S. 2007, ApJ, 660, 641
- Kilic, M., von Hippel, T., Leggett, S. K., & Winget, D. E. 2005, ApJ, 632, L115
- Kilic, M., von Hippel, T., Leggett, S. K., & Winget, D. W. 2006a, ApJ, 646, 474
- Kilic, M., von Hippel, T., Mullally, F., Reach, W. T., Kuchner, M. J., Winget, D. W., & Burrows, A. 2006b, ApJ, 642, 1051
- Kimura, H., Mann, I., Biesecker, D. A., & Jessberger, E. K. 2002, Icarus, 159, 529
- King, A. R., Pringle, J. E., & Livio, M. 2007, MNRAS, 376, 1740
- Koester, D., & Wilken, D. 2006, A&A, 453, 1051
- Lodders, K. 2003, ApJ, 591, 1220
- MacDonald, J., Hernanz, M., & Jose, J. 1998, MNRAS, 296, 523
- McCord, T. B., & Sotin, C. 2005, J. Geophys. Res., 110, 5009
- Michalak, G. 2000, A&A, 360, 363
- Mullally, F., Kilic, M., Reach, W. T., Kuchner, M. J., von Hippel, T., Burrows, A., & Winget, D. E. 2007, ApJS, 171, 206
- O'Brien, D. P., & Greenberg, R. 2005, Icarus, 178, 179
- Paquette, C., Pelletier, C., Fontaine, G., & Michaud, G. 1986, ApJS, 61, 197
- Reach, W. T., Kuchner, M. J., von Hippel, T., Burrows, A., Mullaly, F., Kilic, M., & Winget, D. E. 2005, ApJ, 635, L161
- Reid, M. J., & Menten, K. M. 1997, ApJ, 476, 327
- Rybicki, K. R., & Denis, C. 2001, Icarus, 151, 130
- Thomas, P. C., Parker, J. Wm., McFadden, L. A., Russell, C. T., Stern, S. A., Sykes, M. V., & Young, E. F. 2005, Nature, 437, 224
- Tielens, A. G. G. M., McKee, C. F., Seab, C. G., & Hollenbach, D. J. 1994, ApJ, 431, 321
- von Hippel, T., Kuchner, M. J., Kilic, M., Mullally, F., & Reach, W. T. 2007, ApJ, 662, 544
- von Hippel, T., & Thompson, S. E. 2007, ApJ, 661, 477
- Weidemann, V. 2000, A&A, 363, 647
- Winget, D. E., Hansen, C. J., Liebert, J., van Horn, H. M., Fontaine, G., Nather, R. E., Kepler, S. O., & Lamb, D. Q. 1987, ApJ, 315, L77
- Wolff, B., Koester, D., & Liebert, J. 2002, A&A, 385, 995
- Wyatt, M. C., Smith, R., Greaves, J. S., Beichman, C. A., Bryden, G., & Lisse, C. 2007, ApJ, 658, 569
- Zuckerman, B. 1980, ARA&A, 18, 263
- Zuckerman, B., & Becklin, E. E. 1987, Nature, 330, 138
- Zuckerman, B, Koester, D., Melis, C., Hansen, B., & Jura, M. 2007, ApJ,
- 671, 872 Zuckerman, B., Koester, D., Reid, I. N., & Hunsch, M. 2003, ApJ, 596, 477