

BIG BANG NUCLEOSYNTHESIS PREDICTIONS FOR PRECISION COSMOLOGY

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ABSTRACT

The determination of the primeval deuterium abundance has opened a precision era in big bang nucleosynthesis, making accurate predictions more important than ever before. We present in analytic form new, more precise predictions for the light-element abundances and their error matrix. Using our predictions and the primeval deuterium abundance, we infer a baryon density of $\Omega_b h^2 = 0.020 \pm 0.002$ (95% confidence level) and find no evidence for stellar production (or destruction) of ^3He beyond burning D into ^3He . Conclusions about ^4He and ^7Li currently hinge on possible systematic errors in their measurements.

Subject headings: cosmology: theory — nuclear reactions, nucleosynthesis, abundances

1. INTRODUCTION

The big bang nucleosynthesis (BBN) prediction of a large primeval abundance of ^4He ($Y_p \approx 0.25$) was the first success of the hot big bang model. For two decades, the consistency of the BBN predictions for the abundances of D, ^3He , ^4He , and ^7Li with their inferred primeval abundances has been an important test of the standard cosmology at early times ($t \sim 1$ s). BBN has also been used to “inventory” ordinary matter at a simpler time and to probe fundamental physics (see, e.g., Schramm & Turner 1998 or Olive, Steigman, & Walker 2000).

With the detection of deuterium Lyman features in the absorption spectra of three high-redshift ($z > 2$) quasars and the accurate determination of the primeval abundance of deuterium, $(\text{D}/\text{H})_p = (3.0 \pm 0.2) \times 10^{-5}$ (Burles & Tytler 1998a, 1998b; Kirkman et al. 2000; O’Meara et al. 2001), BBN has entered a new precision era (Schramm & Turner 1998). Because its abundance depends strongly on the baryon density, and its subsequent chemical evolution is so simple (astrophysical processes only destroy D), deuterium can accurately peg the baryon density. Once determined, the baryon density allows the abundances of ^3He , ^4He , and ^7Li to be predicted. These predictions can be used to test the consistency of the big bang framework and to probe astrophysics.

The chemical evolution of ^4He is simple (stars produce it), and so its predicted abundance, $Y_p = 0.246 \pm 0.001$ (Lopez & Turner 1999), can be used as a consistency test of BBN and the standard cosmology. Because the ^7Li abundance in old Population II stars may be depleted, lithium probes both stellar models and the consistency of the standard cosmology.

While the post-big bang evolution of ^3He is complex, the sum $\text{D} + ^3\text{He}$ can be used to study the chemical evolution of the Galaxy. All stars burn D into ^3He as they evolve onto the main sequence (MS). Later stages of stellar evolution may produce or destroy ^3He , depending on stellar mass and subject to uncertainty in modeling. Thus, the evolution of $\text{D} + ^3\text{He}$ measures the net stellar production of ^3He beyond pre-MS burning (Yang et al. 1984), providing an important probe of stellar models.

A key to realizing BBN’s full potential in the precision era is accurate and reliable predictions. With this in mind, we have recently used Monte Carlo techniques (Burles et al. 1999; Nollett & Burles 2000) to link the calculated abundances directly to the nuclear data, making the predictions more reliable.

Previous work (Smith, Kawano, & Malaney 1993; Fiorentini et al. 1998) was based on fitting cross section data to standard forms, estimating conservative uncertainties to accommodate most or all of the data for each reaction. Very recent work (Esposito et al. 2000; Vangioni-Flam, Coc, & Casse 2000) computes only “maximum” uncertainties, using upper and lower limits quoted in a compilation of charged-particle reaction rates (Angulo et al. 1999). In contrast, our procedure ties the abundance errors directly to the experimental measurements by weighting the data by their quoted errors and, furthermore, leads to smaller estimated abundance errors (by factors of 2–3).

In this Letter, we present our results in the form of analytic fits for the abundances and their error matrix. We then use these predictions to make inferences about the baryon density, the consistency of BBN, ^7Li depletion, and stellar ^3He production.

2. ANALYTIC RESULTS

Our BBN code draws reaction rates from a statistical distribution and computes the corresponding distribution of BBN yields. It varies all of the laboratory data (over 1200 individual data points) simultaneously, drawing random realizations of each data point and normalizations for each data set from Gaussian distributions representing reported values and uncertainties. For each realization, the BBN yields are computed using thermally averaged smooth representations of the realized data. The results presented here are based on 25,000 such realizations of the data (see Fig. 1). More details are given in Burles et al. (1999) and Nollett & Burles (2000).

Here we present fits of the means, variances, and correlation matrix of the predicted abundances to fifth-order polynomials in $x \equiv \log \eta + 10$, where η is the baryon-to-photon ratio (see Tables 1, 2, and 3). Applicable over the range $0 \leq x \leq 1$, our fits are accurate to better than 0.2% for the abundances and 10% for the variances. For the mean ^4He yields, we adopt the fitting formula of Lopez & Turner (1999), which is accurate to within 0.05%.⁶ Some of the abundances follow approximate

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⁶ Our fit coefficients are the a_i from their eq. (44). We note that their fitting formula for the dependence of Y_p on the neutron lifetime (δY_p in eq. [43] of that paper) has a misprint in the signs but not the magnitudes of the coefficients b_i . The correct sequence of signs for the b_i is $++--+-$. They also provide a fit for the N_p dependence of Y_p .

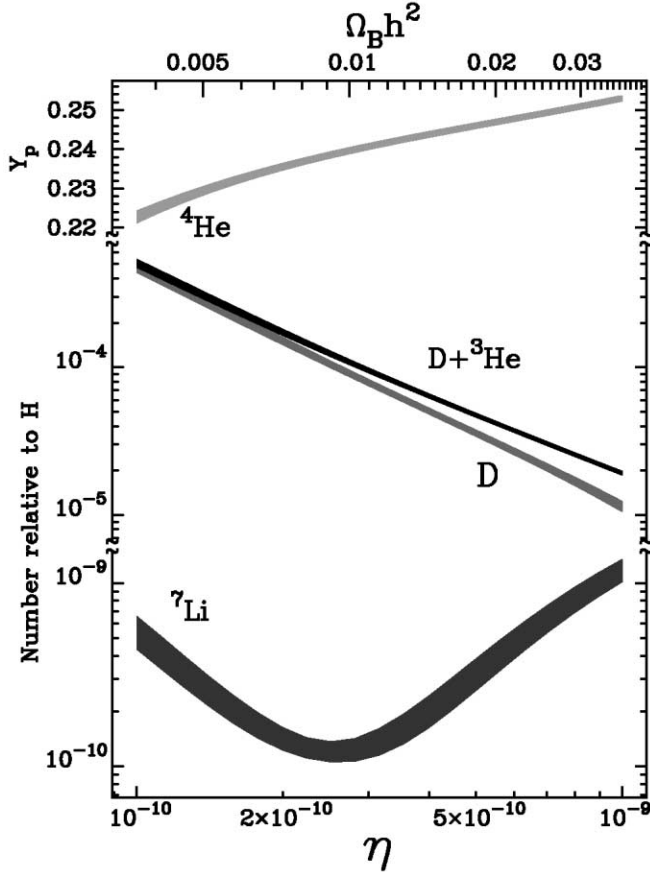


FIG. 1.—Predicted big bang abundances of the light elements shown as bands of 95% confidence.

power laws, and so we have obtained accurate fits by fitting the means and variances of their base 10 logarithms in all cases except the mean Y_p . Because our estimates for the uncertainties are small, $\text{Var}(Y_i) = (\bar{Y}_i/0.4343)^2 \text{Var}(\log Y_i)$. The covariance matrix is written in terms of the variances and a correlation matrix r_{ij} :

$$\rho_{ij} = r_{ij} \sqrt{\text{Var}(Y_i) \text{Var}(Y_j)}, \quad (1)$$

where Y_i is the baryon fraction for ${}^4\text{He}$ and the number relative to hydrogen for the other nuclides, and \bar{Y}_i is its mean over the output yields.

Finally, because BBN produces ${}^7\text{Li}$ by two distinct processes, direct production and indirect production through ${}^7\text{Be}$ with subsequent electron capture to ${}^7\text{Li}$, we have split the ${}^7\text{Li}$ yield into these two pieces to obtain more accurate fits. The mean prediction for ${}^7\text{Li}$ is just the sum of the two contributions; the variance $\text{Var}(Y_7) = \text{Var}(Y_{\text{Li}}) + \text{Var}(Y_{\text{Be}}) + 2\rho_{\text{Li, Be}}$. The co-

variance between the total BBN ${}^7\text{Li}$ and another nuclide $\rho_{i,7} = \rho_{i,\text{Li}} + \rho_{i,\text{Be}}$.

3. IMPLICATIONS

To use our predictions, we need observed abundances of the light elements. This is a lively area of research, with some controversy. Here, based on our evaluation of the data, we state our choices with brief justification and point the reader interested in more detail to the relevant literature. For the primordial deuterium abundance, we use the weighted average of the three detections in high-redshift Ly α , $(\text{D}/\text{H})_p = (3.0 \pm 0.2) \times 10^{-5}$ (for further discussion, see Burles, Nollett, & Turner 2001, Tytler et al. 2000, and O'Meara et al. 2001).

For the present abundance of $\text{D} + {}^3\text{He}$, we use measurements of both elements made in the local interstellar medium (ISM). The deuterium abundance, $\text{D}/\text{H} = (1.5 \pm 0.2 \pm 0.5) \times 10^{-5}$, comes from *Hubble Space Telescope*, *IUE*, and *Copernicus* measurements along 12 lines of sight to nearby stars (Linsky 1998; Lemoine et al. 1999; McCullough 1992). The first error is statistical, and the second error represents the possibility of scatter due to spatial variations (Vidal-Madjar & Gry 1984; Linsky 1998; Vidal-Madjar et al. 1998; Sonneborn et al. 2000); as it turns out, the uncertainty in ${}^3\text{He}$ dominates both. Gloeckler & Geiss (1998) have determined the ratio of ${}^3\text{He}$ to ${}^4\text{He}$ in the local ISM using the pickup ion technique. Allowing for a local ${}^4\text{He}$ mass fraction between 25% and 30%, their measurement translates to ${}^3\text{He}/\text{H} = (2.2 \pm 0.8) \times 10^{-5}$ and $(\text{D} + {}^3\text{He})/\text{H} = (3.7 \pm 1) \times 10^{-5}$.

For the primordial ${}^7\text{Li}$ abundance, we use the value advocated by Ryan (2000) and Ryan et al. (2000), based on the extant measurements of ${}^7\text{Li}$ in the atmospheres of old halo stars. This value, ${}^7\text{Li}/\text{H} = 1.2_{-0.2}^{+0.35} \times 10^{-10}$, includes empirical corrections for cosmic-ray production, stellar depletion, and improved atmospheric models, and the uncertainty arises mainly from these corrections. This is consistent with other estimates (see, e.g., Bonifacio & Molaro 1997; Ryan, Norris, & Beers 1999; Thorburn 1994).

The primordial abundance of ${}^4\text{He}$ is best inferred from H II regions in metal-poor, dwarf emission-line galaxies. While such measurements are some of the most precise in astrophysics, the values for Y_p obtained from the two largest samples of such objects are not consistent, and concerns remain about systematic error.

Olive, Steigman, & Skillman (1997) have compiled a large sample of objects and find that $Y_p = 0.234 \pm 0.002$. On the other hand, Izotov & Thuan (1998) have assembled a large sample from a single observational program, extracting Y_p from the spectra by a different method. They find that $Y_p = 0.244 \pm 0.002$ (consistent with the earlier sample of Kunth & Sargent 1983, who found that $Y_p = 0.245 \pm 0.003$). Furthermore, they have shown that at least one of the most metal-poor objects (I Zw 18) used in the earlier sample suffered from

TABLE 1
FITS TO THE ABUNDANCES, $\log \bar{Y}_i = \sum_i a_i x^i$, EXCEPT $\bar{Y}_p = \sum_i a_i x^i$

Nuclide	a_0	a_1	a_2	a_3	a_4	a_5
Y_p	0.22292	0.05547	-0.05639	0.04587	-0.01501	...
D/H	-3.3287	-1.6277	-0.2286	0.7794	-0.6207	0.0846
${}^3\text{He}/\text{H}$	-4.4411	-0.7955	0.4153	-0.9909	1.0925	-0.3924
$(\text{D} + {}^3\text{He})/\text{H}$	-3.2964	-1.5675	-0.1355	0.8018	-0.7421	0.2225
${}^7\text{Li}/\text{H}$	-9.2729	-2.1707	-0.6159	4.1289	-3.6407	0.7504
${}^7\text{Be}/\text{H}$	-12.0558	3.6027	2.7657	-6.5512	4.4725	-1.1700

TABLE 2
FITS TO THE VARIANCES, $\text{Var}(\log Y_i) = \sum_i a_i x^i$

Nuclide	a_0	a_1	a_2	a_3	a_4	a_5
$10^5 Y_p$	0.2544	-1.3463	4.0384	-6.3448	4.9910	-1.5446
$10^3 (\text{D}/\text{H})$	0.2560	0.1379	-2.3363	5.0495	-4.6972	1.9351
$10^3 ({}^3\text{He}/\text{H})$	0.0776	0.1826	-0.7725	1.5357	-0.9106	0.1522
$10^3 (\text{D} + {}^3\text{He})/\text{H}$	0.2181	-0.0287	-1.6284	3.5182	-2.8499	0.8323
$10^2 ({}^7\text{Li}/\text{H})$	0.2154	-0.0049	-1.7200	4.0635	-3.8618	1.3946
$10^2 ({}^7\text{Be}/\text{H})$	0.7970	1.2036	-6.5462	6.0483	-0.2788	-1.1190

stellar absorption, and they argue that it and possibly other metal-poor objects in this sample can help explain the discrepancy. Studies of ionization structure in H II regions may demand significant corrections (Viegas, Gruenwald, & Steigman 2000; Ballantyne, Ferland, & Martin 2000; Sauer & Jeddanzik 2001). Finally, a recent study of different parts of a single H II region in the SMC finds that $Y = 0.241 \pm 0.002$ (Peimbert, Peimbert, & Ruiz 2000), at face value implying $Y_p \leq 0.241 \pm 0.002$.

Clearly, the final word on Y_p is not in. For now, because of the homogeneity and size of the Izotov & Thuan sample and the possible corruption of the other sample by stellar absorption, with caution we adopt $Y_p = 0.244 \pm 0.002$. (Had we adopted an intermediate value, with a systematic error reflecting the discrepancy between the two data sets, our conclusions would be largely the same.)

Using these choices, we have constructed separate likelihood functions for the baryon-to-photon ratio η from the abundances of D, D + ${}^3\text{He}$, ${}^4\text{He}$, and ${}^7\text{Li}$, assuming Gaussian distributions for the uncertainties (see Fig. 2). While the D, D + ${}^3\text{He}$, and ${}^4\text{He}$ abundances are all consistent with $\eta \approx 5 \times 10^{-10}$, most precisely pegged by D, the ${}^7\text{Li}$ abundance favors a significantly lower value. Combining these, we find that $\chi^2 = 23.2$ for 3 degrees of freedom (four abundances minus one parameter). This is the well-known lithium problem: the deuterium-inferred value for the baryon density predicts a ${}^7\text{Li}$ abundance that is about 3σ larger than that measured in old Population II halo stars (see, e.g., Burles et al. 1999 or Olive et al. 2000).

Since it is possible, and some stellar models suggest so, that there has been more depletion of ${}^7\text{Li}$ in old halo stars than the 5% inferred by Ryan (2000), we introduce the model parameter f_7 , which is the ratio of the inferred ${}^7\text{Li}/\text{H}$ in old Population II stars to its predicted primordial value. It quantifies how much the primordial ${}^7\text{Li}/\text{H}$ has been affected by additional stellar

depletion, cosmic-ray production, or theoretical difficulties (e.g., systematic errors in the nuclear cross sections or in the modeling of stellar atmospheres). An $f_7 \neq 1$ might also reflect fundamental problems, such as systematic problems with the deuterium abundance or inconsistencies in BBN.

Since there is no reason to believe that the present value of (D + ${}^3\text{He})/\text{H}$ in the local ISM is the primordial value, we introduce an analogous factor, f_{23} , which is the ratio of the present (D + ${}^3\text{He})/\text{H}$ to its primordial value. If $f_{23} = 1$, then the light-element abundances are consistent with the simple hypothesis that stars only convert D into ${}^3\text{He}$ during pre-MS burning, conserving D + ${}^3\text{He}$ by number; $f_{23} > 1$ indicates the additional net stellar production of ${}^3\text{He}$, and $f_{23} < 1$ indicates the net stellar destruction of ${}^3\text{He}$ after the pre-MS.

Figure 3 shows the distributions for f_7 and f_{23} , each marginalized over our other two parameters (e.g., the f_{23} curve results from marginalizing over η and f_7). The most likely value for f_7 is 0.32, with a 95% confidence interval of 0.20–0.55. That is, consistency between the deuterium-predicted ${}^7\text{Li}$ abundance and the Population II abundance requires a depletion of greater than a factor of 2 or some as yet unidentified source of systematic error in the BBN prediction or measurement. Such depletion can be achieved in stellar models and still be consistent with other observational constraints, including the plateau in ${}^7\text{Li}$ abundance in old Population II stars and the detection of ${}^6\text{Li}$ in several stars (see, e.g., Vauclair & Charbonnel 1995; Pinsonneault et al. 1999; Salaris & Weiss 2001).

The most likely value for f_{23} is 0.88, with a 95% confidence interval of 0.55–1.54. Unlike f_7 , this new parameter has essentially no effect on the question of concordance, and its value supports the simple hypothesis of only pre-MS ${}^3\text{He}$ production. It also disfavors stellar models that predict significant net ${}^3\text{He}$ production (or destruction) and is consistent with an earlier comparison of presolar and ISM measurements of D + ${}^3\text{He}$

TABLE 3
FITS TO THE CORRELATION COEFFICIENTS, $r_{j,k} = \sum_i a_i x^i$

Coefficient	j, k	a_0	a_1	a_2	a_3	a_4	a_5
Y_p	D	-0.8121	0.6430	3.3284	-7.2925	5.6748	-1.5914
	${}^3\text{He}$	0.2129	1.3468	-8.3646	15.8093	-12.8939	3.9055
	D + ${}^3\text{He}$	-0.8091	0.6468	3.3848	-7.4565	5.7605	-1.5838
	${}^7\text{Li}$	-0.3630	-0.1017	5.1531	-10.3563	7.5445	-1.8680
	${}^7\text{Be}$	0.7744	-0.3414	-4.0492	8.4836	-6.7167	1.9345
D	${}^3\text{He}$	-0.1924	-1.9722	8.2683	-13.6301	8.1108	-1.2999
	D + ${}^3\text{He}$	0.9995	-0.0238	0.1229	-0.2574	-0.1625	0.1352
	${}^7\text{Li}$	0.4219	0.2824	-0.9063	-6.9928	14.5503	-6.8278
	${}^7\text{Be}$	-0.8820	-0.0647	-0.4330	3.9867	-4.9394	1.6666
	D + ${}^3\text{He}$	-0.1526	-1.7701	7.2981	-9.4669	3.7557	0.1560
${}^3\text{He}$	${}^7\text{Li}$	-0.1321	-0.8465	3.1187	0.7518	-6.1419	2.9935
	${}^7\text{Be}$	0.3293	1.6390	-6.3839	8.9361	-4.2279	0.3574
	D + ${}^3\text{He}$	0.4186	0.3165	-1.2759	-6.0646	14.4155	-7.2783
D + ${}^3\text{He}$	${}^7\text{Li}$	-0.8744	-0.0455	-0.3596	3.9249	-4.6197	1.5773
	${}^7\text{Be}$	-0.4091	-0.1971	-0.5008	11.8943	-19.0115	8.0258

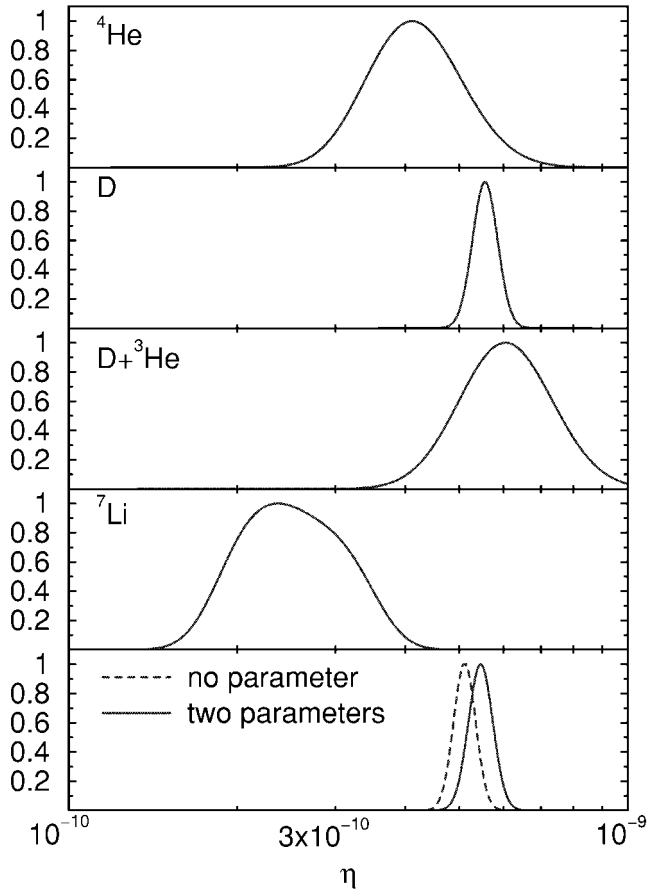


FIG. 2.—Likelihood functions, normalized to unit maximum, for η derived from single-abundance analyses (top four panels) and from a simultaneous analysis of all four abundances and their covariances (bottom panel). In the two-parameter analysis, the likelihood is marginalized over f_7 and f_{23} (see text).

that showed no evidence for an increase over the last 4.5 Gyr (Turner et al. 1996). This is somewhat surprising since the conventional models for the Galactic chemical evolution of ^3He predict a significant increase in $\text{D} + ^3\text{He}$ due to net ^3He production by low-mass stars (Iben & Truran 1978; Dearborn, Schramm, & Steigman 1986). However, Wasserburg, Boothroyd, & Sackmann (1995) argue that ^3He destruction by some low-mass stars is possible.

BBN and the light-element abundances can be used to fix the baryon-to-photon ratio at the end of BBN ($t \sim 200$ s). We have computed the likelihood function for the baryon density using the abundances of all four light elements and marginalizing over f_7 and f_{23} , giving all the weight to D and ^4He . We find that $\eta = (5.5 \pm 0.5) \times 10^{-10}$, shown as the “two-parameter” curve in Figure 2. The value is driven almost entirely by deuterium: using the deuterium alone, we find that $\eta = (5.6 \pm 0.5) \times 10^{-10}$.

To relate η to the present baryon density ($\Omega_b h^2$) one needs to know the present photon temperature ($T = 2.725 \pm 0.001$ K) and the average mass per baryon number [$\bar{m} = 1.6700$ (1.6701) $\times 10^{-24}$ g for the post-BBN mix (solar abundance)] and make the assumption that the expansion has been adiabatic since the BBN. Then η and the baryon density are related by $\Omega_b h^2 = (3.650 \pm 0.004) \times 10^7 \eta_{\text{BBN}}$. Within the standard cosmology, $\eta = (5.5 \pm 0.5) \times 10^{-10}$ translates to a baryon density,

$$\Omega_b h^2 = 0.020 \pm 0.002 \quad (95\% \text{ confidence}). \quad (2)$$

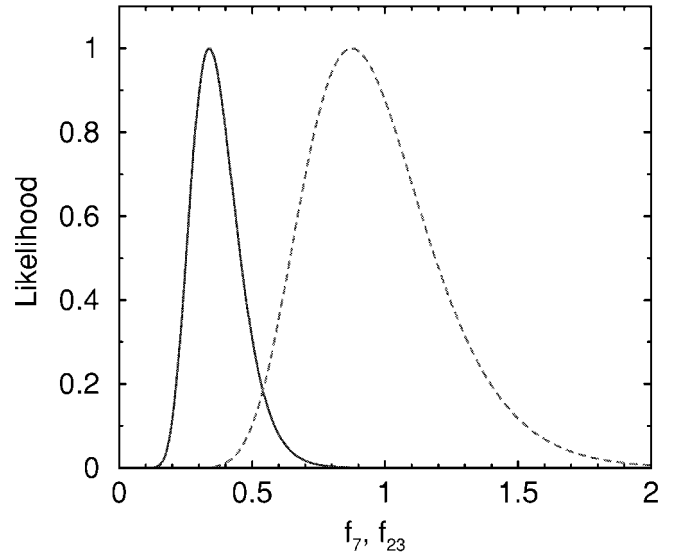


FIG. 3.—Marginalized likelihoods for f_7 (solid curve) and f_{23} (dashed curve).

Finally, we mention other recent likelihood analyses of BBN. Hata et al. (1995) addressed the consistency of BBN, focusing especially on ^4He and ^7Li (also see Copi, Schramm, & Turner 1995). Olive & Thomas (1997) and Fiorentini et al. (1998) carried out assessments of BBN using older estimates of the theoretical errors and a broader range for primordial D/H. The present analysis is the first using the new Nollett & Burles (2000) error estimates as well as the recently clarified primeval D/H.

4. CONCLUDING REMARKS

We have presented analytical fits for our new, more accurate predictions of the light-element abundances and their error matrix. These results have already renewed interest in more accurately determining key nuclear rates, and further improvements are likely (see, e.g., Schreiber et al. 2000; Rupak 2000).

Using our results and the primeval deuterium abundance from three high-redshift Ly α systems, we infer that $\Omega_b h^2 = 0.020 \pm 0.002$ (95% confidence level). For $h = 0.7 \pm 0.07$, this implies a baryon fraction $\Omega_b = 0.041 \pm 0.009$, with the error dominated by that in H_0 . Measurements of cosmic microwave background (CMB) anisotropy have recently also determined the baryon density. The physics underlying this method is very different—gravity-driven acoustic oscillations in the universe at 500,000 yr—but the result is similar: $\Omega_b h^2 = 0.032^{+0.009}_{-0.008}$ at a 95% confidence level (Jaffe et al. 2000). While there is about a 2σ difference, this first result from CMB anisotropy confirms the long-standing BBN prediction of a low baryon density and, with it, the need for nonbaryonic dark matter.

The sum of $\text{D} + ^3\text{He}$ predicted for the deuterium baryon density is consistent with that in the ISM today, implying no significant production (or destruction) of ^3He beyond pre-MS burning. The deuterium-predicted ^4He abundance is an important consistency test of BBN; however, a systematic measurement error (the Y_p -values from the two key data sets differ by 5 times the statistical error) precludes firm conclusions at this time. Likewise, the discrepancy between the predicted ^7Li abundance and the abundance measured in Population II stars has no simple explanation: the discrepancy could indicate that ^7Li

has been depleted in Population II stars by about a factor of 2, that uncertainties (in observations or predictions) have been

grossly underestimated, or that there is an inconsistency in BBN.

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