BAND POWER SPECTRA IN THE COBE¹ DMR FOUR-YEAR ANISOTROPY MAPS

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ABSTRACT

We employ a pixel-based likelihood technique to estimate the angular power spectrum of the *COBE* Differential Microwave Radiometer (DMR) 4 yr sky maps. The spectrum is consistent with a scale-invariant power-law form with a normalization, expressed in terms of the expected quadrupole anisotropy, of $Q_{\text{rms-PS}/n=1} = 18 \pm 1.4 \,\mu\text{K}$, and a best-fit spectral index of 1.2 ± 0.3 . The normalization is somewhat smaller than we concluded from the 2 yr data, mainly due to additional Galactic modeling. We extend the analysis to investigate the extent to which the "small" quadrupole observed in our sky is statistically consistent with a power-law spectrum. The most likely quadrupole amplitude ranges between 7 and 10 μ K, depending on the details of Galactic modeling and data selection, but in no case is there compelling evidence that the quadrupole is inconsistent with a power-law spectrum. We conclude with a likelihood analysis of the band power amplitude in each of four spectral bands between $\ell = 2$ and 40, and find no evidence for deviations from a simple power-law spectrum.

Subject headings: cosmic microwave background - cosmology: observations

1. INTRODUCTION

The detection of large angular scale anisotropies in the cosmic microwave background (CMB) radiation was first reported by the *COBE* DMR experiment in 1992 (Smoot et al. 1992; Bennett et al. 1992; Wright et al. 1992; Kogut et al. 1992). The initial detection was based only on the first year of flight data. Since that time the DMR team processed and analyzed the first two years of data and found results to be consistent with the first-year results (Bennett et al. 1994; Górski et al. 1994; Wright et al. 1994a). We have now processed and analyzed the full four years of DMR observations: this Letter is one of a series describing the results of our analysis. The maps and an overview of the scientific results are given in Bennett et al. (1996).

In this Letter we analyze the angular power spectrum of the 4 yr DMR maps using a pixel-based likelihood technique. The method was pioneered by Bond (1995a, 1995b) who applied it to the 1 and 2 yr DMR data, respectively. His method involves expanding the data using a Karhunen-Loève expansion; however, the method is equivalent to ours in the limit that the number of modes in the expansion equals the number of pixels in the map. The method was also applied to the 2 yr data by Tegmark & Bunn (1995). We extend previous work by con-

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sidering several parameterizations of the angular power spectrum. The simplest model for large angular scale anisotropy is the power-law model parameterized by a normalization, $Q_{\rm rms-PS}$, and spectral index, n. It is of interest to separate the quadrupole anisotropy from the rest of the power spectrum since it is most plausibly contaminated by Galactic emission, and, in some models such as some cosmic texture models, is predicted to deviate from the simple power-law form. We extend our likelihood analysis to a three-parameter model in which the quadrupole is fitted independently of the higher order power (which is assumed to follow a power law, see § 3 for details). Lastly we consider band power estimates in which the anisotropy is assumed to be scale-invariant in each of four modestly narrow ℓ bands, chosen to have roughly comparable sensitivity. The results are compared to the power-law fits and indicate that the anisotropy has no significant deviation from a power-law form.

2. DATA SELECTION AND METHOD

The DMR experiment has produced two independent microwave maps (A and B) at each of three frequencies (31.5, 53, and 90 GHz). The results presented here are based on linear combinations of all six channel maps. The combination coefficients are dictated by the sensitivities of the individual channels and on considerations of Galactic foreground removal. Kogut et al. (1996a, 1996b) have analyzed Galactic emission in the 2 and 4 yr DMR data at high latitudes, and conclude that there is statistically significant evidence for a weak Galactic signal at all three frequencies, even at latitudes $|b| \ge 20^{\circ}$. Thus, for the 4 yr analysis, we approach Galactic foreground removal as follows: first, we extend the Galactic plane cut of 20° with additional cuts, guided by the *COBE* DIRBE 140 µm map (Bennett et al. 1996). Second, we model and remove residual high-latitude Galactic emission in two complementary ways described below. Altogether, we analyze three separate maps in this paper. The first map is a weighted average of all six DMR channel maps with no residual Galaxy emission subtracted; we denote this map "31 + 53 + 90." The second is the same weighted average map as the first with

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best-fit Galaxy template maps subtracted from each channel prior to averaging (Kogut et al. 1996b); we denote this the "correlation" model map. The third is a linear combination of all six channels with coefficients designed to maximize sensitivity subject to the constraint that any signal with a free-free frequency spectrum ($\beta_{\rm ff} = -2.15$) cancels. This map also has best-fit synchrotron and dust emission templates subtracted prior to averaging (Kogut et al. 1996b). We denote this the "combination" model map. The specific coefficients used to construct these maps are given in Table 1 of Hinshaw et al. (1996). In all the analyses below we use the maps pixelized in Galactic coordinates.

Most cosmological models make predictions for the mean angular power spectrum of CMB anisotropies, the coefficients, C_{ℓ} . For a rotationally invariant theory, the C_{ℓ} specify the expected variance in each spherical harmonic mode in a Fourier expansion of the sky temperature $T(\theta, \phi) = \sum_{\ell,m} a_{\ell m} Y_{\ell m}(\theta, \phi)$ with $\langle a_{\ell m} a^*_{\ell' m'} \rangle = C_{\ell} \delta_{\ell \ell'} \delta_{mm'}$. For a given power spectrum, C_{ℓ} , the implied covariance between map pixels *i* and *j* is given by

$$M_{ij} = \langle T_i T_j \rangle = \frac{1}{4\pi} \sum_{\ell} (2\ell + 1) W_{\ell}^2 C_{\ell} P_{\ell}(\hat{\boldsymbol{n}}_i \cdot \hat{\boldsymbol{n}}_j), \quad (1)$$

where T_i is the temperature in pixel *i* of a map, the angle brackets denote a universal ensemble average, W_ℓ^2 is the experimental window function that includes the effects of beam smoothing and finite pixel size (see below), C_ℓ is the power spectrum, $P_\ell(\hat{n}_i \cdot \hat{n}_j)$ is the Legendre polynomial of order ℓ , and \hat{n}_i is the unit vector toward the center of pixel *i*. For Gaussian fluctuations, the covariance matrix fully specifies the statistics of the temperature fluctuations. The probability of observing a map with pixel temperatures T, given a power spectrum C_ℓ , is

$$P(T|C_{\ell}) dT = \frac{dT}{(2\pi)^{N/2}} \frac{e^{-1/2T^{T} \cdot M(C_{\ell})^{-1} \cdot T}}{\sqrt{\det M(C_{\ell})}}, \qquad (2)$$

where *N* is the number of pixels in the map. Assuming a uniform prior distribution of cosmological model parameters, the probability of a power spectrum C_{ℓ} , given a map *T*, is then $\mathscr{L}(C_{\ell}|T) \propto [\det M(C_{\ell})]^{-(1/2)} \exp \left[-\frac{1}{2}T^{T} \cdot M^{-1}(C_{\ell}) \cdot T\right].$

In the following section, we evaluate the above likelihood function using three different parameterizations of the power spectrum, C_{ℓ} . To test the effects of data selection and Galaxy modeling, we analyze three separate DMR maps, as specified above. To make the analysis computationally efficient, we have degraded the maps by one step in pixel resolution (to index level 5) for which there are 1536 pixels in the full sky and 954 pixels surviving the extended Galaxy cut. We account for the effects of smoothing due to pixelization by including a term in the window function: $W_{\ell} = G_{\ell}F_{\ell}$. The G_{ℓ} are the Legendre coefficients of the DMR beam pattern, tabulated by Wright et al. (1994b). The F_{ℓ} are the Legendre coefficients for a circular top-hat function with area equal to the pixel area. The coefficients for index level 5 pixels are available on request.

We ignore the contribution of the monopole and dipole moments in the maps since these modes are either unconstrained by the data (the monopole), or dominated by local effects (the dipole). In principle, this is achieved by integrating the likelihood over the modes C_0 and C_1 , or, equivalently, by letting C_0 , $C_1 \rightarrow \infty$ in equation (1). In practice, we have found that setting $C_0 = C_1 = 10^8 \ \mu \text{K}^2$ renders the likelihood insensitive to monopole and dipole moments of several hundred μ K, without compromising the inversion of the covariance matrices. This is more than sufficient for our application since the analyzed maps have approximately zero mean by construction, and approximately zero dipole since an estimate of the CMB dipole is removed during the raw data processing. We assume the noise in the sky maps is uncorrelated from pixel to pixel (Lineweaver et al. 1994), which adds a diagonal contribution to the pixel covariance matrix in equation (1). Tegmark & Bunn (1995) have shown the assumption of uncorrelated noise to be an excellent approximation for this application. The noise per pixel is derived from the noise per observation, given in Bennett et al. (1996), and the number of observations per pixel.

3. RESULTS

We consider three parameterizations of the angular power spectrum. First, we adopt the power-law model, parameterized by the amplitude of the mean quadrupole anisotropy, $Q_{\rm rms-PS}$, and the power-law spectral index *n*. Specifically (Bond & Efstathiou 1987)

$$C_{\ell} = C_{\ell}(Q_{\rm rms-PS}, n)$$

= $(4\pi/5)Q_{\rm rms-PS}^2 \frac{\Gamma[\ell + (n-1)/2]\Gamma[(9-n)/2]}{\Gamma[\ell + (5-n)/2]\Gamma[(3+n)/2]}.$ (3)

This model is extended to study the quadrupole anisotropy by parameterizing the power at $\ell = 2$ separately:

$$C_{\ell} = \begin{cases} C_2, & \ell = 2, \\ C_{\ell}(Q_{\text{rms-PS}}, n), & \ell \ge 3. \end{cases}$$
(4)

The most likely value of C_2 that results from this model is closely related to the quadrupole anisotropy observed in our sky, which we denote $Q_{\rm rms}$; the precise connection is discussed below. Note also that the power-law parameters, $Q_{\rm rms-PS}$ and n, inferred from this model are essentially the same as those derived from marginalizing over C_2 since they are only weakly coupled to C_2 . Lastly, we study a model in which the spectrum is taken to be scale-invariant in each of four relatively narrow ℓ bands, and let the amplitude in each be a free parameter:

$$\ell(\ell+1)C_{\ell} = \begin{cases} (24\pi/5)Q_{\alpha}^{2}, & 2 \le \ell \le 5, \\ (24\pi/5)Q_{\beta}^{2}, & 6 \le \ell \le 10, \\ (24\pi/5)Q_{\gamma}^{2}, & 11 \le \ell \le 20, \\ (24\pi/5)Q_{\delta}^{2}, & 21 \le \ell \le 40. \end{cases}$$
(5)

Note that within each band, the amplitude parameters $Q_{\alpha..\delta}$ correspond to Q_{flat} as defined by Scott, Silk, & White (1995). The spectral band widths were chosen to give roughly equal sensitivity in each band except the highest which suffers loss of signal due to the 7° beam width. The model is designed to probe for deviations from a power law while maintaining computational feasibility.

The fits to power-law spectra, including the quadrupole in the analysis, are summarized in the first half of Table 1. The results are generally consistent with the 2 yr data. The overall normalization is slightly smaller due to the additional Galactic cutting and modeling. The most likely spectral index is slightly greater than unity, while the quadrupole normalization for a scale-invariant spectrum ranges from 17.2 to 18.4 μ K, depending on Galactic model. For comparison, the scale-invariant

POWER-LAW SPECIRAL PARAMETERS						
Map ^a	n ^b	$Q_{ m rms-PS}{}^{ m b}_{(\mu m K)}$	$Q_{\mathrm{rms-PS} n=1}^{\mathrm{c}} (\mu \mathrm{K})^{\mathrm{c}}$	$Q_{ m rms}^{\ b}$ $(\mu{ m K})$		
	Pure	e Power Law				
31 + 53 + 90	$1.25^{+0.26}_{-0.29}$	$15.4^{+3.9}_{-2.9}$	$18.4^{+1.4}_{-1.3}$			
Correlation	$1.23\substack{+0.26\\-0.27}$	$15.2^{+3.6}_{-2.8}$	$17.8^{+1.3}_{-1.3}$			
Combination	$1.00\substack{+0.40\\-0.43}$	$17.2\substack{+5.6\\-4.0}$	$17.2^{+1.9}_{-1.7}$			
	Quadrup	ole + Power I	.aw			
31 + 53 + 90	$1.09\substack{+0.29\\-0.30}$	$17.5^{+4.7}_{-3.6}$	$18.7^{+1.4}_{-1.3}$	$6.9^{+5.4}_{-2.7}$		
Correlation	$1.09\substack{+0.29\\-0.31}$	$17.0^{+4.7}_{-3.6}$	$18.1^{+1.4}_{-1.3}$	$10.0\substack{+6.5\\-4.4}$		
Combination	$0.57^{+0.44}_{-0.49}$	$23.0^{+8.4}_{-5.7}$	$17.9^{+1.9}_{-1.8}$	$7.6^{+6.2}_{-4.5}$		

TABLE 1

^a Linear combination coefficients for the maps analyzed here are given in Table 1 of Hinshaw et al. (1996).

^b Table entries specify the mode and $\pm 68\%$ confidence interval for the projection of the two- or three-dimensional likelihood, $\mathscr{L}(Q_{\rm rms-PS}, n)$ or $\mathscr{L}(Q_{\rm rms}, Q_{\rm rms-PS}, n)$, onto a single parameter.

^c Table entries for $Q_{\text{rms}-\text{PS}|n=1}$ specify the mode and $\pm 68\%$ confidence interval for the slice of the two- or three-dimensional likelihood at n = 1 (projecting over Q_{rms} in the latter case).

normalization derived from the weighted average map using a straight 20° cut with no additional Galactic modeling is 20.1 μ K, 1.6 μ K higher than we obtain with the extended cut, and comparable to the normalization quoted by Górski et al. (1994) for the 2 yr data (using a straight cut). In assessing the results obtained from the three maps, we note that the DIRBE 140 μ m map appears to trace the bulk of the free-free emission seen by DMR (Kogut et al. 1996b), and since the correlation map is more sensitive than the combination map, we give it more weight in our conclusions. Taken together, the results in Table 1 are consistent with a spectral index of 1.2 \pm 0.3 and a scale-invariant quadrupole normalization of 18 \pm 1.4 μ K.

The fits to power-law spectra with the quadrupole parameterized independently are summarized in the second half of Table 1. The first three columns summarize the power-law portion of the spectrum. These results are based on projecting the three-dimensional likelihood over the quadrupole C_2 . The last column of Table 1 gives the 68% confidence interval for C_2 expressed in terms of $\bar{Q}_{\rm rms} \equiv [(5/4\pi)C_2]^{1/2}$. The mode gives a self-consistent estimate of the quadrupole moment observed in our sky, while the confidence range accounts for both instrument noise and cosmic variance. A complimentary approach to analyzing the quadrupole, based on fitting and squaring a_{2m} coefficients (Kogut et al. 1996b) gives consistent results, after accounting for the bias introduced by uncertainties in the a_{2m} . As with previous analyses, the observed quadrupole is smaller than that expected from the power-law fits: the most likely amplitude ranges from 6.9 to 10.0 μ K depending on Galaxy model. Figure 1 shows the full likelihood for $Q_{\rm rms}$ for each map analyzed. It is important to stress that while the quadrupole in our sky is most likely $\sim 10 \ \mu K$, the cosmic variance combined with experimental uncertainties are so large that its value is easily consistent with a power-law model of anisotropy. For example, the likelihood for $Q_{\rm rms}$ derived from the correlation map implies there is a 22% chance that $Q_{\rm rms}$ exceeds 18 μ K, the value favored in a scale-invariant power-law model.

The band power fits are summarized in Table 2, and are



FIG. 1.—Likelihood function for the mean quadrupole moment observed in our sky for the three maps defined in § 2. Curves include cosmic variance and instrument noise. In all cases the most likely quadrupole is smaller than that favored by the power-law fits to the full data, but the likelihoods are all sufficiently broad to encompass the case $Q_{\rm rms} = Q_{\rm rms-PS}$. The effect of Galactic modeling on $Q_{\rm rms}$ is relatively modest, but it does have a significant effect on the phase of the quadrupole, particularly the coefficient a_{20} (Kogut et al. 1996b).

plotted in Figure 2. The vertical uncertainties in the figure indicate the extent of the 68% confidence interval in each band power parameter when the other three are fixed at their maximum likelihood value. These uncertainties include both instrument noise and cosmic variance. The horizontal error bars represent the extent of each band, as defined in equation (5). The covariance between bands, which arises from the Galaxy cut and from nonuniform sky coverage, is quite small. Defining $\sigma_{ij}^2 = \int dQ_i dQ_j \mathcal{L}'(Q_i, Q_j)(Q_i - \langle Q_i \rangle)(Q_j - \langle Q_j \rangle),$ where \mathcal{L}' is a two-dimensional likelihood with the remaining parameters fixed at their most likely values, we find $\sigma_{ii}/\sigma_{ii} < 0.1$ for nearest neighbor bands, with smaller limits for non-neighboring bands. Note that each of the three lowest bands have consistently significant detections of power, while, in all cases, the highest band, $\ell = 21-40$, does not. Thus, we only plot 95% confidence upper limits for this band. To compare the band power fits to the power-law fits we have also

TABLE 2 BAND POWER SPECTRAL PARAMETERS^a

	Band					
MAP ^b	$2 \le \ell \le 5$	$6 \leq \ell \leq 10$	$11 \leq \ell \leq 20$	$21 \le \ell \le 40$		
31 + 53 + 90 Correlation Combination	$18.6^{+4.5}_{-3.4}\\18.0^{+3.6}_{-2.6}\\17.5^{+4.7}_{-3.7}$	$16.7^{+2.4}_{-2.0} \\ 15.9^{+2.3}_{-1.8} \\ 17.2^{+2.9}_{-2.5}$	$20.3^{+2.2}_{-2.1} \\ 19.9^{+2.2}_{-2.0} \\ 17.2^{+4.6}_{-4.7}$	$\begin{array}{c} 1.0^{+13.2}_{-1.0} \\ 0.8^{+12.6}_{-0.8} \\ 0.1^{+22.2}_{-0.1} \end{array}$		

^a Mode and $\pm 68\%$ confidence interval for the band power amplitudes, expressed in terms of $Q_{\rm flat}$. $Q_{\rm flat}$ is the quadrupole normalization expected for a scale-invariant power-law spectrum within the specified range of ℓ . The units are μ K.

are μK . ^b Linear combination coefficients for the maps analyzed here are given in Table 1 of Hinshaw et al. (1996).



FIG. 2.—Power spectral estimates for the three maps defined in § 2. Points with error bars give the most likely band power amplitude within each ℓ band, as indicated by the horizontal error bars, under the assumption that the power spectrum is scale-invariant within each band. The fourth band, $21 \le \ell \le 40$, is plotted as a 95% CL upper limit, since there is no significant detection of power in this band. Vertical errors include both noise and cosmic variance. The shaded region indicates the locus of the mean of acceptable power-law models, i.e., those models within the 68% confidence region in the $(Q_{\rm rms-PS}, n)$ plane, as determined from the power-law fits to each map. Dashed white line within the shaded region gives the mean power spectrum for the most likely power-law model. Note that any given realization of a power-law spectrum will, in general, deviate from the mean spectra plotted here due to cosmic variance.

plotted the 68% confidence locus of acceptable power-law models in Figure 2. More precisely, the dashed white line in the figure is the mean power spectrum for the most likely power-law model, while the gray band represents the locus of mean power spectra within the 68% confidence region in the

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 $(Q_{\rm rms-PS}, n)$ plane. The general agreement between the powerlaw model and the band power model is an indication that there are no significant wideband deviations (with $\Delta \ell \sim a$ few) from a simple power-law in the low- ℓ anisotropy spectrum. The band power amplitude in the highest ℓ band we probe is consistently low, but this estimate is rather sensitive to the details of the beam and pixelization filters, and to the level of noise in the maps, so the uncertainty attached to this estimate is quite large. To date, two other experiments have measured anisotropy on angular scales probed by the DMR: FIRS (Ganga et al. 1994) and Tenerife (Hancock et al. 1994). Both experiments report significant detections of anisotropy: the FIRS team quotes $Q_{\text{flat}} = 19 \pm 5 \ \mu\text{K}$ for $\ell \lesssim 30$, while the Tenerife team quotes $Q_{\text{flat}} = 26 \pm 6 \ \mu\text{K}$ for $13 \lesssim \ell \lesssim 30$, both of which are consistent with DMR.

4. CONCLUSIONS

We have estimated various parameterizations of the angular power spectrum in the COBE DMR 4 yr sky maps. We find the results to be generally consistent with the first and second year results. The data are consistent with a scale-invariant spectrum with a quadrupole normalization of $18 \pm 1.4 \,\mu\text{K}$, and a best-fit spectral index of 1.2 ± 0.3 . The quadrupole anisotropy is somewhat smaller than the best-fit power-law spectrum would prefer, but the discrepancy is not statistically significant when we take account of Galactic modeling uncertainties, instrument noise, and cosmic variance. We have further analyzed the spectrum in each of four ℓ bands and find no evidence for significant, wideband deviations from a simple power-law form.

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