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Soft rescattering in DIS: effects of helicity flip

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ABSTRACT: Soft rescattering in hard QCD processes may involve non-perturbative, chiral symmetry breaking interactions. We find that rescattering which changes the helicity of the struck quark gives rise to a leading twist single spin asymmetry in semi-inclusive DIS, the angular dependence of which is the same as that usually ascribed to the Collins effect. We argue that helicity-changing rescattering can contribute also to $k_{\perp}$ -integrated parton distributions.

KEYWORDS: Deep Inelastic Scattering, Spin and Polarization Effects, QCD.

Contents

1. Introduction	1
2. Single spin asymmetry with Pauli coupling in the BHS model	2
2.1 The amplitudes	3
2.2 Evaluation of the asymmetry	5
3. Concluding remarks	6

1. Introduction

Deep Inelastic Scattering (DIS, $e + N \rightarrow e + X$) is non-local on the light-cone ($x^2 = 0$). Some time ago it was noted [1, 2] that soft rescattering occurring within the finite Ioffe coherence length along the light-cone has physical, observable effects such as shadowing and diffraction. Studies of perturbative model amplitudes have led to broad agreement that such rescattering enables a single spin asymmetry (A_N) at leading twist [3, 4], the “Sivers” effect [5] in semi-inclusive DIS. In the model proposed by Brodsky, Hwang and Schmidt (BHS, [3]) a transverse spin asymmetry arises from the interference of the Born term with the absorptive part of the one-loop amplitude, and is thus proportional to an elastic, on-shell rescattering amplitude of the struck quark. It is recognized that such calculations are not quantitatively reliable due to the softness of the rescattering. However, it appears unlikely that a non-vanishing effect thus established would be cancelled by the non-perturbative sector of QCD.

In this paper we consider what effects the specifically non-perturbative features of QCD may have on A_N . Due to spontaneous chiral symmetry breaking the helicity of massless quarks need not be conserved in soft processes. *E.g.*, instantons can generate a Pauli-type coupling (anomalous magnetic moment) of quarks to gluons [6]. We use the BHS model to study the effect on A_N of adding a Pauli coupling at the vertex between the struck quark and the exchanged gluon,

$$-ig_s\gamma^\mu \rightarrow -ig_s\gamma^\mu + a(p^2)\sigma^{\mu\nu}p_\nu \quad (1.1)$$

where the effective coupling $a(p^2)$ vanishes at large virtualities p^2 of the gluon.

We present our calculation in the next section. However, one can qualitatively anticipate the result. The remarkable fact that a soft gluon can be coherent with the hard photon (of virtuality $Q^2 \rightarrow \infty$) is a consequence of Lorentz dilation. The proper coherence length $1/Q$ of the virtual photon is dilated by a factor $\gamma = \nu/Q$ in the target rest frame,

where the photon has energy ν . Thus the Ioffe coherence length is finite in the Bjorken limit, and inversely proportional to x_B ,

$$L_I = \frac{1}{Q} \cdot \frac{\nu}{Q} = \frac{1}{2Mx_B} \quad (1.2)$$

where M is the target mass. Note that soft interactions with partons that are *comoving* with the struck quark (i.e., which emerge in the current fragmentation region), do not benefit from the dilation factor and thus are incoherent with the hard process. This is why hadronization does not influence the DIS cross section at leading twist.

For the rescattering to be relevant its cross section must be constant in the high energy ($\nu \rightarrow \infty$) limit, i.e., the rescattering amplitude must be $\propto \nu$. This is indeed the case for longitudinal gluon exchange, whereas transverse gluon exchange does not contribute. It is readily checked that also the Pauli part of the vertex in (1.1) gives an elastic amplitude $\propto \nu$. This leads one to expect that the Pauli coupling will contribute to A_N , which is caused by an interference between amplitudes where the target has opposite helicity. As we shall see, the azimuthal dependence of this new contribution is the same as that of the Collins effect [7].

2. Single spin asymmetry with Pauli coupling in the BHS model

We study the single transverse-spin asymmetry in semi-inclusive DIS using the BHS model [3], in which a target quark emits a scalar particle before being struck by the virtual photon (cf. figure 1). We evaluate the effect of an anomalous magnetic moment (Pauli coupling) in the rescattering of the struck quark. Such a coupling might be generated non-perturbatively, due to the softness of the rescattering gluon.

The spin asymmetry for a target polarized in the transverse (y) direction is defined as

$$A_N \equiv \frac{\sum_{\{\sigma\}} [|\mathcal{M}_{\uparrow, \{\sigma\}}|^2 - |\mathcal{M}_{\downarrow, \{\sigma\}}|^2]}{\sum_{\{\sigma\}} [|\mathcal{M}_{\uparrow, \{\sigma\}}|^2 + |\mathcal{M}_{\downarrow, \{\sigma\}}|^2]} = \frac{2 \sum_{\{\sigma\}} \text{Im} [\mathcal{M}_{\leftarrow, \{\sigma\}}^* \mathcal{M}_{\rightarrow, \{\sigma\}}]}{\sum_{\{\sigma\}} [|\mathcal{M}_{\rightarrow, \{\sigma\}}|^2 + |\mathcal{M}_{\leftarrow, \{\sigma\}}|^2]} \quad (2.1)$$

where the $\mathcal{M}_{\leftarrow, \{\sigma\}}$ are helicity amplitudes and $\{\sigma\}$ represents the helicities of all particles except the target. The asymmetry vanishes at Born level but can get a contribution from the interference between the Born amplitude and the absorptive part of the one-loop amplitude. We study the asymmetry which arises when a Pauli coupling is used at the quark-gluon vertex of the rescattering in figure 1c.

We introduce the Pauli coupling through the replacement (1.1) at the quark-gluon vertex, where p is the (incoming) gluon momentum. In the absorptive part of the rescattering amplitude the quark is on-shell. If the Pauli contribution arises from non-perturbative effects $a(p^2)$ should vanish at large virtualities $-p^2$ of the exchanged gluon. For our purposes the precise dependence on p^2 is not important, we take

$$a(p^2) = a_0 e^{Ap^2} \quad (2.2)$$

where a_0 and A are constants.

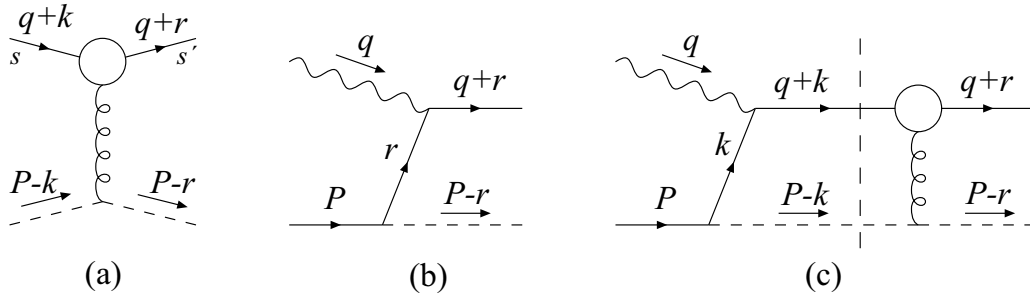


Figure 1: Amplitudes which contribute to the asymmetry. The blob represents the Pauli coupling in (1.1). (a) Elastic scattering amplitude with Pauli coupling. (b) The Born amplitude. (c) The discontinuity of the loop amplitude.

We use a coordinate system where the virtual photon momentum is along the $+z$ axis and the target is at rest, i.e., the photon and target momenta read

$$\begin{aligned} q &= (q^+, q^-, 0_\perp) \simeq (2\nu, -x_B M, \mathbf{0}_\perp) \\ P &= (M, M, \mathbf{0}_\perp) \end{aligned} \quad (2.3)$$

where ν is the photon energy, M is the target mass and $x_B \equiv Q^2/2M\nu$ is the Bjorken variable. The struck quark thus gets a large momentum in the $+z$ direction, making the use of the standard light-front (LF) spinors defined in [8] convenient. We evaluate the asymmetry A_N at leading twist with finite target and scalar masses M and m_s , taking the quark mass m to be zero.

2.1 The amplitudes

The relevant amplitudes are shown in figure 1. The Pauli coupling contribution to the on-shell elastic quark-scalar amplitude (figure 1a) is given by

$$i\mathcal{M}_{ss'}^{\text{el}} \equiv \bar{u}(q+r, s') a_0 e^{A(k-r)^2} \sigma^{\mu\nu} u(q+k, s) (r_\nu - k_\nu) (2P_\mu - k_\mu - r_\mu) \frac{-i}{(k-r)^2} (-ie_2) \quad (2.4)$$

with the LF spinors defined in [8]. The helicity of the (massless) quark flips at the Pauli vertex: only the spin flip amplitudes are non-zero. Their leading behavior in the limit of $q^+ \rightarrow \infty$ at fixed k, r is

$$\mathcal{M}_{+-}^{\text{el}} \simeq 2a_0 e_2 \frac{(1-x_B)Mq^+ (k_\perp e^{+i\phi} - r_\perp e^{+i\psi})}{(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} e^{-A(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} \simeq -\left(\mathcal{M}_{-+}^{\text{el}}\right)^* \quad (2.5)$$

where we used $k^- \simeq r^- \simeq Mx_B$ (as required for the quarks to be on-shell, with $q^- \simeq -Mx_B$) and denoted

$$\begin{aligned} \mathbf{k}_\perp &= k_\perp (\cos \phi, \sin \phi) \\ \mathbf{r}_\perp &= r_\perp (\cos \psi, \sin \psi). \end{aligned} \quad (2.6)$$

Note that the amplitudes (2.5) are proportional to $s \simeq Mq^+$. This is required for the Pauli coupling to contribute at leading twist in figure 1c.

The Born amplitude of figure 1b reads

$$i\mathcal{A}_{ss'}^\lambda \equiv \bar{u}(q+r, s')(-ie_1 \not{\epsilon}^\lambda) \frac{i \not{r}}{r^2} (-ig) u(P, s) \quad (2.7)$$

where $u(P, s)$ is the target spinor (of mass M). At leading twist only transversely polarized photons contribute, with polarization vectors $\epsilon^{\lambda=\pm 1} \equiv -(0, 0, \pm 1, i)/\sqrt{2}$. We get¹

$$\begin{aligned} \mathcal{A}_{++}^\lambda &\simeq e_1 g \sqrt{2Mq^+} \frac{1-x_B}{r_\perp^2 + B} r_\perp e^{+i\psi} \delta_{\lambda,+1} \\ \mathcal{A}_{+-}^\lambda &\simeq e_1 g \sqrt{2Mq^+} \frac{1-x_B}{r_\perp^2 + B} M x_B \delta_{\lambda,-1} \end{aligned} \quad (2.8)$$

where

$$B \equiv x_B [m_s^2 - (1-x_B)M^2]. \quad (2.9)$$

The remaining helicity amplitudes are obtained through

$$\mathcal{A}_{ss'}^\lambda = -(-1)^{s-s'} \left(\mathcal{A}_{-s,-s'}^{-\lambda} \right)^* \quad (2.10)$$

where $s, s' = \pm \frac{1}{2}$. The amplitudes $\mathcal{M}$ in (2.1) involve also the contribution from the lepton vertex. The denominator of (2.1) is (at lowest order) given by the Born amplitude through

$$\mathcal{N} \equiv \sum_{\{\sigma\}} [|\mathcal{M}_{\rightarrow, \{\sigma\}}|^2 + |\mathcal{M}_{\leftarrow, \{\sigma\}}|^2] = \frac{1}{Q^4} \sum_{s,s'} \sum_{\lambda,\lambda'} L^{\lambda,\lambda'} \mathcal{A}_{ss'}^\lambda (\mathcal{A}_{ss'}^{\lambda'})^*. \quad (2.11)$$

Defining the transverse momentum of the leptons as

$$\mathbf{l}_{1\perp} = \mathbf{l}_{2\perp} = l_\perp (\cos \tau, \sin \tau) \quad (2.12)$$

the dependence on the lepton momenta l_1, l_2 is given by

$$L^{\lambda,\lambda'} = \frac{2e^2 Q^2}{y^2} \left\{ [1 + (1-y)^2] \delta_{\lambda,\lambda'} - 2(1-y) e^{-2i\lambda\tau} \delta_{\lambda,-\lambda'} \right\} \quad \text{for } \lambda, \lambda' = \pm 1 \quad (2.13)$$

where $y \equiv P \cdot q / P \cdot l_1$ is the fraction of the beam energy carried by the virtual photon. The helicity dependence of the Born amplitudes (2.8) restricts the photon helicities in (2.11) to $\lambda = \lambda' = \pm 1$. Using (2.13) we find

$$\mathcal{N} = \frac{8e^2}{y^2 Q^2} [1 + (1-y)^2] (e_1 g)^2 M q^+ \left(\frac{1-x_B}{r_\perp^2 + B} \right)^2 [r_\perp^2 + (M x_B)^2]. \quad (2.14)$$

The loop amplitude is shown in figure 1c. Only its discontinuity (absorptive part) contributes to the asymmetry (2.1). According to the Cutkosky rules the discontinuity is given by a convolution of the amplitudes (2.5) and (2.8):

$$\begin{aligned} \text{Disc } \mathcal{B}_{ss'}^\lambda &\equiv i \int \frac{d^4 k}{(2\pi)^4} 2\pi \delta[(k+q)^2] 2\pi \delta[(P-k)^2 - m_s^2] \mathcal{A}_{s,-s'}^\lambda \mathcal{M}_{-s',s'}^{\text{el}} \\ &\simeq \frac{i}{2(1-x_B)Mq^+} \int \frac{d^2 \mathbf{k}_\perp}{(2\pi)^2} \mathcal{A}_{s,-s'}^\lambda \mathcal{M}_{-s',s'}^{\text{el}} = (-1)^{s-s'} \left(\text{Disc } \mathcal{B}_{-s,-s'}^{-\lambda} \right)^* \end{aligned} \quad (2.15)$$

where $\mathcal{A}_{s,-s'}^\lambda$ is to be expressed in terms of the quark momentum k rather than r as in (2.8).

¹Here the spin non-flip amplitudes are proportional to the proton mass M whereas in the original BHS model they were $\propto r_\perp$. This is due to our choice of frame (2.3).

2.2 Evaluation of the asymmetry

The single spin asymmetry (2.1) is given by the amplitudes (2.8) and (2.15) as

$$\begin{aligned}\mathcal{N}A_N &\simeq \frac{2}{Q^4} \sum_{\lambda, \lambda'} \sum_{s'} \text{Im} \left\{ L^{\lambda, \lambda'} \left[\mathcal{A}_{+, s'}^\lambda + \frac{1}{2} \text{Disc } \mathcal{B}_{+, s'}^\lambda \right] \left[\mathcal{A}_{-, s'}^{\lambda'} + \frac{1}{2} \text{Disc } \mathcal{B}_{-, s'}^{\lambda'} \right]^* \right\} \\ &= \frac{8e^2}{Q^2} \frac{1-y}{y^2} \sum_{\lambda=\pm 1} \text{Im} \left\{ \lambda e^{-2i\lambda\tau} \mathcal{A}_{+, \lambda/2}^\lambda \text{Disc } \mathcal{B}_{+, -\lambda/2}^\lambda \right\}\end{aligned}\quad (2.16)$$

where the contribution arises from photons with opposite helicities, $\lambda = -\lambda'$. From the explicit expressions of the amplitudes we get

$$\mathcal{N}A_N = \frac{16e^2}{Q^2} \frac{1-y}{y^2} (e_1 g)^2 e_2 a_0 M q^+ \frac{(1-x_B)^2}{r_\perp^2 + B} \text{Re} \{ e^{-2i\tau} I^+ + e^{2i\tau} I^- \} \quad (2.17)$$

where

$$\begin{aligned}I^+ &\equiv \int \frac{d^2 \mathbf{k}_\perp}{(2\pi)^2} \frac{k_\perp e^{i\phi} (k_\perp e^{i\phi} - r_\perp e^{i\psi}) r_\perp e^{i\psi}}{(k_\perp^2 + B)(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} e^{-A(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} \\ &= e^{3i\psi} \int \frac{d^2 \mathbf{k}_\perp}{(2\pi)^2} \frac{(k_\perp e^{i\phi} + r_\perp) k_\perp e^{i\phi} r_\perp e^{-Ak_\perp^2}}{(k_\perp^2 + r_\perp^2 + 2k_\perp r_\perp \cos \phi + B) k_\perp^2} \equiv e^{3i\psi} J^+\end{aligned}\quad (2.18)$$

and we substituted $\mathbf{k}_\perp \rightarrow \mathbf{k}_\perp + \mathbf{r}_\perp$ followed by $\phi \rightarrow \phi + \psi$ in (2.18). Similarly,

$$\begin{aligned}I^- &\equiv \int \frac{d^2 \mathbf{k}_\perp}{(2\pi)^2} \frac{(Mx_B)^2 (k_\perp e^{-i\phi} - r_\perp e^{-i\psi})}{(k_\perp^2 + B)(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} e^{-A(\mathbf{k}_\perp - \mathbf{r}_\perp)^2} \\ &= e^{-i\psi} \int \frac{d^2 \mathbf{k}_\perp}{(2\pi)^2} \frac{(Mx_B)^2 k_\perp e^{-i\phi} e^{-Ak_\perp^2}}{(k_\perp^2 + r_\perp^2 + 2k_\perp r_\perp \cos \phi + B) k_\perp^2} \\ &\equiv e^{-i\psi} J^-\end{aligned}\quad (2.19)$$

with B given by (2.9). Noting that the $J^\pm$ are real and using the expression (2.14) for $\mathcal{N}$ gives for the asymmetry

$$A_N \simeq 2e_2 a_0 \frac{1-y}{1+(1-y)^2} \frac{r_\perp^2 + x_B [m_s^2 - (1-x_B)M^2]}{[r_\perp^2 + (Mx_B)^2]} [J^+ \cos(3\psi - 2\tau) + J^- \cos(\psi - 2\tau)]. \quad (2.20)$$

The integrals in the factors $J^\pm$ defined in (2.18) and (2.19) can be evaluated explicitly in the limit where the rescattering is very soft, i.e., for $r_\perp^2, m_s^2, M^2 \gg 1/A$, where A determines the momentum dependence of the Pauli coupling (2.2). The result for the asymmetry then reads

$$\begin{aligned}A_N &\simeq -\frac{e_2 a_0}{2\pi A} \frac{1-y}{1+(1-y)^2} \frac{r_\perp}{\{r_\perp^2 + x_B [m_s^2 - (1-x_B)M^2]\} [r_\perp^2 + (Mx_B)^2]} \times \\ &\quad \times [r_\perp^2 \cos(3\psi - 2\tau) + (Mx_B)^2 \cos(\psi - 2\tau)] \left[1 + \mathcal{O}\left(\frac{1}{A}\right) \right].\end{aligned}\quad (2.21)$$

Note that $A_N \propto 1/r_\perp$ for large $r_\perp$.

3. Concluding remarks

In the preceding section we used a frame where the target spin was fixed in the y direction, with quark and lepton azimuthal angles defined by eqs. (2.6) and (2.12), respectively. In the Trento convention [9] one uses instead the angle ϕ_s between the target spin direction and the lepton plane,

$$\phi_s = \frac{\pi}{2} - \tau \quad (3.1)$$

and the angle ϕ_h between the hadron (or quark jet) and lepton planes

$$\phi_h = \psi - \tau. \quad (3.2)$$

In terms of these angles our result (2.21) is

$$A_N \simeq \frac{e_2 a_0}{2\pi A} \frac{1-y}{1+(1-y)^2} \frac{r_\perp}{\{r_\perp^2 + x_B[m_s^2 - (1-x_B)M^2]\} [r_\perp^2 + (Mx_B)^2]} \times \\ \times [r_\perp^2 \sin(3\phi_h - \phi_s) - (Mx_B)^2 \sin(\phi_h + \phi_s)] \left[1 + \mathcal{O}\left(\frac{1}{A}\right) \right] \quad (3.3)$$

The angular dependence is the same² as that in the Collins effect [7, 10, 11]. The physical origin of the two asymmetries is, however, quite different. The Collins effect arises from final state interactions at the hadronization stage, which are incoherent with the interaction of the virtual photon. The rescattering giving rise to (3.3) is, on the other hand, coherent with the hard subprocess and thus can potentially affect also the total DIS cross section ($k_\perp$ -integrated parton distributions). In particular, soft rescattering with a Pauli coupling eliminates an obstacle [10, 11] to measuring transversity in DIS, namely that the upper part of the ‘handbag’ conserves quark helicity.

The discussion of physical rescattering effects in [1] concerned the integrated parton distributions which are given by matrix elements of the form

$$f_{q/N}(x_B, Q^2) = \frac{1}{8\pi} \int dx^- \exp(-ix_B P^+ x^-/2) \times \\ \times \langle N(P) | \bar{\psi}(x^-) \gamma^+ W[x^-; 0] \psi(0) | N(P) \rangle \Big|_{x^+ = x_\perp = 0} \quad (3.4)$$

where in the Bjorken limit all fields are evaluated at equal LF time $x^+ \sim 1/\nu$ and vanishing transverse separation $x_\perp \sim 1/Q$. In Feynman gauge the rescattering effects are given by the Wilson line

$$W[x^-; 0] = \text{P exp} \left[ig_s \int_0^{x^-} dw^- A^+(w^-) \right]. \quad (3.5)$$

In light-cone gauge (lcg., $A^+ = 0$) the Wilson line reduces to unity,

$$W[x^-; 0] = 1 \quad \text{for } A^+ = 0 \quad (3.6)$$

which appears to suggest that there is no effect of rescattering in this gauge (and hence in any gauge, due to the gauge invariance of physical quantities).

²Except that our angle ϕ_h refers to the current jet axis rather than to the hadron.

The model analysis of [1] was done in both the Feynman and light-cone gauges. Diagrams involving rescattering of the struck quark were indeed found not to contribute in lcg., in accordance with (3.6). Nevertheless, the same physical effects on the DIS cross section were found in both gauges. The apparent contradiction is resolved by the peculiar origin of the rescattering effect in light-cone gauge: The contributing Feynman diagrams involve instantaneous (in x^+) interactions *between spectators*, mediated by A^+ gluons which carry $k^+ = 0$. These contributions arise from the pole at $k^+ = 0$ of the gluon propagator in lcg.,³

$$d_{LF}^{\mu\nu}(k) = \frac{i}{k^2 + i\varepsilon} \left[-g^{\mu\nu} + \frac{n^\mu k^\nu + k^\mu n^\nu}{k^+} \right] \quad (3.7)$$

where $n = (0, 2, \mathbf{0}_\perp)$. Such interactions are “zero-modes” [8, 12] of the $x^+ = 0$ nucleon state in the matrix element of (3.4). States defined at $x^+ = 0$ are ambiguous with respect to zero-modes since signals can be transmitted on a LF surface. The zero modes of the nucleon LF states thus differ in the Feynman and light-cone gauges.

If the possibility is admitted that soft rescattering can change the quark helicity (and we do not see how to exclude it) then the Wilson line (3.5) does not fully describe the rescattering effect. The Wilson line arises from the $-ig_s\gamma^\mu$ coupling in (1.1) which at high energy conserves helicity.

Our observations are qualitatively consistent with earlier suggestions (see, e.g., [13, 14]) that non-perturbative (e.g., instanton) effects may jeopardize QCD factorization. In particular, Nachtmann [14] has emphasized that timing arguments allow hard QCD subprocesses to be influenced by soft interactions. In our example the soft exchanges carry finite momentum in the target rest frame. Consequently they form in a finite time, compatible with the finite coherence length (1.2) of the virtual photon.

Ellis et al. [13] argued that parton distributions obey the usual DGLAP evolution in Q^2 even if they are not universal. This is consistent with the observation in [2] that the soft rescattering is independent of hard gluon emission. Partons produced at the hard vertex separate with a transverse velocity $v_\perp \sim Q/\nu$ which vanishes in the Bjorken limit. Soft rescattering occurring within the finite coherence length (1.2) therefore cannot resolve hard gluon emission and does not affect the evolution in Q^2 .

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References

- [1] S.J. Brodsky, P. Hoyer, N. Marchal, S. Peigne and F. Sannino, *Structure functions are not parton probabilities*, *Phys. Rev. D* **65** (2002) 114025 [[hep-ph/0104291](#)].

³The poles at $k^+ = 0$ are spurious: they cancel in the sum of all diagrams. However, the poles in the subset of diagrams which involve only spectator-spectator interactions give a non-vanishing contribution.

- [2] S.J. Brodsky, R. Enberg, P. Hoyer and G. Ingelman, *Hard diffraction from parton rescattering in QCD*, *Phys. Rev. D* **71** (2005) 074020 [[hep-ph/0409119](#)].
- [3] S.J. Brodsky, D.S. Hwang and I. Schmidt, *Final-state interactions and single-spin asymmetries in semi-inclusive deep inelastic scattering*, *Phys. Lett. B* **530** (2002) 99 [[hep-ph/0201296](#)].
- [4] J.C. Collins, *Leading-twist single-transverse-spin asymmetries: Drell-Yan and deep-inelastic scattering*, *Phys. Lett. B* **536** (2002) 43 [[hep-ph/0204004](#)].
- [5] D.W. Sivers, *Single spin production asymmetries from the hard scattering of point-like constituents*, *Phys. Rev. D* **41** (1990) 83.
- [6] N.I. Kochelev, *Anomalous quark chromomagnetic moment induced by instantons*, *Phys. Lett. B* **426** (1998) 149 [[hep-ph/9610551](#)]; *The pauli form factor of the quark induced by instantons*, *Phys. Lett. B* **565** (2003) 131 [[hep-ph/0304171](#)].
- [7] J.C. Collins, *Fragmentation of transversely polarized quarks probed in transverse momentum distributions*, *Nucl. Phys. B* **396** (1993) 161 [[hep-ph/9208213](#)].
- [8] S.J. Brodsky, H.-C. Pauli and S.S. Pinsky, *Quantum chromodynamics and other field theories on the light cone*, *Phys. Rept.* **301** (1998) 299 [[hep-ph/9705477](#)].
- [9] A. Bacchetta, U. D'Alesio, M. Diehl and C.A. Miller, *Single-spin asymmetries: the Trento conventions*, *Phys. Rev. D* **70** (2004) 117504 [[hep-ph/0410050](#)].
- [10] V. Barone, A. Drago and P.G. Ratcliffe, *Transverse polarisation of quarks in hadrons*, *Phys. Rept.* **359** (2002) 1 [[hep-ph/0104283](#)].
- [11] V. Barone, *Understanding transversity: present and future*, [hep-ph/0502108](#).
- [12] K. Yamawaki, *Zero-mode problem on the light front*, [hep-th/9802037](#).
- [13] J.R. Ellis, M.K. Gaillard and J. Zakrzewski, Wojciech, *Nonperturbative effects on factorization in high momentum processes*, *Phys. Lett. B* **81** (1979) 224.
- [14] O. Nachtmann and A. Reiter, *The vacuum structure in QCD and hadron-hadron scattering*, *Z. Physik C* **24** (1984) 283; *High energy collisions and nonperturbative QCD*, [hep-ph/9609365](#).