# ON THE RELATIVE SIZES OF PLANETS WITHIN KEPLER MULTIPLE-CANDIDATE SYSTEMS 

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#### Abstract

We present a study of the relative sizes of planets within the multiple-candidate systems discovered with the Kepler mission. We have compared the size of each planet to the size of every other planet within a given planetary system after correcting the sample for detection and geometric biases. We find that for planet pairs for which one or both objects are approximately Neptune-sized or larger, the larger planet is most often the planet with the longer period. No such size-location correlation is seen for pairs of planets when both planets are smaller than Neptune. Specifically, if at least one planet in a planet pair has a radius of $\gtrsim 3 R_{\oplus}, 68 \% \pm 6 \%$ of the planet pairs have the inner planet smaller than the outer planet, while no preferred sequential ordering of the planets is observed if both planets in a pair are smaller than $\lesssim 3 R_{\oplus}$.


Key word: planetary systems

## 1. INTRODUCTION

Approximately $20 \%$ of the planetary candidate systems discovered thus far by Kepler (Borucki et al. 2010) have been identified as having multiple transiting candidate planets (Batalha et al. 2012). As Kepler continues its mission, the number of multiple-planet systems is likely to grow-not only because the total number of systems known to host planets will increase, but also because previously identified "single"candidate systems may be found to have additional planets not previously detected. For example, 96 (11\%) of the "single"candidate systems from the Borucki et al. (2011) Kepler Object of Interest (KOI) list are now listed on the Batalha et al. (2012) KOI list as having multiple planetary candidates. Thus, understanding planets in multiple systems is not only important for placing into context our own solar system (the best-studied planetary system), but multiple planetary systems may turn out to be the rule rather than the exception.

Typical detailed confirmation of individual planetary systems takes a concerted ground-based observational and modeling effort to rule out false positives caused by blends (e.g., Batalha et al. 2011; Torres et al. 2011). However, the multiple-candidate systems provide additional information that can be used to confirm planets directly via transit timing variations (Steffen et al. 2012a; Fabrycky et al. 2012a) or via statistical arguments that multiple transiting systems discovered by Kepler are almost all true planetary systems (Latham et al. 2011; Lissauer et al. 2011b, 2012). Indeed, based upon orbital stability arguments, $\approx 96 \%$ of the pairs within multiple-candidate systems are most likely real planets around the same star (Fabrycky et al. 2012b).

The higher statistical likelihood that candidates in multiple systems are true planetary systems has enabled studies of the properties of planetary systems with a lower level of false positive contamination than would be expected if all transiting systems were studied. The overall false positive rate within the Kepler candidate sample has been estimated to be $10 \%-35 \%$ (e.g., Morton \& Johnson 2011; Santerne et al. 2012), but in comparison, the overall false positive rates among the multiple transiting systems are expected to be $\lesssim 1 \%$ (Lissauer et al. 2012).

The multiple-candidate systems also provide another level of certainty to the studies of planetary systems. The quality of knowledge of planetary characteristics for individual planets often is dependent upon the quality of knowledge of the host stellar characteristics. For example, planetary radii uncertainties for transiting planets are dominated by the uncertainties in the stellar radii (transit depth $\left.\propto\left(R_{p} / R_{\star}\right)^{2}\right)$, and changes in our understanding of the stellar radius can greatly alter our understanding of the radii of individual planets (e.g., Muirhead et al. 2012). By studying the relative properties of planets within multiple systems, systematic uncertainties associated with the stellar properties are minimized.

Understanding the relative sizes and, hence, the relative bulk compositions and structures of the planets within a system can yield clues on the formation, migration, and evolution of planets within an individual system and on planetary systems as a whole (e.g., Raymond et al. 2012). Within our solar system, the distribution of the unique pairwise radii ratios for each planet compared to the planets in orbits exterior to its orbit (e.g., Mercury-Venus, Mercury-Earth, ... , Mercury-Neptune, Venus-Earth, Venus-Mars, ... etc.) is dominated by ratios less than unity (i.e., the inner planets are smaller than the outer planets). For the eight planets in the solar system, 20 of the 28 ( $70 \%$ ) unique radii ratios are $<1$, but only 3 out of 7 ( $42 \%$ ) of neighboring pairs display this sequential size hierarchy. If only the terrestrial planets are considered (Mercury, Venus, Earth, Mars), the fraction is $2 / 3$ with only Mars being smaller than its inner companions.

How the planet sizes are ordered and distributed is likely a direct result of the how the planets formed and evolved. For example, Mars, being the only terrestrial planet in our solar system that does not follow the sequential planet size distribution, may be a direct result of the formation and migration of Jupiter, inward and then back outward leaving a truncated and depleted inner disk out of which Mars was formed (Walsh et al. 2011).

Lissauer et al. (2011b) noted, for adjacent planets within the Kepler multiple-candidate systems, that the distribution of radii ratios for adjacent planets is symmetrically centered
around unity, but hints of a planetary size hierarchy can be seen in multi-planet systems discovered by Kepler. Kepler-11 has six transiting planets (Lissauer et al. 2011a) with the smallest planets residing preferentially inside the orbits of larger planets. Kepler-11 displays an anti-correlation between the mean density of the planets and the semimajor axis distance from the host star; i.e., the larger and lower density planets are located farther out than the smaller and denser planets, possibly indicative of the formation and/or evolution of the planetary system (Migaszewski et al. 2012). Kepler-47, the only known circumbinary multiple-planet system, also displays a size hierarchy with the inner planet ( $\sim 3 R_{\oplus}$ ) being smaller than the outer planet ( $\sim 4.6 R_{\oplus}$; Orosz et al. 2012). Yet, in Kepler-20 (a five-planet system), the relative sizes of the planets do not appear to correlate with the orbital periods of the planets (Gautier et al. 2012; Fressin et al. 2012). But these are only three systems. Is there an overall correlation of planetary size with orbital period?

Here, we explore the relative sizes of the planetary radii for all planet pairs within the multiple-candidate systems discovered thus far by Kepler (Batalha et al. 2012). In this work, we refer to the Kepler candidates as "planets" though the majority have not been formally validated or confirmed as planets; as discussed above, candidates in multiple-candidate systems are statistically more likely to be true planetary systems (Latham et al. 2011; Lissauer et al. 2011b, 2012). We seek to characterize the planetary size hierarchy, as a function of the number of planets detected in the systems and the properties of the stellar hosts, and explore if the size hierarchy seen within the inner solar system also occurs in the Kepler multiple-candidate sample.

## 2. THE SAMPLE

The sample used here is based upon the 2012 KOI candidate list published by Batalha et al. (2012); a full description of the KOI list, the vetting that list underwent, and the characteristics of the sample set as a whole are described in the catalog paper. There are 1425 systems with a single candidate, 245 systems with two planet candidates, 84 systems with three planet candidates, 27 systems with four planet candidates, 8 systems with five planet candidates, and 1 system with six planet candidates. Here we wish to investigate the overall distribution of planet sizes as a function of orbit; that is, do outer planets, in general, tend to be larger than inner planets?

A smaller planet (e.g., shallower transit) will be more easily detected if the period is short, simply from the fact that the number of observed transiting events increases with shorter orbital period. In a complementary manner, the larger planets are more easily detected at all periods, up to some period threshold where only 2-3 transits are detected. Batalha et al. (2012) tabulate for each candidate the transit period, the transit duration, the impact parameter, and the signal-to-noise ratio (S/N) of the transit fits. The $\mathrm{S} / \mathrm{Ns}$, coupled with the transit periods and the impact parameters, enable us to debias the sample for these observational detection efficiencies (see also Lissauer et al. 2011b).

The multiple-candidate systems were identified primarily by searching the single-candidate systems specifically for additional transiting planets. Thus, there could potentially be a detection bias of which we are unaware that is not found in the single-candidate systems. However, no substantial difference between single-planet systems and the multiple-planet systems was found, except for the lack of hot Jupiters in the multipleplanet systems (Latham et al. 2011; Steffen et al. 2012b). The


Figure 1. Distribution of the transit signal-to-noise ratio for all the detected "multiple" candidates from Batalha et al. (2012). The solid curve is an exponential fit to the $S / N$ distribution, and the vertical dashed line at $S / N=25$ marks approximately where the exponential no longer adequately describes the distribution (see inset figure).
overall size distribution of the planets and the $S / N$ detection thresholds appear to be similar between the single-candidate and multiple-candidate systems.

To understand better the detection thresholds for the multiplecandidate systems, we have used the distribution of the total transit $\mathrm{S} / \mathrm{N}$ to estimate where the distribution of planets in multiple systems appears to be complete (Figure 1). Assuming the $\mathrm{S} / \mathrm{N}$ distribution can be characterized with an exponential function where the distribution is complete, we have used the point in the $\mathrm{S} / \mathrm{N}$ distribution function where the exponential no longer adequately describes the distribution as the fiducial for completeness. Fitting the exponential, we find a turnover in detected samples at an $\mathrm{S} / \mathrm{N} \approx 25$. We use this $\mathrm{S} / \mathrm{N}$ threshold to debias the radii-ratio distribution of planets in multiplecandidate systems.

The total $\mathrm{S} / \mathrm{N}$ of all the detected transits for each planetary candidate is predicted for all the observed orbital periods within a system. A planet pair is retained in the analysis only if the predicted total transit $\mathrm{S} / \mathrm{Ns}$ for both planets at the orbital period of the other planet exceeds the $\mathrm{S} / \mathrm{N}$ threshold of $\mathrm{S} / \mathrm{N}>25$. The predicted $\mathrm{S} / \mathrm{N}$ is determined by scaling the measured total $\mathrm{S} / \mathrm{N}$ of the planet transits by the ratio of the orbital periods. Assuming all else is equal, the total $\mathrm{S} / \mathrm{N}$ of all the detected transits for a given planet scales with the orbital period as $P^{-1 / 3}$.

For a given planet, the total $\mathrm{S} / \mathrm{N}$ of all detected transits is proportional to the total number of points $(n)$ detected in all of the transits (e.g., von Braun et al. 2009)

$$
\begin{equation*}
(\mathrm{S} / \mathrm{N})_{\text {transits }} \propto(n)^{1 / 2} \propto\left(N \cdot n_{t}\right)^{1 / 2} \tag{1}
\end{equation*}
$$

where $N$ is the total number of individual transits detected, and $n_{t}$ is the number of points detected within a single transit. The number of transits detected is inversely proportional to the orbital period ( $N \propto 1 / P$ ), and the number of points detected per transit is proportional to the transit duration $\left(n_{t} \propto t_{\text {dur }}\right)$; thus, the total $\mathrm{S} / \mathrm{N}$ of the detected transits can be parameterized as

$$
\begin{equation*}
(\mathrm{S} / \mathrm{N})_{\text {transits }} \propto\left(t_{\mathrm{dur}} / P\right)^{1 / 2} \tag{2}
\end{equation*}
$$

The transit duration $\left(t_{\mathrm{dur}}\right)$ is proportional to the cube root of the orbital period $\left(t_{\text {dur }} \propto v_{\text {orb }}^{-1} \propto P^{1 / 3}\right)$; thus, the total $\mathrm{S} / \mathrm{N}$ of the


Figure 2. Distributions of the radii and orbital periods of the planets that are used in this study. The vertical dashed lines mark the median values of the distributions.
detected transits scales with the orbital period as

$$
\begin{equation*}
(\mathrm{S} / \mathrm{N})_{\text {transits }} \propto\left(P^{1 / 3} / P\right)^{1 / 2} \propto P^{-1 / 3} \tag{3}
\end{equation*}
$$

An additional restriction on the sample was made such that no planet candidate was included that has an impact parameter of $b \geqslant 0.8$. At such high impact parameters, the transit parameters, particularly the transit depth (i.e., the planet radius), are less certain. Using the $\mathrm{S} / \mathrm{N}>25$ detection threshold and the impact parameter restrictions, there are 96 multiple-candidate systems with 159 pairs of planets ( 228 individual planets) in the analysis.

All of the planet pairs used in the analysis of this paper are summarized in Table 1; planets are labeled with roman numerals (I, II, III, IV, V, VI) in the order of increasing orbital period. These do not necessarily correspond to KOI fraction numbers (e.g., . $01, .02, \ldots$ ) nor do they correspond to the confirmed planet letters (e.g., Kepler-11b, Kepler-11c, ...). After the S/N and impact parameter cuts, the largest planet in the sample is $13 R_{\oplus}$, and the median planet radius is $\approx 2.5 R_{\oplus}$; the smallest planet retained in the sample has a radius of $0.75 R_{\oplus}$. The orbital periods of the planets in this sample span 0.45-331 days, with an median period of $\sim 13.1$ days. The distributions of the radii and orbit periods for the 228 planets retained in the sample are shown in Figure 2.

Previous work indicates that the detected planets in the Kepler multiple-candidate systems have mutual inclinations of $1^{\circ}-3^{\circ}$ (Fabrycky et al. 2012b; Fang \& Margot 2012). Due to the usual limitation of the transit technique in only detecting planets that are very nearly edge-on, the Kepler sample used here is naturally biased to systems of nearly coplanar planets. The prevalence of Kepler multiple-candidate systems shows that


Figure 3. Observed cumulative distribution of the planet-radii ratios for all planet pairs (black histogram), and the predicted cumulative distribution for planet radii drawn randomly from the measure planet sample (gray histogram). The horizontal dot-dash line marks the fraction of planet pairs with $R_{\text {inner }} / R_{\text {outer }}<1$; the gray region marks the $1 \sigma$ confidence interval for this fraction. The vertical dashed line marks the boundary where $R_{\text {inner }} / R_{\text {outer }}=1$, and the horizontal dashed line marks the $50 \%$ fraction.
there is a large population of such systems with small planets and orbital periods of tens of days (Figure 2). It may be that other system architectures with higher mutual inclinations or different period ranges do not show the same trend in planet sizes that we describe herein.

## 3. DISCUSSION

We have calculated the ratios of the inner planet radius to the outer planet radius for each unique pair of planets within a system ( $R_{\text {inner }} / R_{\text {outer }}$ ), and the cumulative fraction distribution is displayed in Figure 3. If there were no preference for the ordering of planet sizes, the chance that a given planet-radii ratio is larger than unity would be equal to the chance that the ratio is below unity, and the cumulative fraction distribution would pass through $50 \%$ at $\log \left(R_{\text {inner }} / R_{\text {outer }}\right)=0\left(R_{\text {inner }} / R_{\text {outer }}=1\right)$.
In contrast, 59.7 ${ }_{-4.2}^{+4.1} \%$ of the planet pairs are ordered such that the outer planet is larger than the inner planet ( $R_{\text {inner }} / R_{\text {outer }}<1$ ). The resulting fraction deviates from the null-hypothesis expectation value of $50 \%$ by $\approx 2.5 \sigma$. The $1 \sigma$ upper and lower confidence intervals are based upon the Clopper-Pearson binomial distribution confidence interval (Clopper \& Pearson 1934). The Clopper-Pearson interval is a two-sided confidence interval and is based directly on the binomial distribution rather than an approximation to the binomial distribution. We do caution that in applying the Clopper-Pearson confidence interval there is an implicit assumption that all elements of the sample are uncorrelated. Given that not all planet pairs are from independent stellar systems, there may be a correlation between individual planet pairs within a system (i.e., planet I is smaller than planet III because it is smaller than planet II), and the Clopper-Pearson confidence intervals may underestimate the true uncertainties in the fractions.

In addition to the confidence intervals, the significance of the observed fraction in comparison to the null hypothesis can be evaluated through the $\chi^{2}$ statistic. The probability of the observed fraction $(96 / 159=59.7 \%)$ when compared to the expected fraction $(79.5 / 79.5=50 \%)$ yields $\chi^{2}=6.0$ with a probability of only $1.4 \%$ that the observed fraction is observed only by chance (see Table 2).

Table 1
Summary of Planet-radii Ratios

| KOI | Stellar | Planet | Inner Planet |  |  |  | Outer Planet |  |  |  | Planet-radii |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Temperature <br> (K) | Pair | Radius $\left(R_{\oplus}\right)$ | Period (days) | Transit S/N | Impact Par. | Radius $\left(R_{\oplus}\right)$ | Period (days) | $\begin{gathered} \text { Transit } \\ \mathrm{S} / \mathrm{N} \end{gathered}$ | Impact Par. | Ratio $R_{\text {inner }} / R_{\text {outer }}$ |
| KOIs with Two Candidates |  |  |  |  |  |  |  |  |  |  |  |
| K00072 | 5627 | I/II | 1.38 | 0.837 | 139 | 0.17 | 2.19 | 45.294 | 122 | 0.11 | 0.630 |
| K00108 | 5975 | I/II | 2.94 | 15.965 | 84 | 0.79 | 4.45 | 179.600 | 111 | 0.62 | 0.661 |
| K00119 | 5380 | I/II | 3.76 | 49.184 | 152 | 0.55 | 3.30 | 190.310 | 63 | 0.69 | 1.139 |
| K00123 | 5871 | I/II | 2.64 | 6.482 | 98 | 0.56 | 2.71 | 21.222 | 78 | 0.01 | 0.974 |
| K00150 | 5538 | I/II | 2.63 | 8.409 | 106 | 0.73 | 2.73 | 28.574 | 81 | 0.76 | 0.963 |
| K00209 | 6221 | I/II | 5.44 | 18.795 | 217 | 0.51 | 8.29 | 50.790 | 287 | 0.40 | 0.656 |
| K00222 | 4353 | I/II | 2.03 | 6.312 | 85 | 0.71 | 1.66 | 12.794 | 43 | 0.72 | 1.223 |
| K00223 | 5128 | I/II | 2.52 | 3.177 | 90 | 0.78 | 2.27 | 41.008 | 32 | 0.69 | 1.110 |
| K00271 | 6169 | I/II | 2.48 | 29.392 | 72 | 0.71 | 2.60 | 48.630 | 54 | 0.79 | 0.954 |
| K00275 | 5795 | I/II | 1.95 | 15.791 | 55 | 0.03 | 2.04 | 82.199 | 27 | 0.60 | 0.956 |
| K00312 | 6158 | I/II | 1.91 | 11.578 | 41 | 0.70 | 1.84 | 16.399 | 40 | 0.58 | 1.038 |
| K00313 | 5348 | I/II | 1.61 | 8.436 | 54 | 0.32 | 2.20 | 18.735 | 55 | 0.73 | 0.732 |
| K00386 | 5969 | I/II | 3.25 | 31.158 | 57 | 0.02 | 2.94 | 76.732 | 28 | 0.55 | 1.105 |
| K00413 | 5236 | I/II | 2.75 | 15.228 | 52 | 0.67 | 2.10 | 24.674 | 26 | 0.65 | 1.310 |
| K00431 | 5249 | I/II | 2.80 | 18.870 | 60 | 0.60 | 2.48 | 46.901 | 34 | 0.68 | 1.129 |
| K00433 | 5237 | I/II | 5.60 | 4.030 | 127 | 0.65 | 12.90 | 328.240 | 158 | 0.77 | 0.434 |
| K00446 | 4492 | I/II | 1.76 | 16.709 | 33 | 0.62 | 1.72 | 28.551 | 34 | 0.05 | 1.023 |
| K00448 | 4264 | I/II | 1.77 | 10.139 | 56 | 0.74 | 2.31 | 43.608 | 66 | 0.66 | 0.766 |
| K00464 | 5362 | I/II | 2.63 | 5.350 | 75 | 0.58 | 6.73 | 58.362 | 263 | 0.20 | 0.391 |
| K00475 | 5056 | I/II | 2.04 | 8.181 | 37 | 0.58 | 2.26 | 15.313 | 34 | 0.68 | 0.903 |
| K00509 | 5437 | I/II | 2.24 | 4.167 | 45 | 0.09 | 2.68 | 11.463 | 32 | 0.74 | 0.836 |
| K00518 | 4565 | I/II | 2.11 | 13.981 | 68 | 0.71 | 1.54 | 44.000 | 33 | 0.49 | 1.370 |
| K00638 | 5722 | I/II | 3.60 | 23.636 | 53 | 0.02 | 3.78 | 67.093 | 39 | 0.27 | 0.952 |
| K00657 | 4632 | I/II | 1.63 | 4.069 | 43 | 0.63 | 2.08 | 16.282 | 46 | 0.74 | 0.784 |
| K00672 | 5524 | I/II | 2.60 | 16.087 | 43 | 0.71 | 3.15 | 41.749 | 70 | 0.11 | 0.825 |
| K00676 | 4367 | I/II | 2.56 | 2.453 | 255 | 0.70 | 3.30 | 7.972 | 348 | 0.57 | 0.776 |
| K00693 | 6121 | I/II | 1.87 | 15.660 | 48 | 0.50 | 1.76 | 28.779 | 23 | 0.64 | 1.062 |
| K00708 | 6036 | I/II | 1.82 | 7.693 | 43 | 0.74 | 2.54 | 17.406 | 68 | 0.70 | 0.717 |
| K00800 | 5938 | I/II | 3.27 | 2.711 | 48 | 0.76 | 3.39 | 7.212 | 36 | 0.77 | 0.965 |
| K00841 | 5399 | I/II | 5.44 | 15.334 | 83 | 0.74 | 7.05 | 31.331 | 117 | 0.74 | 0.772 |
| K00842 | 4497 | I/II | 2.04 | 12.718 | 43 | 0.31 | 2.46 | 36.065 | 44 | 0.42 | 0.829 |
| K00853 | 4842 | I/II | 2.38 | 8.204 | 48 | 0.12 | 1.78 | 14.496 | 22 | 0.02 | 1.337 |
| K00870 | 4590 | I/II | 2.52 | 5.912 | 56 | 0.76 | 2.35 | 8.986 | 47 | 0.73 | 1.072 |
| K00877 | 4500 | I/II | 2.42 | 5.955 | 54 | 0.73 | 2.37 | 12.039 | 36 | 0.79 | 1.021 |
| K00896 | 5190 | I/II | 3.22 | 6.308 | 68 | 0.52 | 4.52 | 16.239 | 91 | 0.57 | 0.712 |
| K00936 | 3684 | I/II | 1.54 | 0.893 | 72 | 0.75 | 2.69 | 9.468 | 96 | 0.76 | 0.572 |
| K00951 | 4767 | I/II | 3.74 | 13.197 | 101 | 0.39 | 2.87 | 33.653 | 36 | 0.58 | 1.303 |
| K00988 | 5218 | I/II | 2.20 | 10.381 | 67 | 0.02 | 2.17 | 24.570 | 37 | 0.67 | 1.014 |
| K01236 | 6562 | I/II | 2.04 | 12.309 | 40 | 0.01 | 3.02 | 35.743 | 64 | 0.37 | 0.675 |
| K01270 | 5145 | I/II | 2.19 | 5.729 | 45 | 0.58 | 1.55 | 11.609 | 22 | 0.01 | 1.413 |
| K01781 | 4977 | I/II | 1.94 | 3.005 | 81 | 0.19 | 3.29 | 7.834 | 172 | 0.01 | 0.590 |
| K01824 | 5978 | I/II | 1.75 | 1.678 | 53 | 0.70 | 1.97 | 3.554 | 50 | 0.69 | 0.888 |
| KOIs with Three Candidates |  |  |  |  |  |  |  |  |  |  |  |
| K00085 | 6172 | I/II | 1.27 | 2.155 | 72 | 0.71 | 2.35 | 5.860 | 154 | 0.77 | 0.540 |
| K00085 | 6172 | I/III | 1.27 | 2.155 | 72 | 0.71 | 1.41 | 8.131 | 53 | 0.78 | 0.901 |
| K00085 | 6172 | II/III | 2.35 | 5.860 | 154 | 0.77 | 1.41 | 8.131 | 53 | 0.78 | 1.667 |
| K00111 | 5711 | I/II | 2.14 | 11.427 | 96 | 0.53 | 2.05 | 23.668 | 71 | 0.55 | 1.044 |
| K00111 | 5711 | I/III | 2.14 | 11.427 | 96 | 0.53 | 2.36 | 51.756 | 75 | 0.57 | 0.907 |
| K00111 | 5711 | II/III | 2.05 | 23.668 | 71 | 0.55 | 2.36 | 51.756 | 75 | 0.57 | 0.869 |
| K00115 | 6202 | II/III | 3.33 | 5.412 | 144 | 0.43 | 1.88 | 7.126 | 41 | 0.55 | 1.771 |
| K00137 | 5385 | I/II | 1.82 | 3.505 | 44 | 0.71 | 4.75 | 7.641 | 299 | 0.50 | 0.383 |
| K00137 | 5385 | I/III | 1.82 | 3.505 | 44 | 0.71 | 6.00 | 14.858 | 305 | 0.72 | 0.303 |
| K00137 | 5385 | II/III | 4.75 | 7.641 | 299 | 0.50 | 6.00 | 14.858 | 305 | 0.72 | 0.792 |
| K00152 | 6187 | I/II | 2.59 | 13.484 | 58 | 0.34 | 2.77 | 27.402 | 57 | 0.07 | 0.935 |
| K00152 | 6187 | I/III | 2.59 | 13.484 | 58 | 0.34 | 5.36 | 52.091 | 158 | 0.00 | 0.483 |
| K00152 | 6187 | II/III | 2.77 | 27.402 | 57 | 0.07 | 5.36 | 52.091 | 158 | 0.00 | 0.517 |
| K00156 | 4619 | I/II | 1.18 | 5.188 | 38 | 0.53 | 1.60 | 8.041 | 54 | 0.64 | 0.738 |
| K00156 | 4619 | I/III | 1.18 | 5.188 | 38 | 0.53 | 2.53 | 11.776 | 131 | 0.69 | 0.466 |
| K00156 | 4619 | II/III | 1.60 | 8.041 | 54 | 0.64 | 2.53 | 11.776 | 131 | 0.69 | 0.632 |
| K00284 | 5925 | I/II | 1.09 | 6.178 | 32 | 0.38 | 1.14 | 6.415 | 35 | 0.19 | 0.956 |
| K00343 | 5744 | I/II | 1.86 | 2.024 | 72 | 0.63 | 2.68 | 4.762 | 108 | 0.63 | 0.694 |

Table 1
(Continued)

| KOI | Stellar <br> Temperature <br> (K) | Planet <br> Pair | Inner Planet |  |  |  | Outer Planet |  |  |  | Planet-radii <br> Ratio $R_{\text {inner }} / R_{\text {outer }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Radius $\left(R_{\oplus}\right)$ | Period (days) | Transit S/N | Impact Par. | Radius $\left(R_{\oplus}\right)$ | Period (days) | Transit S/N | Impact Par. |  |
| K00343 | 5744 | I/III | 1.86 | 2.024 | 72 | 0.63 | 1.58 | 41.809 | 20 | 0.53 | 1.177 |
| K00343 | 5744 | II/III | 2.68 | 4.762 | 108 | 0.63 | 1.58 | 41.809 | 20 | 0.53 | 1.696 |
| K00351 | 6103 | II/III | 6.62 | 210.590 | 144 | 0.22 | 9.32 | 331.640 | 211 | 0.19 | 0.710 |
| K00377 | 5777 | II/III | 8.28 | 19.273 | 136 | 0.35 | 8.21 | 38.907 | 81 | 0.62 | 1.009 |
| K00398 | 5101 | I/II | 1.76 | 1.729 | 37 | 0.24 | 3.33 | 4.180 | 102 | 0.00 | 0.529 |
| K00398 | 5101 | II/III | 3.33 | 4.180 | 102 | 0.00 | 8.66 | 51.846 | 215 | 0.66 | 0.385 |
| K00408 | 5631 | I/II | 3.72 | 7.382 | 96 | 0.79 | 2.91 | 12.560 | 52 | 0.77 | 1.278 |
| K00408 | 5631 | I/III | 3.72 | 7.382 | 96 | 0.79 | 2.70 | 30.827 | 34 | 0.79 | 1.378 |
| K00408 | 5631 | II/III | 2.91 | 12.560 | 52 | 0.77 | 2.70 | 30.827 | 34 | 0.79 | 1.078 |
| K00481 | 5227 | I/II | 1.54 | 1.554 | 43 | 0.71 | 2.37 | 7.650 | 56 | 0.76 | 0.650 |
| K00481 | 5227 | II/III | 2.37 | 7.650 | 56 | 0.76 | 2.44 | 34.260 | 39 | 0.73 | 0.971 |
| K00528 | 5448 | I/III | 2.62 | 9.577 | 55 | 0.48 | 3.27 | 96.671 | 32 | 0.71 | 0.801 |
| K00620 | 5803 | I/III | 7.05 | 45.155 | 132 | 0.03 | 9.68 | 130.180 | 279 | 0.06 | 0.728 |
| K00658 | 5676 | I/II | 2.03 | 3.163 | 68 | 0.53 | 2.02 | 5.371 | 52 | 0.65 | 1.005 |
| K00658 | 5676 | I/III | 2.03 | 3.163 | 68 | 0.53 | 1.14 | 11.329 | 17 | 0.01 | 1.781 |
| K00665 | 5864 | I/II | 1.16 | 1.612 | 34 | 0.69 | 1.09 | 3.072 | 27 | 0.64 | 1.064 |
| K00701 | 4807 | I/II | 1.27 | 5.715 | 55 | 0.46 | 1.95 | 18.164 | 71 | 0.66 | 0.651 |
| K00701 | 4807 | II/III | 1.95 | 18.164 | 71 | 0.66 | 1.57 | 122.390 | 34 | 0.29 | 1.242 |
| K00711 | 5502 | II/III | 3.18 | 44.699 | 51 | 0.61 | 2.83 | 124.520 | 35 | 0.49 | 1.124 |
| K00718 | 5788 | I/II | 2.57 | 4.585 | 67 | 0.34 | 3.06 | 22.714 | 58 | 0.29 | 0.840 |
| K00718 | 5788 | I/III | 2.57 | 4.585 | 67 | 0.34 | 2.67 | 47.904 | 27 | 0.68 | 0.963 |
| K00718 | 5788 | II/III | 3.06 | 22.714 | 58 | 0.29 | 2.67 | 47.904 | 27 | 0.68 | 1.146 |
| K00723 | 5244 | I/III | 3.26 | 3.937 | 72 | 0.79 | 3.61 | 28.082 | 60 | 0.58 | 0.903 |
| K00757 | 4956 | I/II | 2.09 | 6.253 | 34 | 0.00 | 4.73 | 16.068 | 120 | 0.25 | 0.442 |
| K00757 | 4956 | II/III | 4.73 | 16.068 | 120 | 0.25 | 3.21 | 41.192 | 40 | 0.35 | 1.474 |
| K00806 | 5461 | II/III | 13.24 | 60.322 | 366 | 0.37 | 9.52 | 143.210 | 69 | 0.34 | 1.391 |
| K00864 | 5337 | I/III | 2.51 | 4.312 | 63 | 0.14 | 2.23 | 20.050 | 30 | 0.00 | 1.126 |
| K00884 | 4931 | II/III | 4.13 | 9.439 | 143 | 0.48 | 4.23 | 20.476 | 73 | 0.70 | 0.976 |
| K00898 | 4648 | I/II | 2.18 | 5.170 | 35 | 0.64 | 2.83 | 9.771 | 47 | 0.68 | 0.770 |
| K00898 | 4648 | II/III | 2.83 | 9.771 | 47 | 0.68 | 2.36 | 20.089 | 28 | 0.59 | 1.199 |
| K00921 | 5046 | II/III | 2.66 | 10.281 | 43 | 0.69 | 3.09 | 18.119 | 46 | 0.70 | 0.861 |
| K00941 | 4998 | I/II | 2.37 | 2.383 | 38 | 0.53 | 4.14 | 6.582 | 99 | 0.03 | 0.572 |
| K00961 | 4188 | I/II | 2.63 | 0.453 | 100 | 0.69 | 2.86 | 1.214 | 73 | 0.77 | 0.920 |
| K01576 | 5445 | I/II | 3.20 | 10.415 | 64 | 0.68 | 2.84 | 13.084 | 50 | 0.65 | 1.127 |
| K01835 | 5004 | I/II | 2.69 | 2.248 | 43 | 0.44 | 3.11 | 4.580 | 37 | 0.67 | 0.865 |
| K01860 | 5708 | II/III | 2.44 | 6.319 | 46 | 0.46 | 2.36 | 12.209 | 36 | 0.35 | 1.034 |
| K01867 | 3892 | I/II | 1.21 | 2.549 | 37 | 0.40 | 1.08 | 5.212 | 25 | 0.31 | 1.120 |
| KOIs with Four Candidates |  |  |  |  |  |  |  |  |  |  |  |
| K00094 | 6217 | I/II | 1.41 | 3.743 | 35 | 0.16 | 3.43 | 10.423 | 78 | 0.01 | 0.411 |
| K00094 | 6217 | II/III | 3.43 | 10.423 | 78 | 0.01 | 9.25 | 22.343 | 455 | 0.30 | 0.371 |
| K00094 | 6217 | II/IV | 3.43 | 10.423 | 78 | 0.01 | 5.48 | 54.319 | 206 | 0.38 | 0.626 |
| K00094 | 6217 | III/IV | 9.25 | 22.343 | 455 | 0.30 | 5.48 | 54.319 | 206 | 0.38 | 1.688 |
| K00191 | 5495 | II/III | 2.25 | 2.418 | 53 | 0.55 | 10.67 | 15.358 | 642 | 0.59 | 0.211 |
| K00191 | 5495 | III/IV | 10.67 | 15.358 | 642 | 0.59 | 2.22 | 38.651 | 21 | 0.52 | 4.806 |
| K00245 | 5288 | II/III | 0.75 | 21.301 | 49 | 0.76 | 2.00 | 39.792 | 282 | 0.79 | 0.375 |
| K00571 | 3881 | I/II | 1.31 | 3.887 | 36 | 0.76 | 1.53 | 7.267 | 36 | 0.76 | 0.856 |
| K00571 | 3881 | II/III | 1.53 | 7.267 | 36 | 0.76 | 1.68 | 13.343 | 36 | 0.79 | 0.911 |
| K00571 | 3881 | II/IV | 1.53 | 7.267 | 36 | 0.76 | 1.53 | 22.407 | 27 | 0.78 | 1.000 |
| K00571 | 3881 | III/IV | 1.68 | 13.343 | 36 | 0.79 | 1.53 | 22.407 | 27 | 0.78 | 1.098 |
| K00720 | 5123 | I/II | 1.41 | 2.796 | 58 | 0.08 | 2.66 | 5.690 | 124 | 0.40 | 0.530 |
| K00720 | 5123 | I/III | 1.41 | 2.796 | 58 | 0.08 | 2.53 | 10.041 | 87 | 0.64 | 0.557 |
| K00720 | 5123 | II/III | 2.66 | 5.690 | 124 | 0.40 | 2.53 | 10.041 | 87 | 0.64 | 1.051 |
| K00733 | 5038 | II/III | 2.54 | 5.925 | 60 | 0.14 | 2.21 | 11.349 | 35 | 0.31 | 1.149 |
| K00812 | 4097 | I/III | 2.19 | 3.340 | 54 | 0.13 | 2.11 | 20.060 | 28 | 0.35 | 1.038 |
| K00834 | 5614 | III/IV | 1.98 | 13.233 | 33 | 0.38 | 5.33 | 23.653 | 154 | 0.38 | 0.371 |
| K00869 | 5085 | II/IV | 2.73 | 7.490 | 43 | 0.47 | 3.20 | 36.280 | 34 | 0.42 | 0.853 |
| K00880 | 5512 | III/IV | 4.00 | 26.442 | 48 | 0.64 | 5.35 | 51.530 | 109 | 0.02 | 0.748 |
| K00952 | 3911 | II/III | 2.25 | 5.901 | 47 | 0.72 | 2.15 | 8.752 | 35 | 0.77 | 1.047 |
| K00952 | 3911 | II/IV | 2.25 | 5.901 | 47 | 0.72 | 2.64 | 22.780 | 38 | 0.77 | 0.852 |
| K00952 | 3911 | III/IV | 2.15 | 8.752 | 35 | 0.77 | 2.64 | 22.780 | 38 | 0.77 | 0.814 |
| K01557 | 4783 | II/IV | 3.60 | 3.296 | 122 | 0.52 | 3.01 | 9.653 | 70 | 0.30 | 1.196 |
| K01567 | 5027 | II/III | 2.46 | 7.240 | 34 | 0.36 | 2.22 | 17.326 | 23 | 0.00 | 1.108 |
| K01930 | 5897 | II/III | 2.21 | 13.726 | 38 | 0.60 | 2.14 | 24.310 | 31 | 0.62 | 1.033 |

Table 1
(Continued)

| KOI | Stellar <br> Temperature (K) | Planet Pair | Inner Planet |  |  |  | Outer Planet |  |  |  | Planet-radii <br> Ratio $R_{\text {inner }} / R_{\text {outer }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Radius $\left(R_{\oplus}\right)$ | Period (days) | Transit S/N | Impact Par. | Radius $\left(R_{\oplus}\right)$ | Period (days) | Transit S/N | Impact Par. |  |
| K01930 | 5897 | II/IV | 2.21 | 13.726 | 38 | 0.60 | 2.46 | 44.431 | 29 | 0.66 | 0.898 |
| K01930 | 5897 | III/IV | 2.14 | 24.310 | 31 | 0.62 | 2.46 | 44.431 | 29 | 0.66 | 0.870 |
| KOIs with Five Candidates |  |  |  |  |  |  |  |  |  |  |  |
| K00070 | 5443 | I/II | 1.92 | 3.696 | 134 | 0.60 | 0.91 | 6.098 | 23 | 0.66 | 2.110 |
| K00070 | 5443 | I/III | 1.92 | 3.696 | 134 | 0.60 | 3.09 | 10.854 | 260 | 0.55 | 0.621 |
| K00070 | 5443 | I/IV | 1.92 | 3.696 | 134 | 0.60 | 1.02 | 19.577 | 18 | 0.74 | 1.882 |
| K00070 | 5443 | I/V | 1.92 | 3.696 | 134 | 0.60 | 2.78 | 77.611 | 103 | 0.55 | 0.691 |
| K00070 | 5443 | III/V | 3.09 | 10.854 | 260 | 0.55 | 2.78 | 77.611 | 103 | 0.55 | 1.112 |
| K00082 | 4908 | III/IV | 1.29 | 10.311 | 79 | 0.71 | 2.45 | 16.145 | 172 | 0.73 | 0.527 |
| K00082 | 4908 | III/V | 1.29 | 10.311 | 79 | 0.71 | 1.03 | 27.453 | 28 | 0.79 | 1.252 |
| K00082 | 4908 | IV/V | 2.45 | 16.145 | 172 | 0.73 | 1.03 | 27.453 | 28 | 0.79 | 2.379 |
| K00232 | 5868 | I/II | 1.73 | 5.766 | 41 | 0.40 | 4.31 | 12.465 | 207 | 0.43 | 0.401 |
| K00232 | 5868 | I/III | 1.73 | 5.766 | 41 | 0.40 | 1.69 | 21.587 | 21 | 0.67 | 1.024 |
| K00232 | 5868 | II/III | 4.31 | 12.465 | 207 | 0.43 | 1.69 | 21.587 | 21 | 0.67 | 2.550 |
| K00232 | 5868 | II/IV | 4.31 | 12.465 | 207 | 0.43 | 1.79 | 37.996 | 21 | 0.56 | 2.408 |
| K00232 | 5868 | II/V | 4.31 | 12.465 | 207 | 0.43 | 1.69 | 56.255 | 19 | 0.38 | 2.550 |
| K00500 | 4613 | III/IV | 1.63 | 4.645 | 30 | 0.72 | 2.64 | 7.053 | 59 | 0.71 | 0.617 |
| K00500 | 4613 | IV/V | 2.64 | 7.053 | 59 | 0.71 | 2.79 | 9.522 | 55 | 0.79 | 0.946 |
| K00707 | 5904 | II/III | 3.42 | 13.175 | 37 | 0.77 | 5.69 | 21.775 | 80 | 0.77 | 0.601 |
| K00707 | 5904 | II/IV | 3.42 | 13.175 | 37 | 0.77 | 4.26 | 31.784 | 42 | 0.77 | 0.803 |
| K00707 | 5904 | II/V | 3.42 | 13.175 | 37 | 0.77 | 4.77 | 41.029 | 51 | 0.77 | 0.717 |
| K00707 | 5904 | III/IV | 5.69 | 21.775 | 80 | 0.77 | 4.26 | 31.784 | 42 | 0.77 | 1.336 |
| K00707 | 5904 | III/V | 5.69 | 21.775 | 80 | 0.77 | 4.77 | 41.029 | 51 | 0.77 | 1.193 |
| K00707 | 5904 | IV/V | 4.26 | 31.784 | 42 | 0.77 | 4.77 | 41.029 | 51 | 0.77 | 0.893 |
| K01589 | 5755 | II/III | 2.23 | 8.726 | 30 | 0.72 | 2.36 | 12.882 | 27 | 0.79 | 0.945 |
| KOIs with Six Candidates |  |  |  |  |  |  |  |  |  |  |  |
| K00157 | 5685 | I/II | 1.89 | 10.304 | 38 | 0.34 | 2.92 | 13.024 | 67 | 0.35 | 0.647 |
| K00157 | 5685 | I/III | 1.89 | 10.304 | 38 | 0.34 | 3.20 | 22.686 | 73 | 0.33 | 0.591 |
| K00157 | 5685 | I/IV | 1.89 | 10.304 | 38 | 0.34 | 4.37 | 31.995 | 87 | 0.79 | 0.432 |
| K00157 | 5685 | II/III | 2.92 | 13.024 | 67 | 0.35 | 3.20 | 22.686 | 73 | 0.33 | 0.913 |
| K00157 | 5685 | II/IV | 2.92 | 13.024 | 67 | 0.35 | 4.37 | 31.995 | 87 | 0.79 | 0.668 |
| K00157 | 5685 | II/V | 2.92 | 13.024 | 67 | 0.35 | 2.60 | 46.687 | 40 | 0.49 | 1.123 |
| K00157 | 5685 | II/VI | 2.92 | 13.024 | 67 | 0.35 | 3.43 | 118.360 | 54 | 0.36 | 0.851 |
| K00157 | 5685 | III/IV | 3.20 | 22.686 | 73 | 0.33 | 4.37 | 31.995 | 87 | 0.79 | 0.732 |
| K00157 | 5685 | III/V | 3.20 | 22.686 | 73 | 0.33 | 2.60 | 46.687 | 40 | 0.49 | 1.231 |
| K00157 | 5685 | III/VI | 3.20 | 22.686 | 73 | 0.33 | 3.43 | 118.360 | 54 | 0.36 | 0.933 |
| K00157 | 5685 | IV/V | 4.37 | 31.995 | 87 | 0.79 | 2.60 | 46.687 | 40 | 0.49 | 1.681 |
| K00157 | 5685 | IV/VI | 4.37 | 31.995 | 87 | 0.79 | 3.43 | 118.360 | 54 | 0.36 | 1.274 |
| K00157 | 5685 | V/VI | 2.60 | 46.687 | 40 | 0.49 | 3.43 | 118.360 | 54 | 0.36 | 0.758 |

Table 2
Planet-radii Ratios Summary Grouped by Number of KOIs

|  | All <br> Systems | 2-KOI <br> Systems | 3-KOI <br> Systems | 4-KOI <br> Systems | 5-KOI <br> Systems | 6-KOI <br> Systems |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of stellar systems | 96 | 42 | 33 | 14 | 6 | 1 |
| No. of $R_{\text {inner }} / R_{\text {outer }}$ pairs | 159 | 42 | 55 | 27 | 22 | 13 |
| No. of $R_{\text {inner }} / R_{\text {outer }}<1$ | 95 | 26 | 33 | 16 | 11 | 9 |
| No. of $R_{\text {inner }} / R_{\text {outer }}>1$ | 64 | 16 | 22 | 11 | 11 | 4 |
| $\chi^{2}$ statistic $^{\text {a }}$ | 6.0 | 2.4 | 2.2 | 0.93 | 0.0 | 1.9 |
| $\chi^{2}$ probability | 0.014 | 0.13 | 0.14 | 0.34 | 1.0 | 0.16 |
| Fraction $R_{\text {inner }} / R_{\text {outer }}<1$ | 0.597 | 0.619 | 0.600 | 0.592 | 0.500 | 0.692 |
| Lower $1 \sigma$ confidence | 0.042 | 0.089 | 0.076 | 0.115 | 0.126 | 0.179 |
| Upper $1 \sigma$ confidence | 0.041 | 0.082 | 0.072 | 0.107 | 0.126 | 0.140 |

Note. ${ }^{\text {a }}$ The $\chi^{2}$ statistic and probability are based upon comparison of the observed fractions to the null hypothesis fractions of $50 \%$.

We also have performed three additional observational tests to assess if the observed fraction may be the result of an unrecognized bias in the sample. The first test repeated the above analysis, but for each unique planet pair, the measured
radii were replaced with radii randomly drawn from the overall radius distribution as measured by Kepler; the same set of periods within a given system was retained. The same impact parameter and $\mathrm{S} / \mathrm{N}$ restrictions described above (Section 2)


Figure 4. Observed fraction of planet pairs with $R_{\text {inner }} / R_{\text {outer }}<1$ is plotted as a function of signal-to-noise cutoff, showing the fraction asymptotically approaches the a value of $\sim 0.6$ for $\mathrm{S} / \mathrm{N} \gtrsim 20$. The dashed line marks the observed fraction (and the $1 \sigma$ confidence interval; dotted lines) for an $\mathrm{S} / \mathrm{N}_{\text {threshold }}=25$ (from Figure 3).
were applied (e.g., if a planet radius was drawn that was too small to be detected at the orbital period ( $\mathrm{S} / \mathrm{N}<25$ ), a new radius was randomly drawn until the $\mathrm{S} / \mathrm{N}$ threshold was met). The random draw was performed 10,000 times for each unique pair of planets, and the cumulative distribution of the planet-radii ratios for all of the random draws is displayed in Figure 3. As expected, the random draw distribution displays no size ordering preference; i.e., the fraction of planets with $R_{\text {inner }} / R_{\text {outer }}<1$ is $\approx 50 \%$. Based upon a Kolmogorov-Smirnov test, the observed distribution and the random draw distribution are not drawn from different parent distributions with only a probability of $3 \times 10^{-8}$-indicating that the observed planetradii ratio distribution has a preferential ordering such that smaller planets are in orbits interior to larger planets.

We also tested if the observed fraction of planet-radii ratios with $R_{\text {inner }} / R_{\text {outer }}<1$ is dependent upon the $\mathrm{S} / \mathrm{N}$ threshold chosen. In Figure 4, the fraction of planet pairs where the inner planet is smaller than the outer planet is plotted as a function of the required $\mathrm{S} / \mathrm{N}$ threshold. If no $\mathrm{S} / \mathrm{N}$ threshold is required, the fraction is $>70 \%$, and as the $\mathrm{S} / \mathrm{N}$ threshold is increased, the fraction systematically decreases and levels out near $\sim 60 \%$. The higher fractions at a lower $\mathrm{S} / \mathrm{N}$ threshold result from incompleteness of the sample (i.e., it is easier to detect larger planets at all orbital periods). As the $\mathrm{S} / \mathrm{N}$ threshold is increased the fraction of planet-radii ratios below unity decreases, but does not systematically approach $50 \%$, as would be expected if there were no preferential size ordering of the planets. Rather, the fraction asymptotically approaches $60 \%$ for $\mathrm{S} / \mathrm{N}_{\text {threshold }}>20$, indicating that the $\mathrm{S} / \mathrm{N}_{\text {threshold }}=25$ threshold ensures that the analysis presented in Figure 3 is based upon a sample not significantly biased by completeness.

The final test performed was to determine if the observed fraction is dependent upon the maximum period of the outer planet (see Figure 5). Transit surveys are typically more complete at shorter orbit periods, and if there truly was no preference for planet size ordering, the fraction would decline and approach $50 \%$ as the maximum orbit period was decreased. Within the confidence intervals, the observed fractions are independent of the maximum outer orbital period and are consistent with the observed $\approx 60 \%$ fraction for the entire sample. The fractions do not approach $50 \%$ at shorter orbital period as would be expected


Figure 5. Observed fraction of planet pairs with $R_{\text {inner }} / R_{\text {outer }}<1$ is plotted as a function of maximum outer orbital period cutoff, showing the fraction asymptotically approaches the value of $\sim 0.6$ for $P \gtrsim 20$. The dashed line marks the observed fraction for the whole sample; the dotted lines mark the $1 \sigma$ confidence interval (from Figure 3). The numbers above each data point indicate the number of planet pairs that appear in that period bin $\left(P_{\text {outer }}<P_{\max }\right)$.
for a random distribution. In fact, a slight (but not statistically significant) hint of a higher fraction is observed if the maximum period is $P<20$ days.

Overall, if the ordering of planets within a given system was random such that there was no sequential ordering of the planets by size, the probabilities of a planet-radii ratio being above or below unity would be equal. But that is not what is observed; the three tests above (i.e., the random radius draw, the $\mathrm{S} / \mathrm{N}_{\text {threshold }}$, and the maximum outer orbital period), in combination with the $\chi^{2}$ probability statistic and the confidence intervals, indicate that for $\approx 60 \%(2.5 \sigma)$ of the unique planet pairs within the Kepler multiple-planet systems, the inner planet is smaller than the outer planet, with only a $1.4 \%$ chance of this being observed by chance. In the following subsections, we explore if and how the number of planets in the system, the orbital separation of the planets, the temperature of the stars, and the size of the planets themselves may affect the observed size hierarchy of the planets in multiple-planet systems.

### 3.1. The Number of Planets and Orbital Separation

If formation and evolutionary mechanisms within a planetary system affect the size distribution and ordering of planets within a system, one might expect to observe differences in the size ordering as a function of the number of planets within a system. When the planets are divided into groups based upon the number of detected planetary candidates in the system (e.g., two-, three-, four-, five-, and six candidates), the fractions do not change appreciably from the fractions calculated for the entire sample set. This can be seen in both the $\chi^{2}$ statistic (Table 2) where the $\chi^{2}$ and associated probabilities are all comparable to each other and in Figure 6, where the observed fractions (with confidence intervals) are plotted and display no dependence on the number of planets in the system. While the number of systems with more than three planets have relatively large uncertainties and poor statistics because of the small numbers of the four-, five-, and six-candidate systems, there is no correlation of the fraction of size-ordered planets with the number of planets within a planetary system.

It might be expected that planets nearer to the central star would undergo a higher level of photoevaporation than planets


Figure 6. Observed fraction of planet pairs with the inner planet being smaller than the outer planet plotted as a function of the number of KOIs within a system. The dashed line marks the observed fraction for the whole sample; the dotted lines mark the $1 \sigma$ confidence interval (from Figure 3).
at longer orbital periods and, thus, the relative sizes of the planets would be more extreme if the planets are more widely separated (larger orbital period ratio). To test this, we have plotted the planet-radii ratios versus the orbital period ratios and the inner and outer planet orbital periods (Figure 7). Using the Spearman non-parametric rank correlation function, we find that the distributions are likely uncorrelated. The correlation coefficients for the three distributions shown in Figure 7 are $0.14,0.22$, and 0.10 with probabilities to be exceeded in the null hypothesis of $0.06,0.004$, and 0.08 , respectively.

Additionally, to search for a non-zero slope that might indicate the planet-radii ratios are related to or dependent upon the period or period spacings, we have fitted a linear model ${ }^{6}$ to each of the distributions. Each of the distributions are statistically consistent with a flat distribution as a function of period ratio and orbital period; the slopes of the fitted linear models were found to be $0.29 \pm 0.15$ for the radii ratios versus period ratios (Figure 7 top), $0.0009 \pm 0.001$ for the radii ratios versus the inner orbital period (Figure 7 middle), and $-0.0002 \pm 0.0005$ for the radii ratios versus the outer orbital period (Figure 7 bottom). In general, we find no correlation between the orbital period separation (or orbital periods themselves) and the size ordering of the planets.

### 3.2. Stellar Temperature

We have also explored whether there is a correlation between the distribution of planet-radii ratios and the effective temperature of the host stars. We have produced planet-radii ratio distributions, but separated out by the stellar temperature. We chose temperature ranges that roughly correspond to the spectral classification of M- and K-stars ( $<5000 \mathrm{~K}$ ), G-stars (5000-5800 K), and F-stars ( $>5800 \mathrm{~K}$; Ciardi et al. 2011). The cumulative distributions of the planet-radii ratios for each of the stellar temperature groups are displayed in Figure 8.
Overall, all three distributions are shifted to lower ratios in comparison to the random draw distribution from Figure 3. Kolmogorov-Smirnov tests between the three distributions indicate that the three distributions do not result from different parent distributions with probabilities of $>75 \%$, indicating

[^0]

Figure 7. Top: distribution of the planet-radii ratios as a function of the orbital period ratio. Middle: distribution of the planet-radii ratio as a function of the inner planet orbital period. Bottom: distribution of the planet-radii ratio as a function of the outer planet orbital period. In each panel, the horizontal dashed line marks unity, and the dot-dashed line delineates the median planet-radii ratio of 0.91 for the entire sample.
that, in general, the preferential planet size ordering occurs at approximately the same level (i.e., $\approx 60 \%$ of the unique planet pairs have $R_{\text {inner }} / R_{\text {outer }}<$ ) across the stellar temperature range. A summary of the planet-radii ratios, the fraction of ratios that exhibit smaller inner planets, and the significance of those fractions based upon the confidence intervals and $\chi^{2}$ statistic is given in Table 3 for each of the stellar temperature groups.

There does appear to be a slight trend such that as the stars become warmer they contain a larger fraction of planet pairs sequentially ordered by radius. For the cooler stars ( $<5000 \mathrm{~K}$ ), this fraction is $55 \% \pm 9 \%$, while for the warmer stars ( $>5800 \mathrm{~K}$ ), this fraction is $65 \% \pm 9 \%$. The resulting $\chi^{2}$ statistics for these three samples indicates that the observed fractions differ from the null hypothesis fraction of $50 \%$ more significantly for the warmer stars than for the cooler stars (Table 3). This trend could be a result of higher planetary evaporation rates associated


Figure 8. Top: observed cumulative distributions of the planet-radii ratios as displayed in Figure 3, except the distributions have been separated out by stellar effective temperature and identified by the plot colors (as labeled in the plot). The plot markings are the same as those in Figure 3. Bottom: cumulative distributions of the individual radii for the planets that are used to determine the planet-radii ratios throughout the paper, separated out by stellar effective temperature (as labeled in the plot).

Table 3
Planet-radii Ratios Grouped by Stellar Temperature

|  | $c$ <br> Stars | $5000-5800 \mathrm{~K}$ <br> Stars | $<5000 \mathrm{~K}$ |
| :--- | :---: | :---: | :---: |
|  | 22 | 47 | Stars |
| No. of stellar systems | 40 | 79 | 27 |
| No. of $R_{\text {inner }} / R_{\text {outer }}$ Pairs | 26 | 47 | 40 |
| No. of $R_{\text {inner }} / R_{\text {outer }}<1$ | 14 | 32 | 22 |
| No. of $R_{\text {inner }} / R_{\text {outer }}>1$ | 3.6 | 2.9 | 18 |
| $\chi^{2}$ statistic | 0.06 | 0.09 | 0.4 |
| $\chi^{2}$ probability | 0.650 | 0.594 | 0.50 |
| Fraction $R_{\text {inner }} / R_{\text {outer }}<1$ | 0.091 | 0.062 | 0.550 |
| Lower $1 \sigma$ confidence | 0.082 | 0.060 | 0.091 |
| Upper $1 \sigma$ confidence | 2.59 | 2.63 | 0.088 |
| Median planet radius $\left(R_{\oplus}\right)$ | 1.49 | 1.18 | 2.19 |
| Med. abs. dev. $\left(R_{\oplus}\right)$ | 1.09 | 0.75 | 0.61 |
| Min. planet radius $\left(R_{\oplus}\right)$ | 9.68 | 13.2 | 1.03 |
| Max. planet radius $\left(R_{\oplus}\right)$ |  |  | 4.73 |

with the higher luminosity stars or perhaps could result from the warmer (i.e., more massive) stars tending to contain larger (i.e., more massive) planets (see Figure 8 and Table 3).
The median planet radius does not vary significantly between the three stellar groups (2.2-2.6 $R_{\oplus}$; see Table 3), but the size of the largest planets in each group does. The G and F stars ( $T_{\text {eff }}>5000 \mathrm{~K}$ ) contain Saturn-sized and Jupiter-sized planets


Figure 9. Comparison of the inner planet radius to the outer planet radius for each pair of planets, The dashed line delineates unity and the dotted lines mark the boundaries where one planet is $50 \%$ bigger than the planet to which it is compared (ratio $=0.67$ if the outer planet is larger and ratio $=1.5$ if the inner planet is larger).


Figure 10. Distribution of the planet radii for those planet pairs where one planet is $>50 \%$ larger than the other planet. The top panel is for those planet pairs where the outer planet is larger than the inner planet ( $R_{\text {inner }} / R_{\text {outer }} \leqslant 0.67$ ); the bottom panel is for those planet pairs where the inner planet is larger than the outer planet ( $R_{\text {inner }} / R_{\text {outer }} \geqslant 1.5$ ).
(in addition to smaller planets), while the cooler ( $T_{\text {eff }}<5000 \mathrm{~K}$ ) contain Neptune-sized planets and smaller (see Figure 8 and Table 3). In this sample, $15 \%$ of the planets around G-stars and $25 \%$ of the planets around the F-stars are Neptune-sized or larger; the cooler stars host only six (4\%) planets larger than Neptune, and these four planets orbit three stars with effective temperatures of $>4900 \mathrm{~K}$ (KOI 757, 884, 941). The absence of large planets around cooler stars is evident in the cumulative


Figure 11. Fraction of planet pairs with $\left(R_{\text {inner }} / R_{\text {outer }}<1\right)$ are plotted as a function of maximum planet radius. In the top panel, only those planet pairs are included that have at least one planet that is larger than a planet radius $R_{p}$. In the middle panel, only those planet pairs are included where both planets are smaller than a planet radius $R_{p}$. In the bottom panel, only those planet pairs are included where both planets are larger than a planet radius $R_{p}$. The numbers underneath each data point list the number of pairs in that bin. In each panel, the dashed-dot line and gray area delineate the fraction and uncertainties found for the entire sample (from Figure 3); the dashed line delineates the $50 \%$ fraction.
distribution of the planet radii (Figure 8) and in the smaller median absolute deviations of the median planet radius for each stellar group (Table 3).

This paper is not intended to provide a discussion of the occurrence rates of planets or a detailed analysis of the size distribution of planets (e.g., Howard et al. 2012), but this may imply that the cooler (i.e., smaller) stars only produce smaller planets that do not preferentially follow a size hierarchy of planets. In fact, large planets around small stars may not form at all (Endl et al. 2003; Johnson et al. 2010) or, if they do, they may not survive their youth (e.g., van Eyken et al. 2012). Thus, cool stars may only be left with a population of relatively small planets (Lopez et al. 2012). The warmer stars, in contrast, appear to host a larger array of planet sizes with a slightly higher preference for the larger planets ( $>$ Neptune-sized) to be in longer orbits exterior to the orbits of the smaller planets. Given that there appears to be only a weak correlation with the planet-radii ratio and the orbital period (ratio), perhaps the formation and migration of large planets (perhaps in conjunction with photoevaporation of the innermost planets) is necessary for a radius hierarchy to be present.

### 3.3. Planet Radius

If hotter stars tend to show a planet radius hierarchy and the hotter stars also host relatively larger planets, then the planet hierarchy might be expected to be correlated with the planet size. In Figure 9, we compare the sizes of the planet radii for the inner and outer planets for each pair of planets within the sample. The overall planet-radii ratio is near unity but there is more scatter below than above the unity line (i.e., smaller planets are interior to larger planets). There are 36 planet pairs where the outer planet is $>50 \%$ larger than the inner planet ( $R_{\text {inner }} / R_{\text {outer }} \leqslant 0.67$ ); in contrast, there are only 13 planet pairs where the inner planet is $>50 \%$ larger than the outer planet ( $R_{\text {inner }} / R_{\text {outer }} \geqslant 1.5$ ).

For the planet pairs that are in these relatively extreme ratio pairs, we have plotted the radii distributions of the candidates, separated out by inner and outer planet and by the sense of the ratio (see Figure 10). For the pairs where the outer planet is significantly larger, the ratio tends to be dominated by relatively large planets. Half $(18 / 36)$ of the outer planets are Neptunesized or larger $\left(>4 R_{\oplus}\right)$, while only $25 \%(9 / 36)$ of the inner

Table 4
Planet-radii Ratios Summary Group by Maximum Planet Radius

| $R_{p}=$ | $1.5 R_{\oplus}$ | $2.0 R_{\oplus}$ | $2.5 R_{\oplus}$ | $3.0 R_{\oplus}$ | $3.5 R_{\oplus}$ | $4.0 R_{\oplus}$ | $4.5 R_{\oplus}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| At least one planet in the planet pair is larger than $R_{p}$ |  |  |  |  |  |  |  |
| No. of stellar systems | 93 | 86 | 63 | 44 | 29 | 23 | 18 |
| No. of $R_{\text {inner }} / R_{\text {outer }}$ Pairs | 154 | 138 | 106 | 74 | 49 | 42 | 29 |
| No. of $R_{\text {inner }} / R_{\text {outer }}<1$ | 93 | 87 | 71 | 50 | 32 | 30 | 22 |
| No. of $R_{\text {inner }} / R_{\text {outer }}>1$ | 61 | 51 | 35 | 24 | 17 | 12 | 7 |
| $\chi^{2}$ statistic | 6.7 | 9.4 | 12.2 | 9.1 | 4.6 | 7.7 | 7.8 |
| $\chi^{2}$ probability | 0.009 | 0.002 | 0.0005 | 0.003 | 0.03 | 0.005 | 0.005 |
| Fraction $R_{\text {inner }} / R_{\text {outer }}<1$ | 0.603 | 0.630 | 0.670 | 0.676 | 0.653 | 0.714 | 0.759 |
| Lower $1 \sigma$ confidence | 0.043 | 0.045 | 0.052 | 0.063 | 0.081 | 0.086 | 0.105 |
| Upper $1 \sigma$ confidence | 0.041 | 0.043 | 0.048 | 0.058 | 0.073 | 0.075 | 0.084 |
| No planets in the planet pair are larger than $R_{p}$ |  |  |  |  |  |  |  |
| No. of stellar Systems | 5 | 15 | 38 | 58 | 73 | 78 | 82 |
| No. of $R_{\text {inner }} / R_{\text {outer }}$ pairs | 5 | 20 | 53 | 85 | 110 | 117 | 130 |
| No. of $R_{\text {inner }} / R_{\text {outer }}<1$ | 2 | 7 | 24 | 45 | 63 | 65 | 73 |
| No. of $R_{\text {inner }} / R_{\text {outer }}>1$ | 3 | 13 | 29 | 40 | 47 | 52 | 57 |
| $\chi^{2}$ statistic | 0.0 | 1.8 | 0.47 | 0.29 | 2.3 | 1.4 | 1.9 |
| $\chi^{2}$ probability | 1.0 | 0.18 | 0.49 | 0.59 | 0.13 | 0.23 | 0.16 |
| Fraction $R_{\text {inner }} / R_{\text {outer }}<1$ | 0.400 | 0.350 | 0.453 | 0.529 | 0.572 | 0.555 | 0.561 |
| Lower $1 \sigma$ confidence | 0.253 | 0.088 | 0.076 | 0.060 | 0.052 | 0.050 | 0.048 |
| Upper $1 \sigma$ confidence | 0.302 | 0.164 | 0.078 | 0.059 | 0.051 | 0.049 | 0.046 |
| Both planets in the planet pair are larger than $R_{p}$ |  |  |  |  |  |  |  |
| No. of stellar systems | 89 | 67 | 42 | 21 | 13 | 11 | 10 |
| No. of $R_{\text {inner }} / R_{\text {outer }}$ pairs | 138 | 98 | 64 | 30 | 15 | 13 | 10 |
| No. of $R_{\text {inner }} / R_{\text {outer }}<1$ | 82 | 59 | 42 | 21 | 10 | 8 | 6 |
| No. of $R_{\text {inner }} / R_{\text {outer }}>1$ | 56 | 39 | 22 | 9 | 5 | 5 | 4 |
| $\chi^{2}$ statistic | 4.9 | 4.1 | 6.2 | 4.8 | 1.7 | 0.69 | 0.4 |
| $\chi^{2}$ probability | 0.03 | 0.04 | 0.01 | 0.03 | 0.20 | 0.40 | 0.50 |
| Fraction $R_{\text {inner }} / R_{\text {outer }}<1$ | 0.594 | 0.602 | 0.656 | 0.700 | 0.667 | 0.615 | 0.600 |
| Lower $1 \sigma$ confidence | 0.046 | 0.055 | 0.069 | 0.106 | 0.162 | 0.141 | 0.204 |
| Upper $1 \sigma$ confidence | 0.044 | 0.053 | 0.064 | 0.091 | 0.135 | 0.172 | 0.180 |

planets are very small (e.g., Earth-sized $<1.5 R_{\oplus}$ ) planets. In contrast, for those planet pairs where the inner planet is much larger than the outer planet, the pairs are evenly split between relatively small outer planets ( $6 / 13$ are $<1.5 R_{\oplus}$ ) and relatively large inner planets ( $5 / 13>4 R_{\oplus}$ ).

It appears that for there to be a planet radius hierarchy, one of the planets most often needs to be $\sim$ Neptune-sized or larger. To explore this more closely, we have calculated the fraction of planet pairs with ( $R_{\text {inner }} / R_{\text {outer }}<1$ ), if at least one planet is larger than some maximum planet radius $\left(R_{p}\right)$, or if both planets are smaller than that same maximum planet radius $\left(R_{p}\right)$, or if both planets are larger than that same maximum planet radius. The fractions were calculated for maximum planet radii of $R_{p}=[1.5,2.0,2.5,3.0,3.5,4.0,4.5] R_{\oplus}$ (see Figure 11) and are tabulated in Table 4.

If planet pairs with planets larger than $3 R_{\oplus}$ are excluded, the fraction is very near $50 \%$ with little preference for sequential planet ordering, but if one planet in the pair is larger than $\sim 3 R_{\oplus}$, the observed fraction of planet pairs with $R_{\text {inner }} / R_{\text {outer }}<1$ is $68 \pm 6 \%-\mathrm{a} 3 \sigma$ separation from the random ordering fraction of $50 \%$ (see Table 4). Based upon the $\chi^{2}$ statistic and probability and the confidence intervals, the fraction of planet pairs is significantly above $50 \%$ only when Neptune-sized planets or larger are allowed in the pairs.

The fraction is most significant when Neptune-sized or larger planets are compared to planets of all sizes (top panel Figure 11); the $\chi^{2}$ statistic are all $>4$ with a $\lesssim 1 \%$ probability that the non $-50 \%$ fractions are achieved solely by chance. When the sizes of both planets are restricted to radii smaller than Neptune,
the fractions remain near or below 50\% (middle panel Figure 11 and Table 4), with a $\gtrsim 15 \%$ probability of the observed fractions being generated by chance for the null-hypothesis distribution. When both planets within a planet pair are restricted to planets larger than a certain radius, sequential ordering of the planet sizes is still apparent, but is less significant (bottom panel Figure 11 and Table 4). If both planets in a pair are $\gtrsim 3.0 R_{\oplus}$, then the observed fraction of planet pairs where the inner planet is smaller than the outer planet is consistent with no planet size hierarchy. These results suggest that the size ordering primarily occurs when a system contains both super-Earth-sized (or Earthsized) planets and Neptune-sized or larger planets, and may be a direct result of the shepherding of smaller inner planets by larger outer planets (Raymond et al. 2008).

## 4. SUMMARY

We have performed a study of the relative sizes of planets within the multiple-candidate systems using the Kepler planetary candidate list (Batalha et al. 2012). For each multiple-planet system, we have compared the radius of each planet to the radius of every other planet within a planetary system, after correcting for detection biases. We find that for planet pairs for which one or both objects is approximately Neptune-sized for larger, the larger planet is most often the planet with the longer period, while no such size-location correlation is seen for pairs of planets when both planets are smaller than Neptune. Overall, for all planet pairs in the sample, $60 \% \pm 4 \%$ of the unique planet pairs are structured in a hierarchical manner such that the inner
planet is smaller than the outer planet. If at least one planet in the planet pair is Neptune-sized or larger $\left(\gtrsim 3 R_{\oplus}\right)$, the fraction of inner planets being smaller than outer planets is $\approx 68 \% \pm 6 \%$. However, if both planets are smaller than Neptune, then the fraction is consistent with random planet ordering ( $53 \% \pm 6 \%$ ) with no apparent size hierarchy.

The planet radius size hierarchy may be a natural consequence of planetary formation and evolution. In particular, the sequential ordering may be a result of a combination of core accretion, migration, and evolution. Core accretion models predict that smaller planets are expected to form prior to and interior to the giant planets (Zhou et al. 2005). Additionally, larger planets formed farther out may migrate inward, shepherding smaller planets inward as the planets move (Raymond et al. 2008).

This scenario is consistent with the planet size hierarchy being observed for planet pairs involving Neptune-sized planets, but being absent for small planet pairs and for the planets around cool stars. For the cooler stars, the forming planets may begin migrating prior to starting rapid gas accretion (e.g., Ida \& Lin 2005), coupled with a lower extreme ultraviolet luminosity that is not capable of substantially evaporating the planets (Lopez et al. 2012). For example, Lopez et al. (2012) suggest that the Kepler-11 planets did not form in situ, but rather, the planets formed beyond the snow line, migrated inward, and were evaporated by the star to their present sizes.

These scenarios (perhaps all in concert) predict a radius hierarchy of planets as a function of orbital distance from the central host star, in particular predicting that Neptune-sized and larger planets are outside super-Earth and terrestrial-sized planets. As Kepler discovers more planets in longer orbital periods, it will be interesting to learn if our solar system is indeed typical of the planetary architectures found in the Galaxy.

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[^0]:    6 Fitting was done with an outlier resistant linear regression routine based upon Numerical Recipes (Press et al. 2007).

