

THE BLUE TIP OF THE STELLAR LOCUS: MEASURING REDDENING WITH THE SLOAN DIGITAL SKY SURVEY

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ABSTRACT

We present measurements of reddening due to dust using the colors of stars in the Sloan Digital Sky Survey (SDSS). We measure the color of main-sequence turnoff stars by finding the “blue tip” of the stellar locus: the prominent blue edge in the distribution of stellar colors. The method is sensitive to color changes of order 18, 12, 7, and 8 mmag of reddening in the colors $u - g$, $g - r$, $r - i$, and $i - z$, respectively, in regions measuring 90' by 14'. We present maps of the blue tip colors in each of these bands over the entire SDSS footprint, including the new dusty southern Galactic cap data provided by the SDSS-III. The results disfavor the best-fit O'Donnell and Cardelli et al. reddening laws, but are described well by a Fitzpatrick reddening law with $R_V = 3.1$. The Schlegel et al. (SFD) dust map is found to trace the dust well, but overestimates reddening by factors of 1.4, 1.0, 1.2, and 1.4 in $u - g$, $g - r$, $r - i$, and $i - z$ largely due to the adopted reddening law. In select dusty regions of the sky, we find evidence for problems in the SFD temperature correction. A dust map normalization difference of 15% between the Galactic north and south sky may be due to these dust temperature errors.

Key words: dust, extinction – Galaxy: stellar content – ISM: clouds

Online-only material: color figures

1. INTRODUCTION

Most astronomical observations are affected by Galactic interstellar dust, whether as a source of foreground light in the microwave, far-infrared (FIR), and gamma-ray wavelength regions or as a cause of extinction in the infrared through ultraviolet (Draine 2003). Characterizing the properties of the dust and accounting for its effects on observations is then a central problem in astronomy.

Dust is formed as stars burn nuclear fuel to form heavy elements and emit these elements in stellar winds or in more violent eruptions, and these elements are reprocessed in the interstellar medium (ISM; Draine 2009). The distribution of dust is correspondingly correlated with the hydrogen in the ISM, though the dust-to-gas ratio varies. Burstein & Heiles (1978, hereafter BH) took advantage of the correlation between H I and dust column density to make the first widely used map of dust column density, combining H I emission and galaxy counts.

The BH dust map was superseded by the Schlegel et al. (1998, hereafter SFD) dust map, which took advantage of the full-sky FIR data provided by IRAS and DIRBE, which are dominated by thermal emission from the Galactic dust at wavelengths of 100 μm and longer. After correction for dust temperature using FIR color ratios, these maps trace dust column density. Calibration of dust column density to color excess $E(B - V)$ was performed using the colors of a sample of 389 galaxies with Mg_2 indices (Faber et al. 1989), which were also used to test the performance of the resulting map.

The advent of large astronomical surveys permits stronger tests of the SFD dust map and the assumptions used to construct

it. We test the SFD dust map using the colors of stars from the Sloan Digital Sky Survey (SDSS; York et al. 2000), including the recently completed SDSS-III imaging (Weinberg et al. 2007), which covers about 2000 deg² in the southern Galactic sky. This allows us to more tightly constrain the SFD normalization and the dust extinction spectrum, or “reddening law,” over the SDSS bands, as well as to provide a map of color residuals that point to problems with the SFD dust map, and particularly with the temperature correction.

Previous tests of SFD have usually found that SFD overpredicts extinction in high-extinction regions. Shortly after its introduction, Arce & Goodman (1999) found that SFD extinction was too high by 40% in Taurus, using star counts, colors, and FIR emission. Likewise, studies using globular cluster photometry, galaxy counts, and NIR colors have found that SFD overpredicts extinction by a similar fraction in other dusty regions (Stanek 1998; Chen et al. 1999; Yasuda et al. 2007; Rowles & Froebrich 2009). Cambr  s et al. (2001) explore the link between the SFD overestimation and dust temperature using star counts in the Polaris Flare. At $|b| < 40^\circ$, Dobashi et al. (2005) use optical star counts to conclude that SFD overpredicts extinction by a factor of two or more. We perform tests similar to these in regions of lower extinction than had been previously possible, taking advantage of the high quality and depth of the SDSS stellar photometry, and complementing the recent work of Peek & Graves (2010), who use SDSS galaxy spectra. In these regions, we do not find that SFD overpredicts reddening by a large factor; rather, we find that SFD overpredicts reddening by about 14% in $B - V$, though, because of the reddening law adopted by SFD, this varies from color to color.

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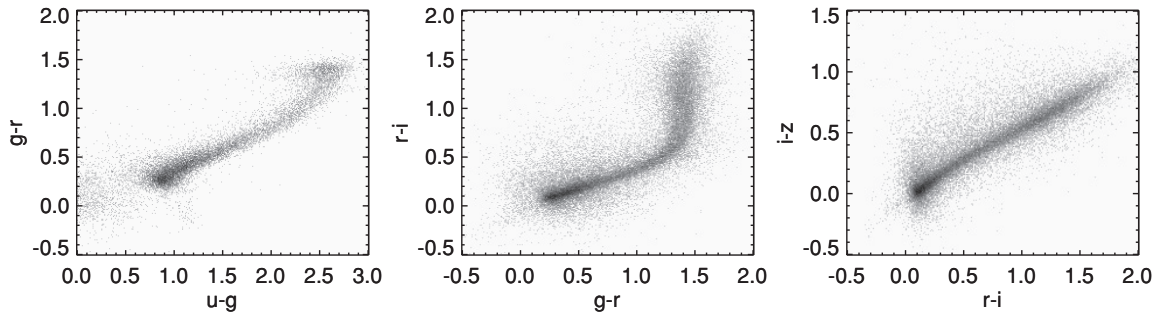


Figure 1. Color–color diagrams for point sources from the SDSS, within two degrees of the north Galactic pole. The sharp cutoff in stellar density blueward of the “blue tip” is prominent. In $u - g$, the points blueward of the blue tip are mostly quasars and white dwarfs. The blue tip is at about 0.8, 0.2, 0.1, and 0.0 mag in $u - g$, $g - r$, $r - i$, and $i - z$, respectively.

The colors of stars vary substantially with stellar type, and with location in the Galaxy due to the effect of metallicity on color. Nevertheless, we find that the colors of the most blue main-sequence stars in old populations—the main-sequence turnoff (MSTO) stars—are remarkably stable over the sky, and that we can empirically model their slow spatial variation. We therefore present measurements of the colors of the “blue tip” of the stellar locus, and use them to constrain the SFD dust map. This work is akin to that of High et al. (2009), in which the color of stellar populations is also used as a sort of color standard.

In Section 2, we describe the data sets used in this work: the SDSS imaging data and the SFD dust map. In Section 3, we present our method for measuring the blue tip of the stellar locus, and the corresponding maps of blue tip colors on the sky. In Section 4, we present fits of the SFD dust map to the blue tip colors. In Sections 5 and 6, we discuss these results and conclude. The blue tip maps and measurements can be found at the Web site <http://www.skymaps.info/bluetip>.

2. DATA

2.1. The SDSS

The SDSS is a digital spectroscopic and photometric survey, that, with the additional south Galactic cap (SGC) data provided by the SDSS-III, covers just over one-third of the sky, mostly at high latitudes (Abazajian et al. 2009). The SDSS provides near-simultaneous imaging in five optical filters: u , g , r , i , and z (Gunn et al. 1998; Fukugita et al. 1996). The photometric pipeline has uniformly reduced data for about 10^8 stars. The SDSS is 95% complete up to magnitudes 22.1, 22.4, 22.1, 21.2, and 20.3 in u , g , r , i , and z . The SDSS imaging is performed in a drift-scanning mode in which the shutter is left open while the telescope moves at a constant angular speed across the sky. The resulting imaging “runs” tend to cover strips of sky that are long in right ascension and narrow in declination. These runs are divided into fields, which are 13.5° by $9'$ in size. We use SDSS data that have been photometrically calibrated according to the “ubercalibration” procedure of Padmanabhan et al. (2008).

2.2. The SFD Dust Map

The SFD dust map is a map of thermal emission from dust based on the *IRAS* 100 μm maps. The *IRAS* 100 μm map underwent three major processing steps before being used in the SFD dust map: it was destriped, zodiacal-light-subtracted, and calibrated to match *COBE*/DIRBE at degree scales. The first and third of these steps were necessary because the zero point of the *IRAS* 100 μm detector varied over time, imprinting

the *IRAS* scan pattern on the data in the form of stripes, and making the overall zero point of the data uncertain. The zodiacal-light subtraction is needed to remove the signature of the hot, bright, local interplanetary dust from the *IRAS* and DIRBE data, which, though bright, contributes negligibly to the reddening. The DIRBE 100–240 μm flux ratio is used to constrain the dust temperature and to transform the 100 μm flux map to a map proportional to dust column density. The destriped *IRAS* data have resolution of 6 arcmin, while the temperature correction is smoothed to degree scales. The destriped, temperature-corrected *IRAS* 100 μm map is normalized to a map of $E(B - V)$ by using a sample of 389 galaxies with Mg_2 indices and $B - V$ colors, for use as color standards (Faber et al. 1989).

3. THE BLUE TIP OF THE STELLAR LOCUS

Main-sequence stars are confined to a tight locus in color–color space, as is apparent from a typical SDSS color–color diagram (Figure 1). The locus has a sharp blue edge at the color of the MSTO stars, blueward of which there are only rare blue stragglers, white dwarfs, and quasars. The intrinsic color of the MSTO is set by the properties of the stellar population: primarily, metallicity and age. The observed colors of the MSTO are the intrinsic colors, altered by reddening due to dust and by systematic color shifts due to imperfect calibration of the observations. Empirically, the intrinsic color of the MSTO is slowly varying in space; the observed color of MSTO stars is therefore a good probe of the reddening due to dust.

Population effects cause the color of main-sequence stars to vary as a function of the magnitude of stars probed. At faint magnitudes and high latitudes, metal-poor halo stars dominate, rendering the MSTO stars bluer than at bright magnitudes and lower latitudes, where redder disk stars dominate (Figure 2). Moreover, the shape of the blue edge changes with magnitude: owing to photometric errors, the edge is sharp for bright stars and becomes blurred at fainter magnitudes. Accordingly, the typical color of MSTO stars depends on magnitude.

Stars of similar metallicities may clump together in the halo, changing the observed color of the blue tip. Because we do not have a good way to model such effects, we cannot distinguish such clumps from reddening due to dust in the blue tip maps.

3.1. Measuring the Blue Tip

We perform fits to the location of the blue tip of the stellar locus in each SDSS field (or group of SDSS fields). To avoid biasing the fits, we select stars in each field for analysis in a reddening-independent way, and then find the location of the blue tip in the resulting sample.

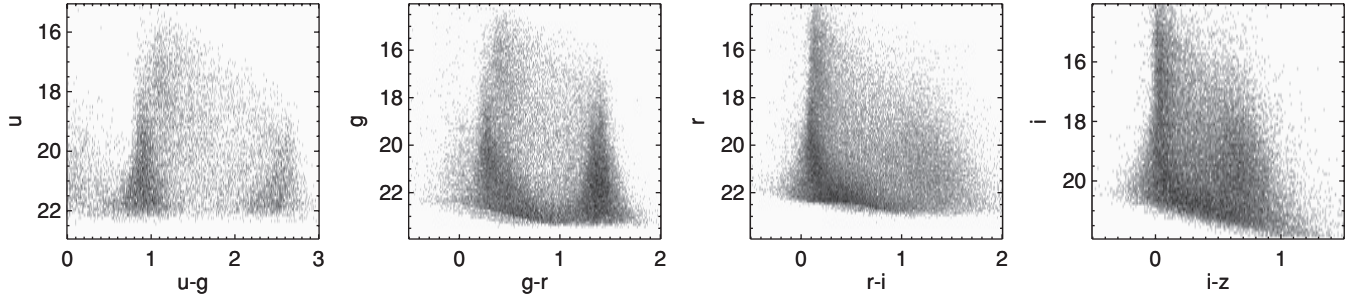


Figure 2. Color–magnitude diagrams from the SDSS, for the same stars as in Figure 1. The location of the blue edge of the stellar locus depends on magnitude, especially in the bluer bands, where bright, nearby, more metal-rich stars are redder than more distant halo stars. In $u - g$, blueward of the blue edge lie mostly quasars and white dwarfs. The location of the blue tip is as in Figure 1.

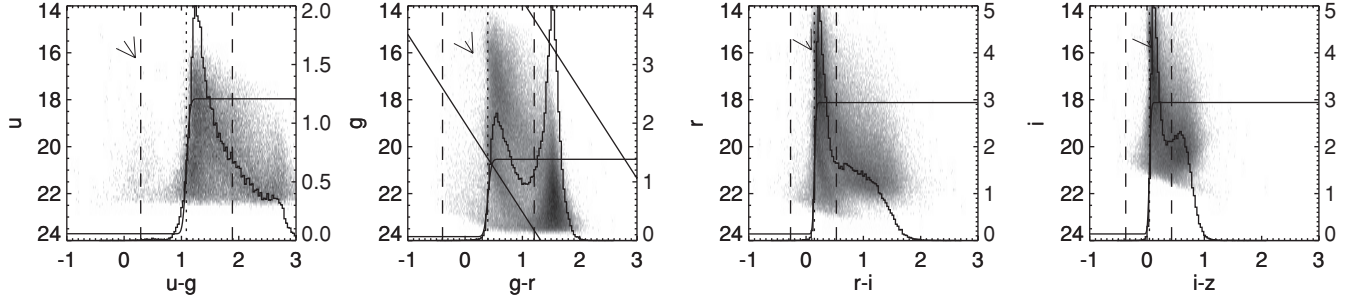


Figure 3. Example fits for the blue tip of the stellar locus in $u - g$, $g - r$, $r - i$, and $i - z$ for a one degree region around $l = 150^\circ$ and $b = 20^\circ$. A gray scale of the color–magnitude diagram is plotted, with features of the fit superimposed. The diagonal solid lines in the $g - r$ plot give the magnitude range within which stars are fitted, corresponding to $10 < D < 19$. One solid curve gives the distribution of stellar colors satisfying this cut. Another solid curve gives the pdf P that best fits this distribution, within the gray dashed vertical lines. The black dotted vertical line gives the derived location of the blue tip. The arrow in the upper left of the diagram gives the magnitude and direction of the reddening vector in this field, according to SFD. Finally, the right-hand axis gives the value of the pdf P ; its integral between the outer dashed lines is unity.

Care must be taken when imposing cuts on the stars in each field to avoid biasing the resulting blue tip color. Because extinction changes the observed magnitudes of stars, a flat cut on magnitude would bias the measurement, as the distance range probed would change with the dust column. Instead, we perform cuts on D , the g magnitude of a star projected along the reddening vector to zero color:

$$D = g - \frac{A_g}{A_g - A_r}(g - r). \quad (1)$$

Provided $A_g/(A_g - A_r)$ is accurate, the set of stars in a particular range of D is independent of the dust column toward the stars. D is related to the distance modulus of the MSTO stars (though not redder stars). Using the Jurić et al. (2008) “bright” photometric parallax relation, MSTO stars with $r - i = 0.1$ and $g - r = 0.2$ have $M_g = 5.3$. Accounting for the projection from $g - r = 0.2$ to zero color along the reddening vector, $D \approx g - M_g + 4.6$. In this work, we frequently use the range $10 < D < 19$. Including the effect of saturation on the bright end, this restriction on D selects stars with distances between about 1 and 8 kpc.

With a reddening-independent population of stars in hand, we measure the color of the blue edge of these stars in each SDSS color. The stellar colors are modeled as drawn from a probability distribution $P(x)$, taken to be a step function convolved with a Gaussian to reflect the photometric uncertainty and the intrinsic width of the blue edge. The maximum-likelihood location for the step is denoted by the “blue tip” of the locus. Specifically, the form of the probability distribution is taken to be

$$P = \frac{1}{2} \left[1 + \operatorname{erf} \left(\frac{x - x_0}{\sqrt{2}\sigma_P} \right) \right] + F, \quad (2)$$

where erf is the Gaussian error function, σ_P corresponds to the width of the edge, and F sets a floor to the probability distribution, to render the fit insensitive to the occasional white dwarf or blue straggler. In this work, we use $F = 0.05$. The variable x_0 is the only free parameter in the fits. We maximize the likelihood $\mathcal{L} = \prod_x P(x - x_0)$, where the product is taken over the color of all the stars satisfying the cuts in the field. The maximum likelihood location of x_0 gives the color of the blue tip. The final results of this work are insensitive to substantial changes in the floor F , from 0.01 to 0.05. The formal statistical uncertainty in the blue tip color is computed for each measurement by fitting $\mathcal{L}$ near the maximum likelihood to a Gaussian.

The width of the blue edge is set by a combination of the intrinsic width of the edge and the typical measurement error in star colors in the SDSS. We adopt the values 0.05, 0.05, 0.025, and 0.025 for the width parameter σ_P in the colors $u - g$, $g - r$, $r - i$, and $i - z$, respectively. Because the photometric uncertainty becomes larger at faint magnitudes, at high extinctions the observed blue edge is expected to broaden. Despite this, σ_P is kept constant in the fits, introducing the possibility of bias in the measurements. Nevertheless, as we look only at relatively bright ranges of D and low extinction, this is a minor effect. Simulations with a mock star catalog (Section 4.4) verify that for the range $10 < D < 19$ used in this work, the introduced bias in the recovered ratio of blue tip color to $E(B - V)$ is less than 2% in $u - g$ and smaller in the other colors.

Some example measurements of the blue tip of the stellar locus are illustrated in Figure 3. In these plots, features of the blue tip fit are overplotted on a gray scale giving the color–magnitude diagram of a one degree region around $l = 150^\circ$ and $b = 20^\circ$. The measurement is performed using stars with $10 < D < 19$, which corresponds to stars falling

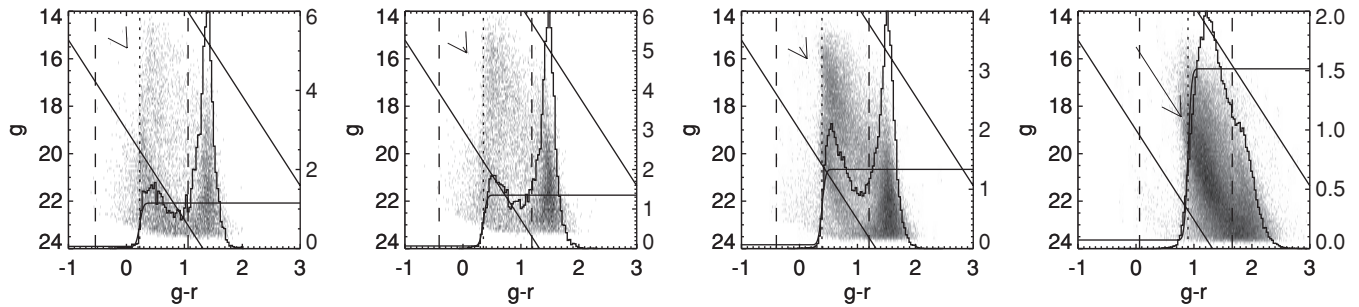


Figure 4. Example fits for the blue tip of the stellar locus in regions of increasing extinction, at $l = 150^\circ$ and $b = 80^\circ, 40^\circ, 20^\circ$, and 10° , from left to right. The SFD extinction prediction is indicated by the length of the arrow in the upper left of the diagram. As we approach the plane, the stellar density increases. At $b = 10^\circ$, the brightest stars are not behind all of the dust, and so the color of the blue tip becomes redder at fainter magnitudes.

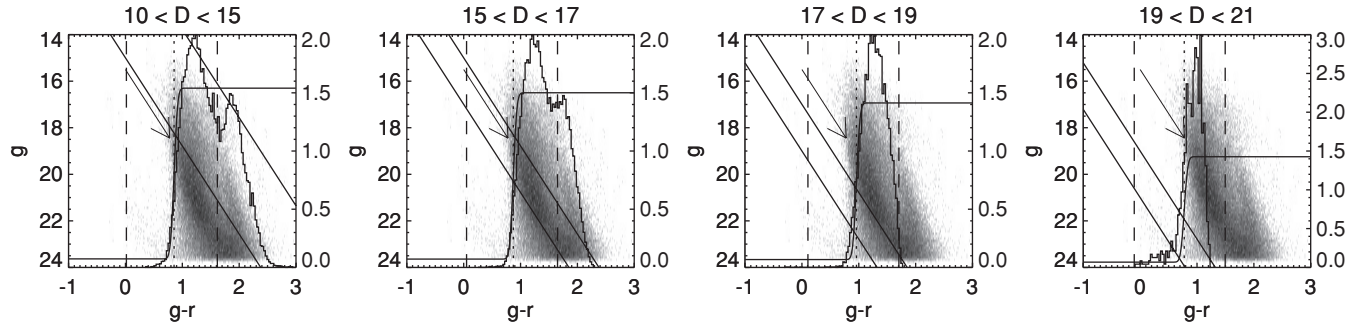


Figure 5. Example fits for the blue tip of the stellar locus for different magnitude ranges D at $l = 150^\circ$ and $b = 10^\circ$. The blue tip shifts redward as the range of D probed goes fainter, until we run out of stars. Additionally, intrinsically red foreground stars increasingly contaminate the blue tip as we go fainter in dusty regions.

between the diagonal lines in the $g - r$ panel. Solid curves give the probability distribution function (pdf) P for the maximum likelihood location of the blue tip color x_0 , and the number of stars as a function of color satisfying $10 < D < 19$. The blue tip color x_0 is given by the dotted line. In order that P can be normalized, the fit is performed only on stars in a finite range of colors. We first make a rough estimate of the blue tip color by using a very broad range of colors, and then perform the fit a second time using only stars within 0.8 (0.4) mag of the estimated blue tip in $u - g$ and $g - r$ ($r - i$ and $i - z$). This color range is given by the dashed lines.

The statistical uncertainty of the fit depends on the number of stars included in the fit, and so on the local stellar density, the sky area, and range of D used. At high latitudes, binning together 10 SDSS fields, for stars with $10 \text{ mag} < D < 19 \text{ mag}$, typical statistical uncertainties are 20, 15, 6, and 6 mmag for $u - g$, $g - r$, $r - i$, and $i - z$, respectively. Finding the standard deviations of measurements taken near the north Galactic pole, where the expected reddening is smooth and small, we find uncertainties of 24, 17, 10, and 12 mmag, similar to the fit results.

The presence of dust reddens stars, pushing the blue edge redward (Figure 4). In low-extinction regions where all of the dust is closer than about 1 kpc, the observed blue tip is uniformly shifted. It is this shift that we track in our measurements. In high-extinction regions or regions with dust beyond about 1 kpc, we can in principle learn about the change in dust column with distance by varying D , though we have not done so in this work (see Section 3.2).

The functional form $P(x, x_0)$ chosen to fit the blue edge of the distribution is usually a close fit only near the blue edge itself, and is rather bad over most of the color range. However, experiments with other functional forms and attempts to adaptively shrink the range over which the fit is performed to a narrow region around the edge tend to render the fit less robust. Moreover, because P is approximately constant away from the

edge, the fit results are robust to outliers far from the edge. Alternative functional forms systematically shift the location of the edge around slightly (mmag), but not in a way that correlates with the dust.

The blue tip fit can occasionally fail to find the blue tip of the stellar locus when too few stars are used. In such cases, it might identify a single blue star or quasar as the blue tip, or latch on to the M-dwarf peak in color-magnitude diagrams. In the maps we present, with $10 < D < 19$ and using 10 SDSS fields worth of stars for each blue tip fit, fewer than 1% of measurements are affected.

3.2. Changing Extinction with Distance

In this work, we treat all MSTO stars observed by the SDSS with $10 < D < 19$ as behind all of the dust. In principle, however, by comparing the color of the blue tip for nearby stars and distant stars, distant clouds of dust could be detected. Such clouds certainly exist, as dust has been detected in the halos of other galaxies and in H I clouds outside the disk in our Galaxy (Ménard et al. 2010; Wakker et al. 1996). However, comparing blue tip maps made for nearby ranges of D and distant ranges of D reveals no readily identifiable structures larger than the noise in the halo. We note that if such structures vary slowly spatially, they will be difficult to distinguish from variation in blue tip colors due to changing stellar populations. We defer to later work the attempt to identify such clouds.

On most sight lines the great majority of the dust column comes from the Galactic disk and is associated with the H I disk, which has a scale height of about 150 pc (Kalberla & Kerp 2009). Accordingly, as the brightest unsaturated MSTO stars are approximately a kiloparsec away, at high Galactic latitudes even the nearest MSTO stars observed by the SDSS are behind this dust.

At low Galactic latitudes, extinction increases rapidly and the color of the blue tip of the stellar locus becomes dramatically

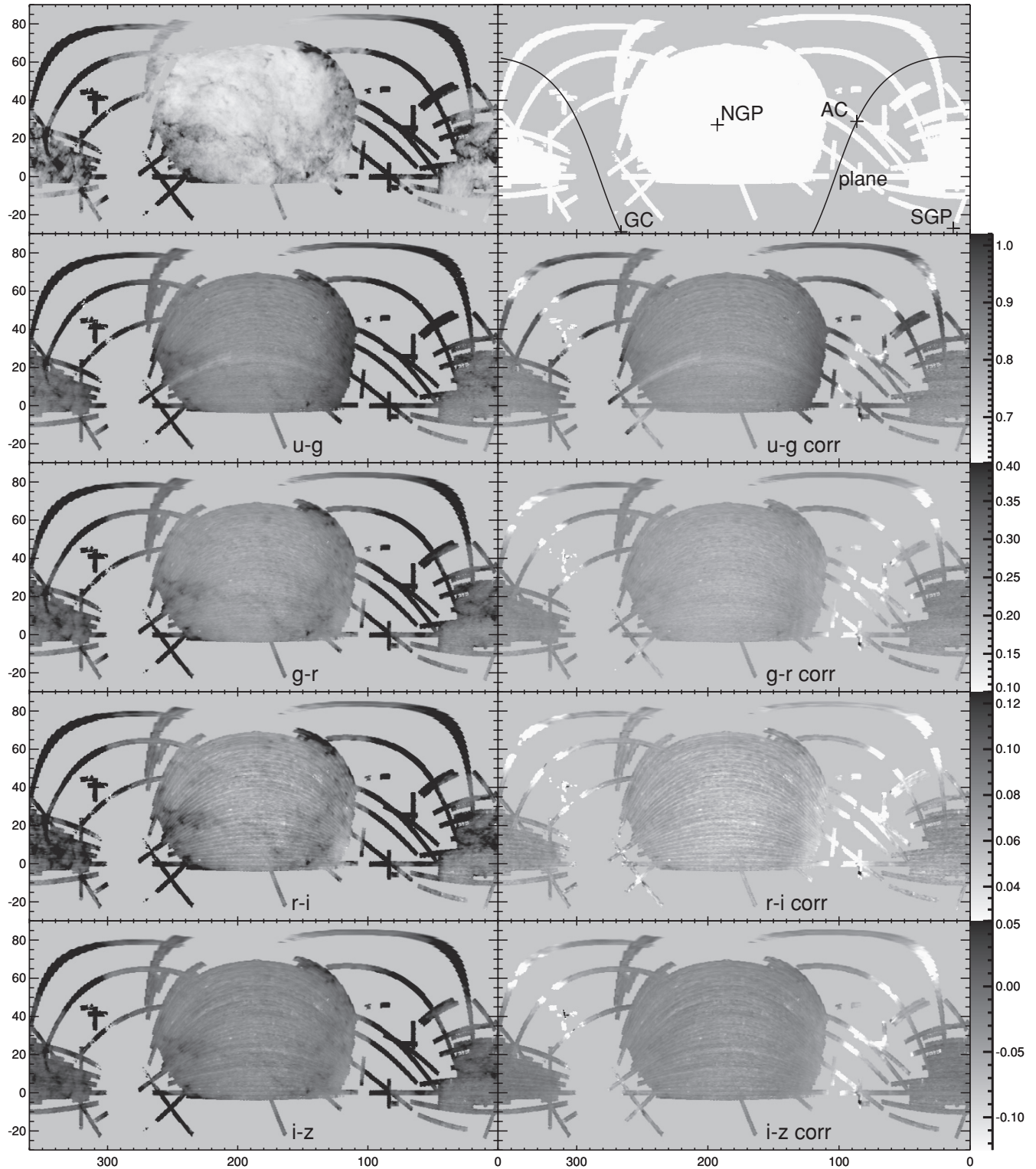


Figure 6. Blue tip colors over the SDSS footprint, for each SDSS color. The left-hand panels give the observed blue tip color, while the right-hand panels give blue tip colors after correction for dust extinction according to SFD and the coefficients $(A_u - A_b)/(\text{SFDE}(B - V))$ presented in this paper. The upper row of panels gives SFD and the locations of important points in the sky.

redder as fainter magnitudes are probed (Figure 5). In these dusty regions, reddened blue tip stars may be redder than intrinsically red foreground stars. Moreover, blue tip stars in these regions are spread out along the reddening vector, making it hard to isolate stars of a given reddening and distance using D . We attempt to identify and exclude such regions when analyzing blue tip maps.

3.3. Blue Tip Maps

We measure the blue tip color over the entire SDSS footprint, in each color, and for a variety of ranges of D (Figure 6). Here we present maps using blue tip fits to stars in a broad range of magnitudes: $10 \text{ mag} < D < 19 \text{ mag}$, using fits to the stars in 10 adjacent SDSS fields.

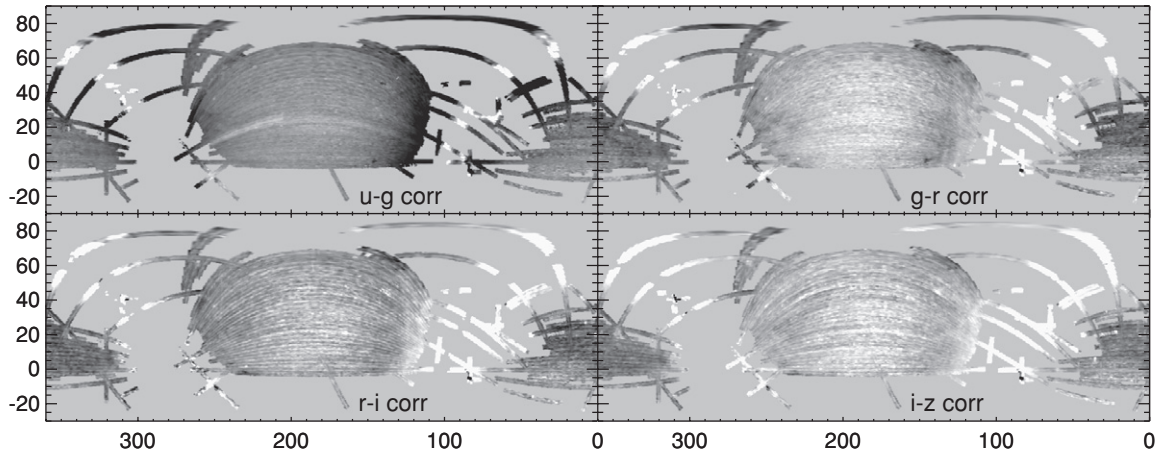


Figure 7. Stretched version of Figure 6, highlighting residuals. The Monoceros stream is prominent at the right-hand side of the NGP region of the footprint. White to black spans 0.225, 0.11, 0.05, and 0.06 mag.

The maps show unmistakable signatures of dust (dark clouds in the left panels of Figure 6) that are almost entirely removed when stellar colors are corrected according to the SFD map. The residuals at high Galactic latitude after extinction correction are dominated by problems with the survey calibration—striping in the SDSS scan direction and a few runs with bad zero points in $u - g$ (Figure 7). There is also a slowly varying residual in which blue tip color becomes redder near the Galactic plane, until deep in the Galactic plane when the color shifts very blue.

The former effect is caused by the various stellar populations sampled in different parts of the sky. In the plane, the higher metallicity, redder disk population becomes increasingly dominant over the halo population. The latter effect is a result of the violation of the assumption that all of the stars are behind all of the dust. Stars in front of the dust are dereddened with the full SFD dust column, and are therefore rendered extremely blue. These stars are then seen by the blue tip algorithm as the signature of the blue tip, resulting in a spuriously blue color. Even in less dusty regions where at least some MSTO stars are behind all of the dust, the method can fail if an insufficiently faint range of D is used. In this case, MSTO stars behind different amounts of dust are grouped together in finding the best fit, blurring the blue edge of the stellar locus. Because σ_P for the fit is fixed, this will result in a bluer than average blue tip color, while SFD would track the color of the MSTO stars behind all of the dust—the reddest stars in the group. These effects, however, are only noticeable in the dustiest region of the sky, where $|b| \lesssim 15^\circ$.

The Monoceros stream is clearly visible as a feature at $(\alpha, \delta) = (110^\circ, -10^\circ) - (110^\circ, 60^\circ)$ in the blue tip maps, because its MSTO is bluer than that of the thick and thin disks (Newberg et al. 2002), except in $u - g$.

There are two types of survey-systematic induced residuals in the maps, both of which are seen as striping along the SDSS scan direction. The less important are the few, large, $\sim 3^\circ$ wide stripes that are most noticeable on the eastern edge of the $u - g$ blue tip maps. These regions correspond to the footprints of SDSS runs that have slight zero point offsets from the rest of the survey. The more troubling residual is the universal small-scale striping along the scan direction. This corresponds to the 13 arcmin scale of the SDSS camera columns. We have not fully examined this residual, but attribute it to different filter responses

between the six SDSS camera columns (Doi et al. 2010). The SDSS ubercalibration algorithm ties stars of some mean color together, but does not account for color terms between the SDSS camera columns (Padmanabhan et al. 2008). As the MSTO stars are substantially more blue than the typical SDSS star, they are particularly vulnerable to color terms. Complicating this explanation of the camera column striping is the observation that the best-fit camera column offsets derived in Section 4.2 are different for the brightest range of D used than for fainter ranges of D , which are mutually compatible. We interpret this as a saturation or nonlinearity effect that depends on camera column, though we remove any stars flagged as saturated from the analysis. These systematics need to be addressed in fits to maps of the blue tip.

4. FITTING THE BLUE TIP MAP

The sensitivity of the blue tip colors to dust reddening makes for a natural test of the SFD map. We carry out the simplest tests of SFD permitted by the blue tip maps here, checking the dust map normalization and the $R_V = 3.1$ reddening law assumed by SFD for extrapolating reddening to colors other than $B - V$. The reddening law used in SFD is from O'Donnell (1994), which is similar to the Cardelli et al. (1989, hereafter CCM) reddening law.

The SFD dust map is often used as a map of reddening $E(B - V)$, but is based fundamentally on thermal emission from dust. In SFD, the thermal emission is converted to reddening based on a single dust map normalization constant. This constant was derived by comparing the observed reddenings $E(B - V)$ of a sample of elliptical galaxies to the SFD temperature-corrected emission from dust at their locations (Faber et al. 1989).

We repeat this test, using the colors of the blue tip of the stellar locus in place of the $B - V$ color of galaxies. Because of the five band photometry provided by the SDSS, we are able to extend the SFD test by additionally checking the assumed O'Donnell $R_V = 3.1$ reddening law. Because of the number and accuracy of the blue tip color measurements, we are able to further look for spatial variation in the SFD normalization constant and the reddening law. The method is ultimately the same as in SFD, however, we find the best-fit normalization constants that convert from dust emission (or $E(B - V)_{\text{SFD}}$, as these are proportional) to reddening. We extend this test to multiple colors and check for variation over the sky.

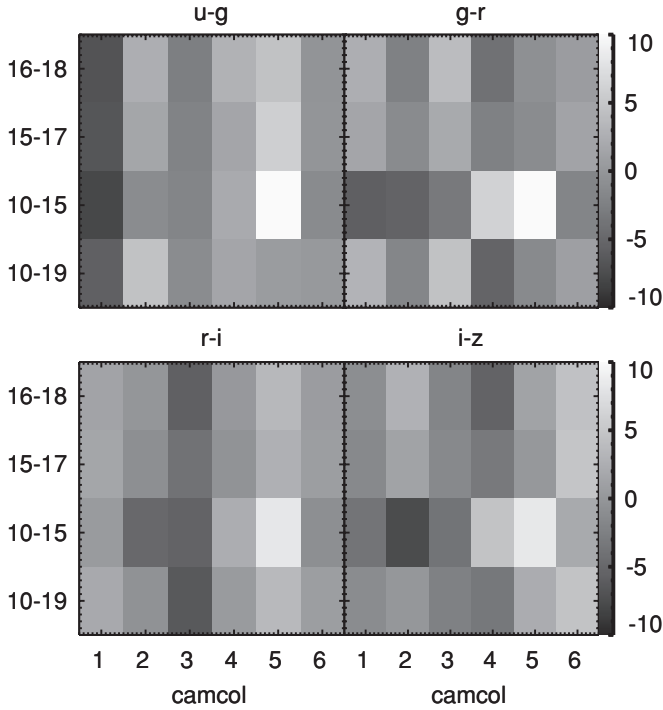


Figure 8. Camera column offsets used to destripe the SDSS blue tip maps, derived from the global blue tip map fits (Section 4.2). The left-hand axis labels give the range of D to which the offsets apply. The right-hand labels give the value of the gray scale in mmag. The offsets are compatible for different ranges of D , except at the brightest magnitudes ($10 < D < 15$), where nonlinearity effects may be coming into play.

To perform this test each blue tip map would be fit, ideally, as

$$(m_a - m_b)_{\text{bluetip}} = R_{a-b} E(B - V)_{\text{SFD}} + C, \quad (3)$$

over a part of the sky, where $(m_a - m_b)_{\text{bluetip}}$ is the blue tip map for the color $a - b$, R_{a-b} is the normalization constant to be measured, and C is the intrinsic blue tip color. However, because the blue tip of the stellar locus is not a universal color standard, but rather varies with position in a way likely substantially covariant with the dust map, this fit is impractical. Moreover, the survey striping artifacts discussed in Section 3.3 could further throw off the fit. To account for these two effects, we instead fit

$$(m_a - m_b)_{\text{bluetip}} = R_{a-b} E(B - V)_{\text{SFD}} + Q_r(f) + C_i, \quad (4)$$

where $Q_r(f)$ is a quadratic for run r in SDSS field number f and C_i is the camera column offset for camera column i . We fix C_1 to be zero to remove the degeneracy with the constant term in $Q_r(f)$. The quadratic $Q_r(f)$ simultaneously accounts for zero point errors in the SDSS calibration and slow intrinsic variation in blue tip color.

Because we bin 10 SDSS fields together for each blue tip measurement, variations in the dust map on scales much smaller than $1^\circ.5$ in the scan direction will not be captured in the blue tip measurements. The blue tip method is not a linear operator on the underlying stellar colors, so the measured color of the blue tip is not linearly related to the mean of $E(B - V)_{\text{SFD}}$ in the fields. In this work, for each set of fields contributing to a blue tip measurement, we use the median $E(B - V)_{\text{SFD}}$ in those fields as proportional to the expected reddening of that measurement. This is not strictly correct, but insofar as the dust does not vary too quickly, this filtering seems to approximate the correct behavior.

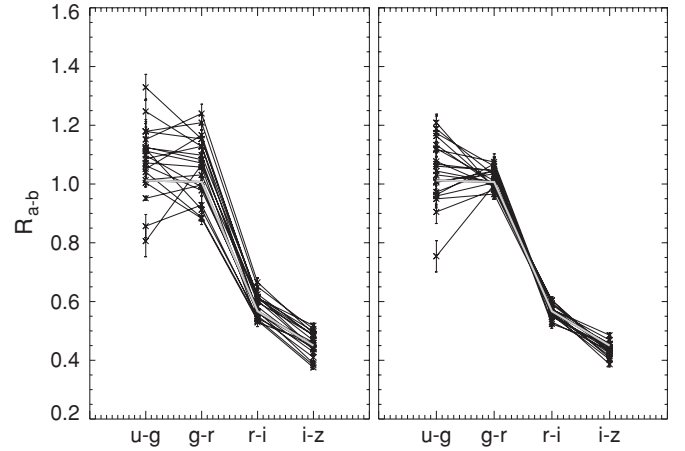


Figure 9. R_{a-b} for the four SDSS colors, for a selection of individually well constrained SDSS runs. The reddening spectrum has a similar shape among the different runs, but there is substantial scatter in the overall normalization (left). After forcing the mean of R_{g-r} , R_{r-i} , and R_{i-z} to match for each run, there is close agreement among the various dust extinction spectra (right). Error bars account only for the formal statistical uncertainties. The thick gray line in each plot gives the global best-fit R_{a-b} derived in this work.

After finding the best-fit R_{a-b} in each color, we repeat the blue tip measurements on the SDSS stars, this time with individual stellar colors corrected according to the derived fit parameters R_{a-b} , at the full resolution of the dust map. This process converges in a few iterations. The iteration renders the final fits insensitive to the details of the dust map filtering. We have verified the insensitivity to the filtering by noting that fits to the unbinned blue tip maps using an unfiltered SFD map give fit coefficients that are compatible with the fits to the binned blue tip maps.

We model the striping in camera columns by constant terms in the fit for each camera column. Empirically this correction is satisfactory, but we note that if our interpretation of the camera column offsets as derived from color terms is correct, the response of each camera column to dust is slightly biased. However, we detect camera column offsets of ~ 5 mmag over differences in stellar colors of a few tenths of magnitudes, implying that this bias is less than 1% (Figure 8). Furthermore, the bias will be different in each camera column and it must be, on average, zero. We have further confirmed that our results are unaffected by the color terms by separately fitting the dust map to each SDSS camera column individually, obtaining fits consistent with the global six camera column fit (Section 4.3).

4.1. Fits to Individual SDSS Runs

In some cases, a single run is long enough and dusty enough to individually constrain the dust reddening coefficients R_{a-b} in each color at the 10% level, even when fitting for camera column offsets and a quadratic. The fits show substantial variation in R_{a-b} (Figure 9). Most of this variation takes the form of an overall difference in dust absorption normalization, rather than as variation in the shape of the dust reddening spectrum. Some low, outlying values of R_{u-g} suggest that the run is so extinguished that substantial numbers of stars are not detected in the u band, ruining the fit. The fits remove nearly any trace of dust in these runs (Figure 10).

Fits to the runs individually well constrained by the dust map indicate significant variation in normalization ($\sim 20\%$) as well as, to a lesser extent, variation in dust extinction spectrum. Accordingly, in finding a global fit to the dust properties, we

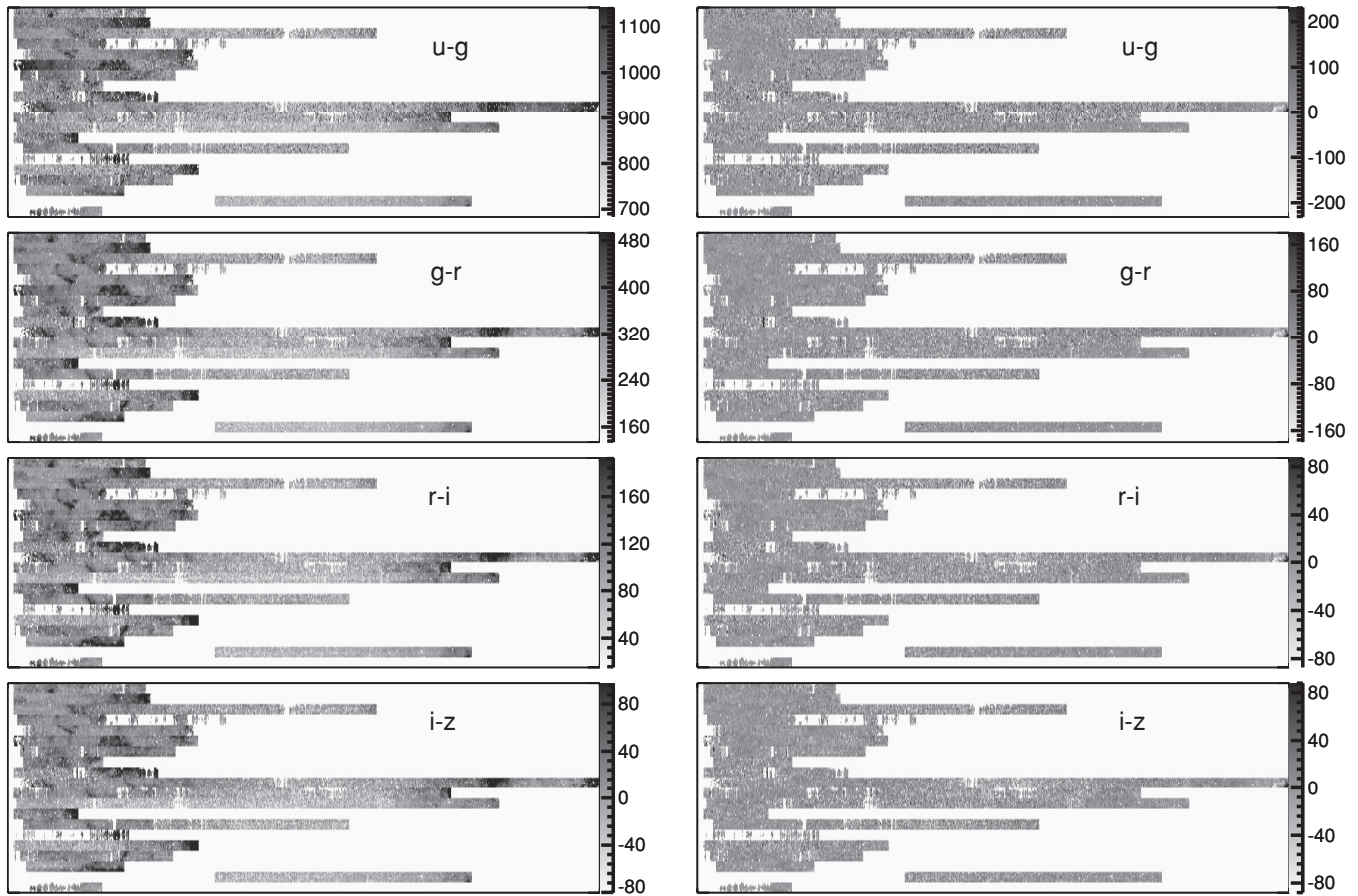


Figure 10. Blue tip colors (left) and residuals (right) for the runs in Figure 9, in mmag. Coherent signals from the dust are manifest (left). After fitting according to Section 4, the residuals show little structure (right). Each row of these plots corresponds to a specific SDSS run and camcol, for 20 example runs. The columns correspond to the fields in that run. Fields with bad seeing or deemed unphotometric have been omitted, resulting in some patchy areas. SDSS runs may be of different lengths, as seen in the plots.

remove from the fit regions that we deem discrepant from the “average” dust properties. To do this, first we individually fit each SDSS run. Runs with best-fit R_{a-b} more than 5σ from the inverse variance weighted average of R_{a-b} for all the SDSS runs are excluded from the global fit. Additionally, the global fit is iterated and σ -clipped field-by-field at 5σ .

4.2. Global Fit to All SDSS Runs

We find the best-fit (least-squares sense) combination of the SFD dust map, constant offsets for each camera column other than the first, and quadratics in field number for each run to the blue tip map via singular value decomposition. We do not fit for the offset for the first camera column because changing the offsets for all of the camera columns is degenerate with changing the constant offsets in the quadratics for each run. Specifically, we find the parameter $\mathbf{x}$ satisfying

$$\mathbf{A}^T \mathbf{C}^{-1} \mathbf{A} \mathbf{x} = \mathbf{A}^T \mathbf{C}^{-1} \mathbf{b} \quad (5)$$

which provides the least-squares solution to $\mathbf{A} \mathbf{x} = \mathbf{b}$. Here, $\mathbf{C}$ is a diagonal covariance matrix, with the variances determined by the formal statistical uncertainties in the blue tip fit to each field (or binned fields). The blue tip color for each field (or binned fields) is in $\mathbf{b}$. The design matrix $\mathbf{A}$ has dimensions $n_{\text{field}} \times n_{\text{param}}$. It contains one column for the SFD dust map values in each field, five columns for the offsets for the SDSS camera columns two through six, and three columns for each of

the 792 runs composing the SDSS-III, for the three terms in the quadratics for each run.

The SDSS-III contains imaging data on 1,147,506 fields. We require that the SDSS score⁸ of each run be greater than 0.5 and the point-spread function (PSF) full width at half-maximum (FWHM) be less than 1.8 arcsec in r , which reduces the number of fields to 686,554. Excluded runs typically are unphotometric, have bad seeing, or are Apache Wheel calibration runs. The blue tip method is run on all of the remaining fields, or binned sets of these fields. It occasionally fails, due to an insufficient number of stars or apparent detection of the blue tip blueward of -0.75 mag or redward of 2.4, 2.4, 1.8, and 1.6 mag in $u - g$, $g - r$, $r - i$, and $i - z$, respectively. The number of binned fields that successfully make it through the blue tip fit depends on the range of D used and the color, but in the ranges of D examined here it ranges from 684,000 to 677,000. Unbinned fields fail for lack of stars at high Galactic latitudes, and so fewer fields are successful: in ranges of D of interest, between 683,000 and 620,000 fields pass. The median number of stars contributing to the fits in each unbinned field at $10 < D < 19$ is 100. About 10^8 stars enter into the fits.

The global fit produces the coefficients R_{a-b} in Table 1 and at high latitudes leaves few noticeable coherent residuals

⁸ The SDSS score of a field reflects sensitivity to point sources and is derived from sky brightness and seeing. It further is capped at 0.5 for fields deemed unphotometric or runs fields using binned pixels (i.e., Apache Wheel fields).

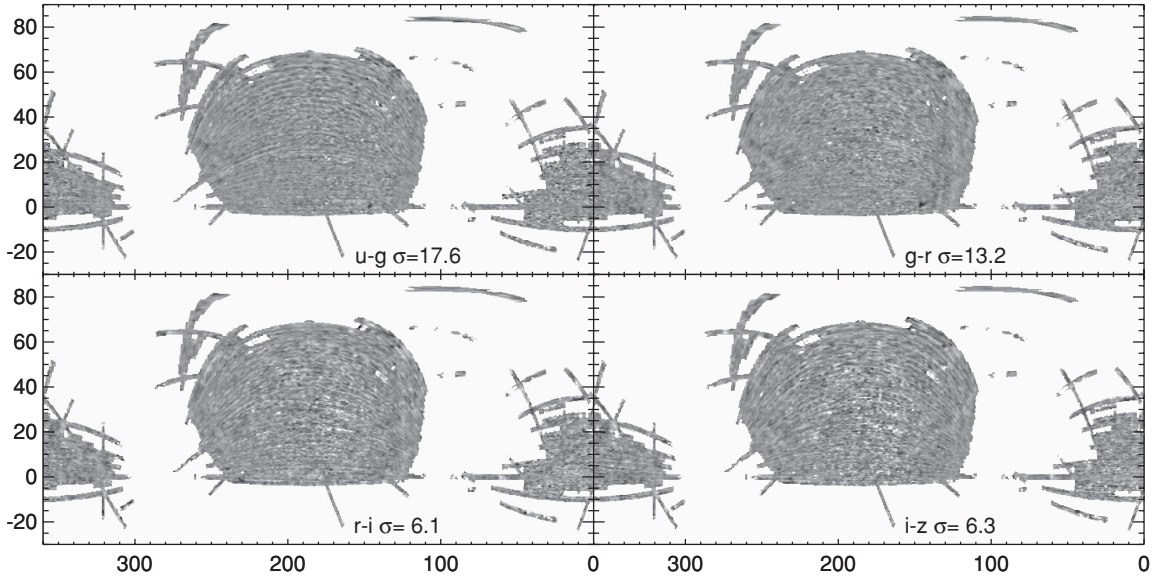


Figure 11. Blue tip color residuals after removing best-fit linear combination of dust map and polynomials, as described in Section 4.2. White corresponds to $+3\sigma$, while black corresponds to -3σ .

Table 1
 R_{a-b} for the SDSS Colors

SDSS Color	SFD	$R_V = 3.1$ O'Donnell	Blue Tip
$u - g$	1.362	1.138	1.01 ± 0.10
$g - r$	1.042	1.141	1.01 ± 0.08
$r - i$	0.665	0.616	0.57 ± 0.05
$i - z$	0.607	0.624	0.45 ± 0.05

Notes. R_{a-b} according to the original SFD prescription, an $R_V = 3.1$ O'Donnell prescription with updated SDSS filter definitions, and the best blue tip global fit coefficients. The formal statistical error bars are negligible; those presented here are based on the empirical field-to-field variation in best-fit extinction law as discussed in Section 5. This gives highly covariant uncertainties because the field-to-field variations are dominated by changes in best-fit dust map normalization (see the covariance matrix in Table 3).

(Figure 11). Nevertheless, a few dust clouds are clearly imperfectly subtracted. Most prominently, in the north, a few under-subtracted clouds in $g - r$ stand out on the eastern side of the north Galactic cap (NGC). Undersubtracted clouds in the northwest and at $(\alpha, \delta) = (145^\circ, 0^\circ)$ cause the runs including them to be excluded from the fit. The former feature is the largest residual in the Peek & Graves (2010) maps. Subtraction in the south is remarkably clean, though at right ascensions and declinations of $(340^\circ, 20^\circ)$ and $(60^\circ, 0^\circ)$ there are slightly oversubtracted clouds. A cloud at $(45^\circ, 20^\circ)$ barely makes it into the SDSS footprint, and is badly oversubtracted, causing the exclusion of its run from the global fit. In $g - r$ especially, a residual associated with the Monoceros stream stands out at the western edge of the NGC. We have tried masking this region and repeating the fit, but as the Monoceros stream is not correlated with the dust, the fit results were unchanged.

The blue tip color residuals as a function of $E(B - V)_{\text{SFD}}$ are generally flat (Figure 12). In $r - i$ and $i - z$, any trend with $E(B - V)$ is at less than the 2% level. In $u - g$ there is no discernible trend, though the scatter is large. In $g - r$ there seem to be disturbing 5%–10% trends with $E(B - V)$ but they may stabilize around $E(B - V) = 0.4$ mag, with reddenings off by only 15 mmag there.

The blue tip maps have residuals with distributions given in Figure 13. The core of the distribution is Gaussian, but the

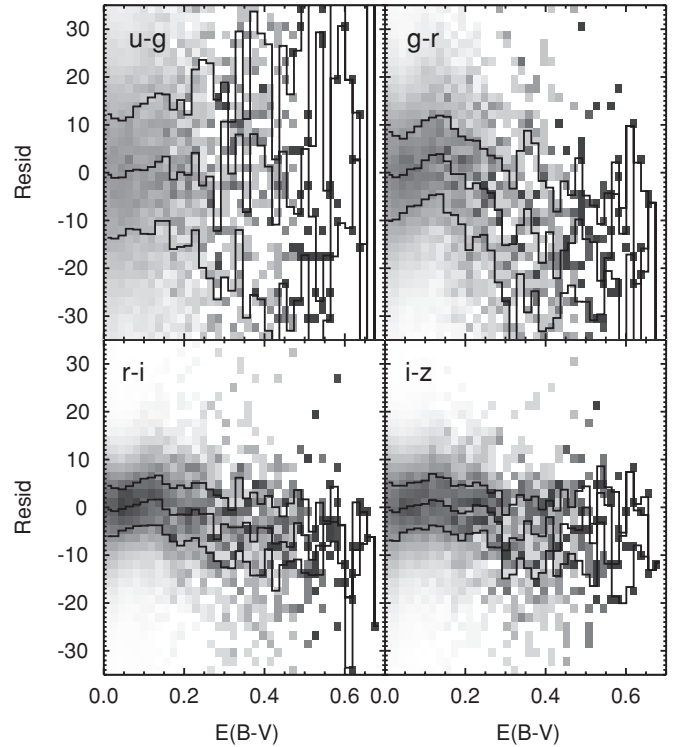


Figure 12. Blue tip color residuals with $E(B - V)_{\text{SFD}}$. The residuals in $u - g$, $r - i$, and $i - z$ reassuringly show no trend with $E(B - V)$. In $g - r$, the residuals have some structure, but the positive slope at $E(B - V) < 0.2$ and the negative one around $0.2 < E(B - V) < 0.4$ are only 5% effects—the residuals are largely uncorrelated with $E(B - V)$.

wings are non-Gaussian, falling off more slowly than would be expected. The blue tip method gives median estimated uncertainties as 17.5, 12.5, 5.7, and 5.8 mmag, closely reproducing the Gaussian fits to the residual distribution, which give 18.1, 12.3, 6.9, and 7.8 mmag in $u - g$, $g - r$, $r - i$, and $i - z$, respectively.

The polynomial terms from the global fit are intended to model the slow, intrinsic variation in the blue tip color and per-run calibration offsets, and so are of independent interest

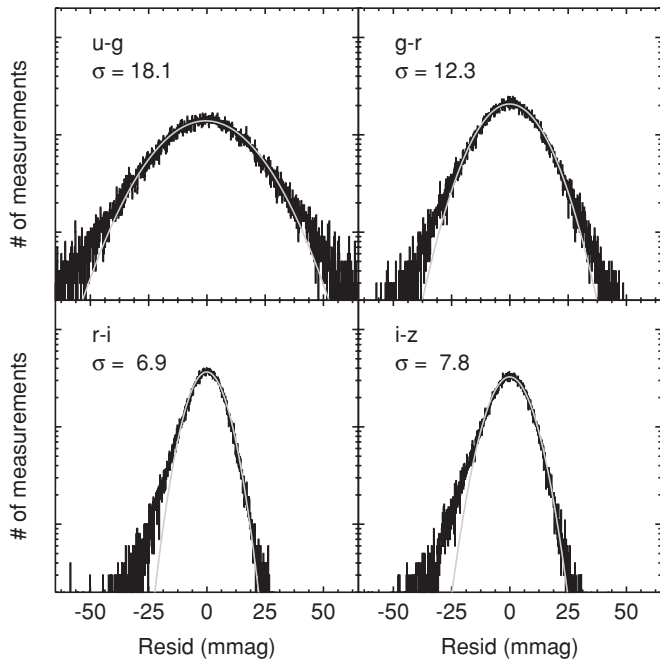


Figure 13. Fit residuals, in mmag. The core of the distribution is well fit by a Gaussian, but the wings fall off more slowly than in a Gaussian. The colors $r - i$ and $i - z$ have the tightest distributions, likely because the blue tip is less dependent on metallicity in these colors.

(Figure 14). These maps are clearly heavily striped. Some of this striping is clearly removing calibration problems with the SDSS, as in the eastern side of the NGC in $u - g$. The striping at high latitudes in the north in other colors is probably substantially an artifact of the low signal in these regions, but the typical stripe-to-stripe difference there is only ~ 5 mmag, and at worst 10 mmag.

The SDSS imaging contains a number of runs crossing the Galactic plane, as part of SEGUE (Yanny et al. 2009). All of these runs and a few other low Galactic latitude runs get identified as discrepant by the fitting algorithm and discarded from the final fit. In a run-by-run treatment, this is inevitable, as at very high extinction the blue tip method will fail because the stars are not behind all the dust. However, for $|b| > 10^\circ$, inspection of the blue tip residual maps suggests that the SEGUE runs could be well fit also, although we have not tried that here. The signal from the dust in the SEGUE runs is sufficiently

rich to merit treatment separate from the bulk of the high Galactic latitude sky, as is done in M. J. Berry et al. (2011, in preparation).

4.3. Fits to Different Sky Regions

Given the presence of dust-correlated residuals in different parts of the sky, one wonders whether the fit is actually “global” in a useful sense, or is primarily a product of the footprint we have decided to look at. Accordingly, we have cut the sky into a number of subregions and separately found the best-fit R_{a-b} in each. To test for large-scale variations in R_{a-b} , we divide the sky into northern ($b > 25^\circ$) and southern ($b < -25^\circ$) Galactic regions, as well as octants of the sky divided by lines of constant Galactic longitude (Figure 15). To try to test variation in dust properties as a function of extinction or temperature, we divide the sky into regions of dust of different extinctions and temperatures. Finally, to verify that we have satisfactorily accounted for the camera column offsets, we divide the SDSS survey into its six camera columns.

We restrict to the main global fit region and apply the globally derived camera column offsets to the blue tip colors. We remove best-fit polynomials from the filtered SFD dust map and from the blue tip colors, as in Section 4, using the global fit region. We then find the best fit of the filtered, polynomial-subtracted dust map to the polynomial-subtracted blue tip map, restricted to various subsets of the full region.

The results are encouragingly consistent, given that we have already seen that dust reddening normalization can vary substantially, along with, to a lesser extent, its spectrum (Figure 9). We find the dust extinction normalization and spectrum to be consistent at the 10% level. The north/south normalization discrepancy is the most surprising, with the north preferring a normalization about 15% larger. We also find that dust with $0.6 \text{ mag} < E(B - V) < 1.0 \text{ mag}$ prefers a $\sim 15\%$ smaller normalization than dust with $0 \text{ mag} < E(B - V) < 0.05 \text{ mag}$. Dust at different temperatures likewise has similar extinction normalizations and spectra.

4.4. Fits to a Mock Star Catalog

The reliability of the fitting procedure can be tested by running the fit on a star catalog from a mock galaxy model. The mock catalog was generated with the *galfast* catalog generation code (M. Jurić 2011, in preparation). Given a model of stellar number

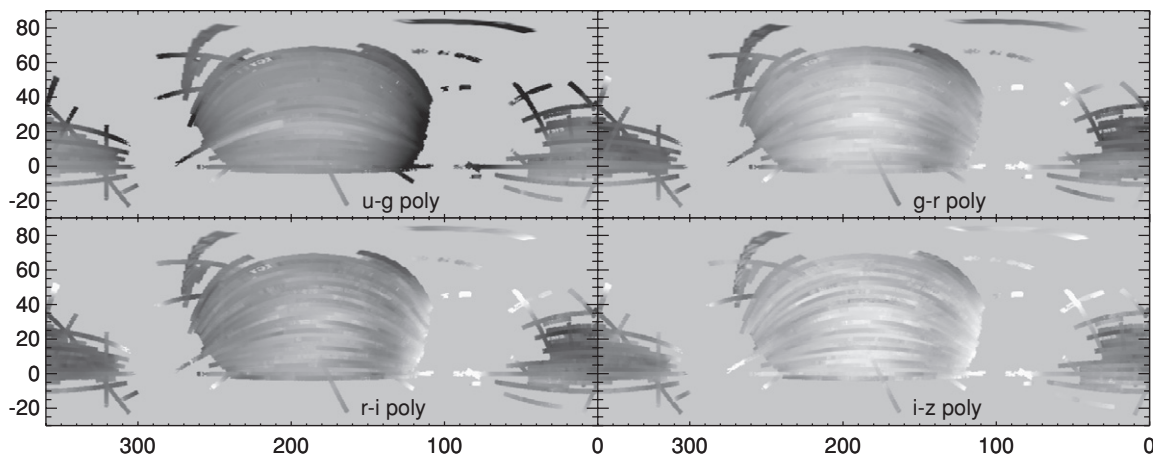


Figure 14. Map of the polynomial terms from the global fits. The scale is the same as in Figure 7. These maps model the intrinsic variation of the blue tip color on the sky as well as per-run SDSS calibration offsets.

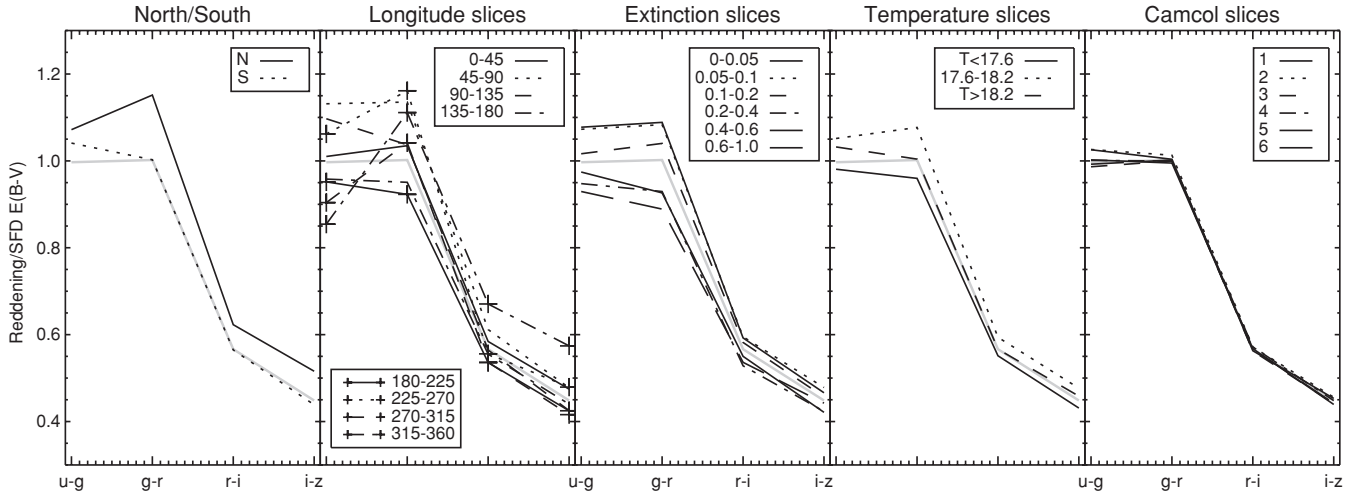


Figure 15. R_{a-b} for the SDSS colors over different subsets of the SDSS footprint. The first panel gives the coefficients for the north ($b > 25^\circ$) and south ($b < -25^\circ$). The next panel gives the best-fit coefficients for eight slices in Galactic longitude. The third panel gives coefficients in regions of sky with increasing extinction. The fourth panel divides the sky into regions of three different temperatures, and the fifth panel divides the survey by SDSS camera column. The thick gray line in each panel gives the global best-fit R_{a-b} derived in this work.

density, metallicity, a three-dimensional extinction map, the photometric system, and instrumental errors, *galfast* generates realistic mock photometric survey catalogs.

As inputs, we used the number density distribution parameters from Jurić et al. (2008) and the metallicity distribution from Ivezić et al. (2008). The three-dimensional dust distribution map was generated using the model of Amôres & Lépine (2005). The generated u , g , r , i , and z magnitudes were convolved with magnitude-dependent errors representative of SDSS, and the final catalog was flux limited at $r < 22.5$.

The three-dimensional dust map was modified from Amôres & Lépine (2005) to contain the small-scale clouds seen in SFD. This was performed by scaling each line of sight from the model by the ratio $E(B - V)_{\text{SFD}}/E(B - V)_{\text{model, 100 kpc}}$, so that the model matches SFD at 100 kpc. The resulting map contains the expected average three-dimensional distribution of the dust combined with the angular structures present in SFD.

We construct a mock galaxy using *galfast* and then construct catalogs of observations of these stars for each SDSS run. The resulting catalogs are processed by the blue tip analysis code in exactly the way that the actual SDSS catalogs are processed. As for the actual catalogs, the median number of stars per field is ~ 100 .

Blue tip fits performed on the mock galaxy recover the R_{a-b} used to within 3%. This verifies that we properly account for shifts in the blue tip color due to metallicity. However, for these tests we have assumed that SFD correctly predicts the line of sight column density and that the reddening law is the same everywhere on the sky, at least at high Galactic latitudes and in the optical. Insofar as the final fit residuals are largely flat (Figure 11), this assumption seems justified. Moreover, we can verify that the ratios of the R_{a-b} derived independently from SFD agree with the ratios of the R_{a-b} derived here.

4.5. Fitting Ratios of R_{a-b} without SFD

The preceding analysis has assumed that SFD is a good template for the dust. However, we can relax our dependence on SFD if we restrict our attention to ratios between different R_{a-b} .

In the absence of changing stellar populations and calibration errors, blue tip colors will fall along a single line given by the

Table 2
Blue Tip Color-Color Fit Results

Color Ratio	SFD	O'Donnell	Blue Tip	Color-Color
A_{u-g}/A_{g-r}	1.307	0.997	1.005	1.019 ± 0.025
A_{g-r}/A_{r-i}	1.567	1.852	1.776	1.728 ± 0.038
A_{r-i}/A_{i-z}	1.096	0.987	1.260	1.237 ± 0.042

Notes. The results are in close agreement with the global blue tip fits, while excluding the original SFD reddening law and an $R_V = 3.1$ O'Donnell reddening law. These fits do not use SFD as a template and so test the shape of the reddening law without reference to SFD.

reddening vector. By removing a quadratic in field number and accounting for camera column offsets as in Section 4.2, we remove variations in blue tip color not associated with reddening. By fitting a line to the resulting polynomial-subtracted blue tip color-color diagrams, we measure the ratio of the R_{a-b} . Some striping along the SDSS scan direction is evident in the blue tip residuals despite our attempts to remove it, and this striping will be deleterious to the fit results because we cannot rely on its being uncorrelated with the dust template we fit. Accordingly, we fit lines for each camera column, eliminating the effect of striping, and average the results (Figure 16).

These color-color fit results are in good agreement with the results of Section 4.2 (Table 2). The results agree to about 1σ with the SFD fit results, where the uncertainties σ are given by the standard deviations of the fit results between the camera columns. The original SFD prescription is seen to clearly overestimate R_{u-g}/R_{g-r} (see Section 5.1.3), while both the original SFD prescription and the updated $R_V = 3.1$ O'Donnell reddening law are found to underestimate R_{r-i}/R_{i-z} .

5. DISCUSSION

In this section, we use the blue tip fits presented above to constrain reddening laws and to test the SFD normalization and temperature correction. We then briefly point out a discrepancy in the color of the dereddened blue tip between the north and south, which is plausibly a consequence of a different stellar population in the north than in the south.

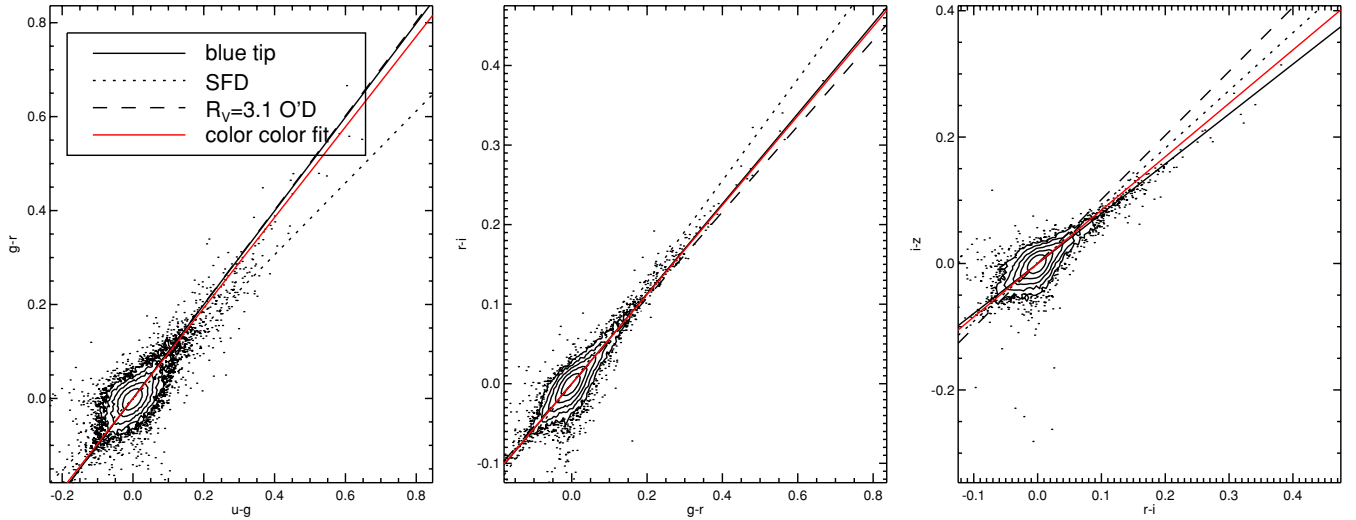


Figure 16. Plots of the colors of the blue tip in different colors, for camera column one. Spatially slowly varying terms have been removed, so points should fall along the line R_{a-b}/R_{c-d} . The reddening coefficients presented here best trace the distribution of points.

(A color version of this figure is available in the online journal.)

5.1. Constraining Reddening Laws

5.1.1. Connecting Reddening Laws to R_{a-b}

A reddening law gives the extinction $A(\lambda)$ over a range of wavelengths λ and so makes a prediction for the R_{a-b} that we have fit. The extinction in band b , in the limit that the variation in the extinction over that band is small, is given by $\Delta m_b = A(\lambda_{\text{eff},b,S})E(B-V)$, with

$$\lambda_{\text{eff},b,S} = \frac{\int d\lambda \lambda S(\lambda) W_b(\lambda)}{\int d\lambda S(\lambda) W_b(\lambda)}. \quad (6)$$

Here the system response for band b is given by $W_b(\lambda)$, $S(\lambda)$ is the source spectrum in photons $\text{s}^{-1} \text{\AA}^{-1}$, and $A(\lambda)$ is the reddening law, normalized to give $A(\lambda_{\text{eff},B,S}) - A(\lambda_{\text{eff},V,S}) = 1$. The reddening in the color $a-b$ is then given by $(A(\lambda_{\text{eff},a,S}) - A(\lambda_{\text{eff},b,S}))E(B-V)$, from which it follows that $R_{a-b} = (A(\lambda_{\text{eff},a,S}) - A(\lambda_{\text{eff},b,S}))E(B-V)/E(B-V)_{\text{SFD}}$. Here we have assumed that the variation in the extinction over the band pass is small; for $E(B-V) < 1$, this assumption changes the predicted R_{a-b} by less than 1% in $r-i$ and $i-z$, and less than 5% in $g-r$ and $u-g$.

Accordingly, we evaluate the extinctions in each SDSS pass band using the SDSS system throughputs and an MSTO source spectrum from a Kurucz model with $T_{\text{eff}} = 7000 \text{ K}$, for a variety of reddening laws (Gunn et al. 1998; Kurucz 1993). We examine in particular the CCM, O'Donnell, and Fitzpatrick (1999, F99) reddening laws, which are parameterized by $R_V = A_V/E(B-V)$. We find the best-fit factors R_V to our measured R_{a-b} for each of these reddening laws.

The other free parameter in these fits is the best-fit normalization $N' = E(B-V)/E(B-V)_{\text{SFD}}$. We do not report this parameter directly. The SFD dust map is based on a map of thermal emission from dust and is correspondingly proportional to $\tau_{100\mu\text{m}}$, the optical depth of dust at $100 \mu\text{m}$. Empirically, the ratio between $\tau_{100\mu\text{m}}$ and $E(B-V)$ is itself a function of R_V , and so N' is covariant with R_V . However, the ratio between $\tau_{1\mu\text{m}}$ and $\tau_{100\mu\text{m}}$ depends less on R_V , so we report $N = A_{1\mu\text{m,predicted}}/A_{1\mu\text{m,SFD}}$. Here, $A_{1\mu\text{m,predicted}}$ is the extinction at $1 \mu\text{m}$ implied by the best-fit reddening law and $A_{1\mu\text{m,SFD}}$

is the SFD-predicted extinction, extrapolated to $1 \mu\text{m}$ following the $R_V = 3.1$ O'Donnell reddening law assumed by SFD. The quantity $A_{1\mu\text{m,SFD}}$ is simply $1.32 \cdot E(B-V)_{\text{SFD}}$. We find that the F99 reddening law provides the best fit to the R_{a-b} we measure, so we additionally mention for reference that the F99 reddening law ratio $E(B-V)/A_{1\mu\text{m}}$ is 11% larger than the O'Donnell ratio $E(B-V)/A_{1\mu\text{m}}$, though this depends on the adopted R_V and source spectrum.

5.1.2. R_V and N for Individual Runs

We have found that the dust extinction spectrum normalization and shape vary over the sky (Figure 9). We can quantify this effect in terms of variation in N and R_V by fitting reddening laws to the runs that individually well constrain R_{a-b} (Section 4.1). We use the F99 reddening law here rather than the traditional CCM or O'Donnell reddening law because the latter two reddening laws (especially the O'Donnell reddening law) predict that $R_{r-i} \approx R_{i-z}$, which is a poor fit to the data. The derived N and R_V vary from run to run, especially as a $\sim 20\%$ scatter in normalization (Figure 17). Almost all of the runs are consistent with $2.8 < R_V < 3.2$. The distribution of R_V and N validates our use of $1 \mu\text{m}$ as a reference wavelength for N , as the two parameters appear uncorrelated.

5.1.3. R_V and N for the Global Fit

In order to compute best-fit reddening laws for the global fit R_{a-b} , we need to account for the covariance in the R_{a-b} over the sky in addition to the formal statistical uncertainties in the fit. These uncertainties are about a part in one thousand. However, the best-fit normalization can vary at the 10% level from field to field, and the part in a thousand uncertainty reflects averaging these fluctuations over many fields. While the dust extinction spectrum seems relatively constant, it would be surprising if the average reddening reflected the reddening of any particular dust cloud at the part in a thousand level, so another method for estimating the uncertainties is needed. The uncertainties reported in Table 1 are the standard deviations in R_{a-b} for eight octants in Galactic longitude, and do not account for the covariance of the measurements in the different colors owing to the changing best-fit normalization.

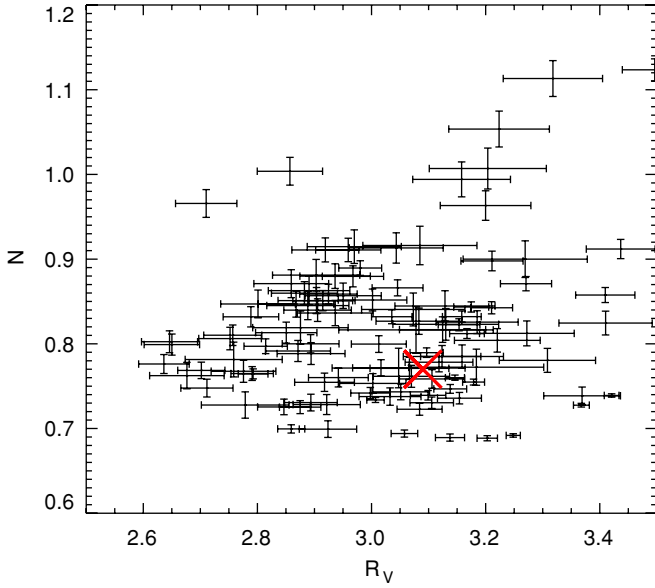


Figure 17. Best-fit R_V and dust map normalization N for SDSS runs that individually well constrain R_{a-b} , examples of which are in Figure 9. Dust map normalizations vary by as much as a factor of 2, though most are consistent at the 20% level. The large red “X” indicates the location of the best-fit R_V and normalization to the global fit R_{a-b} . Error bars account only for the formal statistical uncertainties.

(A color version of this figure is available in the online journal.)

The consequence of adopting uncertainties based on the field-to-field variation in the dust extinction spectrum is that the resulting uncertainties on N and R_V will describe the range of N and R_V among the clouds within the footprint we analyze. They do not give the uncertainties on the best-fit N and R_V within our sample, which are more tightly constrained. As mentioned, the formal statistical uncertainties are about one part in a thousand. Uncertainties estimated from using different ranges of D for selecting the stars give uncertainties of 2%, 2%, 1%, and 2% in R_{a-b} for the colors $u-g$, $g-r$, $r-i$, $i-z$, respectively.

The field-to-field variation in R_{a-b} can be estimated from the sample covariance matrix of best-fit R_{a-b} in different sky regions. We find the best-fit R_{a-b} at each point in the footprint. Because over most of the footprint the signal-to-noise ratio (S/N) in the filtered blue tip maps is too low to make a reliable determination of R_{a-b} , we include nearby pixels in the fit with weights given by a 7° smoothed Gaussian. The best-fit R_{a-b} is then given by

$$R_{a-b,n} = \frac{\sum_i D_i C_i^{-1} W_{i,n} b_i}{\sum_i D_i^2 C_i^{-1} W_{i,n}}, \quad (7)$$

where n is the pixel on the sky, i indexes over blue tip measurements, D gives the filtered dust map, b and C^{-1} give the blue tip measurement and its inverse variance, and $W_{i,n}$ is the weight matrix, corresponding to Gaussian smoothing with an FWHM of 7° .

The sample covariance matrix of the resulting maps of R_{a-b} is used as the covariance matrix for fits of reddening laws to R_{a-b} (Table 3). Only pixels with estimated uncertainty in R_{i-z} less than 0.01 are used for computing the sample covariance matrix, to avoid overestimating the intrinsic variance due to the uncertainty in the estimates. The largest eigenvalue of the covariance matrix (2.4×10^{-2}) is 94 times larger than the smallest eigenvalue (2.6×10^{-4}). The eigenvector with the

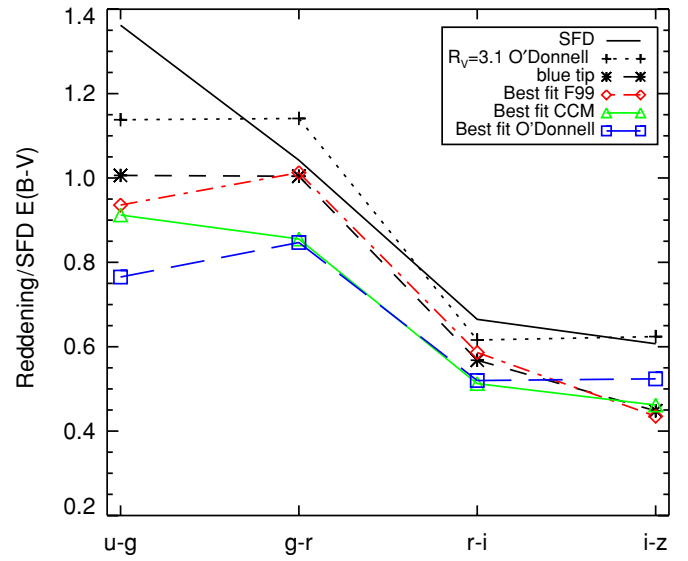


Figure 18. Original SFD reddening coefficients (solid line), updated coefficients according to the actual SDSS filters (crosses), and the best-fit global coefficients found in this work (stars). We fit our best-fit coefficients with reddening laws according to F99 (diamonds), CCM (triangles), and O'Donnell (squares). The F99 reddening law seems a good fit to each SDSS band (Section 5.1.3).

(A color version of this figure is available in the online journal.)

Table 3

Eigenvalues and Eigenvectors of the Reddening Covariance Matrix

$\sqrt{\lambda}$	v_{u-g}	v_{g-r}	v_{r-i}	v_{i-z}
0.155	0.88	1.21	0.45	0.36
0.079	1.23	-0.51	-0.41	-0.79
0.031	0.51	-0.91	0.61	1.05
0.016	-0.15	-0.15	1.35	-0.83

Notes. Eigenvalues λ and eigenvectors $\mathbf{v}$ for the sample covariance matrix. Eigenvectors are normalized so that $|\mathbf{v}| = |\mathbf{R}_{\text{globalfit}}|$, to facilitate comparison between R_{a-b} and the first, least well-constrained eigenvector, which is roughly parallel to R_{a-b} .

largest eigenvalue is roughly parallel to a vector corresponding to changing the normalization of the spectrum, and that with the smallest eigenvalue corresponds to changing the relative amount of reddening in $r-i$ to $i-z$. This quantitatively agrees with our claim that the normalization of the reddening law is poorly constrained relative to its shape.

With this covariance matrix, the best-fit reddening laws have $R_V = 3.9 \pm 0.4$, $N = 0.98 \pm 0.10$ for the O'Donnell reddening law, $R_V = 3.0 \pm 0.4$, $N = 0.75 \pm 0.10$ for the CCM reddening law, and $R_V = 3.1 \pm 0.2$, $N = 0.78 \pm 0.06$ for the F99 reddening law (Figure 18). The χ^2/dof of the O'Donnell, CCM, and F99 reddening laws are 7.8, 3.5, and 2.1, respectively. The O'Donnell and CCM reddening laws are disfavored because they predict smaller reddening differences between $r-i$ and $i-z$ relative to the data and the F99 reddening law. The F99 reddening law fits all of the points reasonably well.

The O'Donnell reddening law in particular and CCM reddening law to a lesser extent provide poor fits to the blue tip data, and the best-fit parameters are seriously driven by the poorly matching $r-i$ and $i-z$ data. Accordingly, the derived R_V and N for these reddening laws are unphysical.

All of the fits give R_{u-g} substantially less than the value given in SFD (Figure 18). The values given in the SFD appendix were based on preliminary estimates of the system response of the

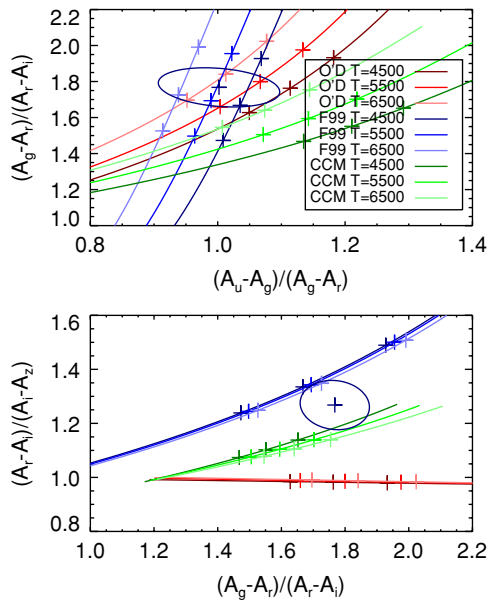


Figure 19. O'Donnell, CCM, and F99 reddening laws for different stars of different temperatures. $R_V = 2.6, 3.1$, and 3.6 are marked with crosses. R_V increases to the left. Ellipses are for the best-fit blue tip values, with uncertainties computed from the covariance matrix of Table 3.

(A color version of this figure is available in the online journal.)

SDSS, which varied somewhat from the actual system response. Using the SDSS system response from Gunn et al. (1998) for the $R_V = 3.1$ O'Donnell reddening law gives values different from those in SFD by 20% in $u - g$ and 10% in $g - r$ and $i - z$.

The predicted R_{a-b} depends somewhat on the source spectrum used (Figure 19). We illustrate the effect of changing the source spectrum by plotting the derived reddening laws for the O'Donnell, CCM, and F99 reddening laws for Kurucz models (Kurucz 1993) with $T = 6500, 5500$, and 4500 from the stellar spectra grid of Munari et al. (2005). The blue tip best-fit reddening law is relatively insensitive to T over this range.

The maps of R_{a-b} over the sky can be combined to make maps of R_V and reddening law normalization (Figure 20). We have combined the measured values with a prior of $R_V = 3.1 \pm 0.2$ and $N = 0.78 \pm 0.06$ to reduce the scatter in regions of low S/N.

One feature of the maps of R_V and N is that the two maps are substantially uncorrelated. This again confirms the expectation that the ratio of $\tau_{1\mu\text{m}}/\tau_{100\mu\text{m}}$ does not depend on R_V .

5.2. Comparison with SFD Normalization

We can directly compare our predicted $E(B - V)$ with $E(B - V)_{\text{SFD}}$ by using our best-fit reddening law and accounting for the difference in source spectrum between the galaxies that SFD analyzed and the MSTO stars we analyze. We get $E(B - V)_{\text{bluetip}} = 0.86 \cdot E(B - V)_{\text{SFD}}$, suggesting SFD overpredicts reddening by about 14%. The estimated normalization uncertainty in SFD was 4%, while we claim 8% uncertainty in our normalization. However, the estimated fractional uncertainty of SFD was 16%, and we are now in a position to attribute most of this uncertainty to varying best-fit normalization. Accordingly, it is unsurprising that the SFD normalization differs from ours by 14%, particularly given that the footprint we analyze is different from that used in SFD, and that we have found north/south normalization differences of about 15%.

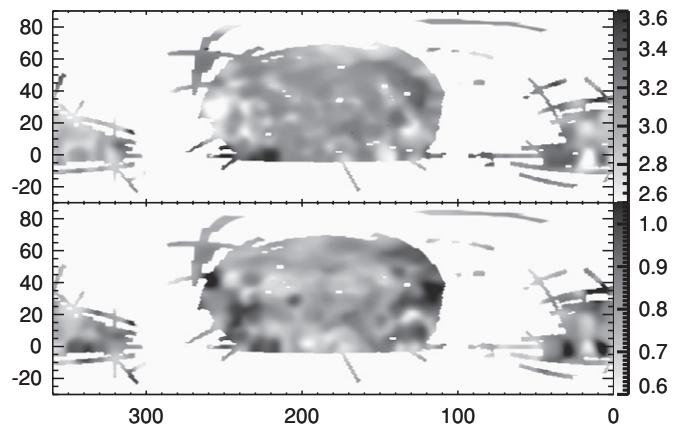


Figure 20. Maps of R_V (top) and dust map normalization (bottom) over the SDSS footprint. The map has been combined with a prior (Section 5.1.3) to reduce the scatter in regions of low S/N.

5.3. The SFD Temperature Correction

The final $E(B - V)_{\text{SFD}}$ takes the form $E(B - V)_{\text{SFD}} = p \mathbf{I}_{\text{corr}} \mathbf{X}$, where p represents a normalization coefficient, $\mathbf{I}_{\text{corr}}$ represents the destriped, zodiacal-light subtracted *IRAS* 100 μm flux and $\mathbf{X}$ represents a temperature correction factor. An error in determining the temperature correction factor will lead to dust with a different best-fit normalization, but with the same reddening spectrum, very much like what we see in the blue tip maps.

Accordingly, the blue tip fit residuals can plausibly be attributed to errors in the SFD temperature correction factor. In Section 4.3, we attempted to test the temperature correction by verifying that the best-fit dust normalization was consistent for regions of different temperature according to SFD. However, this procedure assumes that the SFD temperature correction adequately distinguishes hot and cold dust. At high latitudes, the S/N of the DIRBE 100 μm and especially the 240 μm map is too low to construct a 100 $\mu\text{m}/240 \mu\text{m}$ ratio map without substantial filtering. The SFD ratio map was constructed by first smoothing the 100 and 240 μm maps to 1° and then further weighting low S/N pixels to a high $|b|$ average ratio. Insofar as this procedure mixes dust of different temperatures together to a single reported SFD average temperature, it makes it difficult for us to test the SFD temperature correction using the SFD temperature map in this way.

One way to test the accuracy of the temperature correction at high $|b|$ is to compare the SFD temperature correction with the temperature correction used for the FIRAS dust fits (Finkbeiner et al. 1999). The SFD temperature correction is weighted to constants in the north and south in regions of low S/N, while the FIRAS temperature correction is weighted to a 7° smoothed map in these regions. In high S/N regions the two corrections agree. Letting $\mathbf{X}_{\text{SFD}}$ be the SFD temperature correction and $\mathbf{X}_{\text{FIRAS}}$ be the FIRAS temperature correction, we can plot blue tip color residuals versus the change in predicted dust column density from switching from the SFD to the FIRAS temperature correction: $\Delta = E(B - V)_{\text{SFD}}(\mathbf{X}_{\text{FIRAS}}/\mathbf{X}_{\text{SFD}} - 1)$ (Figure 21).

Were the FIRAS temperature correction a much better predictor of dust temperature than SFD, we would hope for a linear trend between dust correction and blue tip residual, with slope equal to the best-fit dust coefficients. Instead we find slopes of approximately half the best-fit coefficients, suggesting that the true temperature map is between the SFD and F99 temperature maps. The specific values of the coefficients of the linear fits

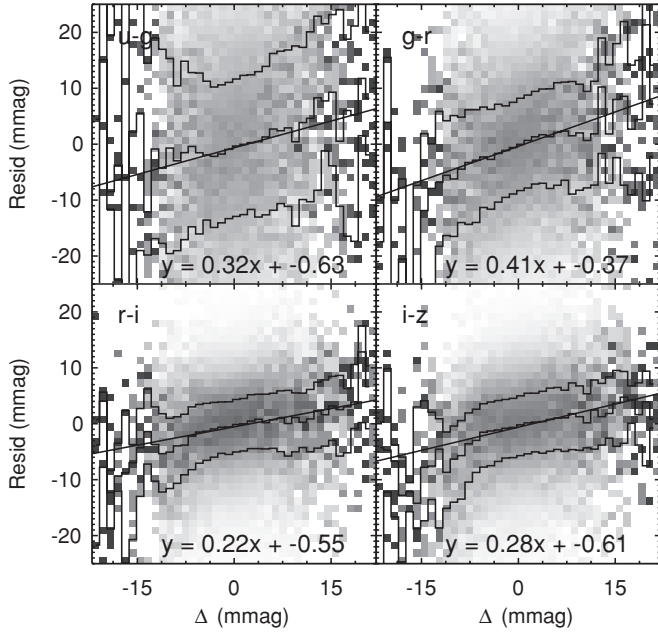


Figure 21. Blue tip color residuals vs. change in filtered dust map $E(B - V)$ from using the FIRAS temperature correction rather than the SFD temperature correction (both in mmag). The linear trend suggests that the temperature correction may be at fault.

shown are not reliable because we have not accounted for the uncertainties in Δ in performing the fit, and so the slopes may be underestimated. Regardless, the fact that a clear linear trend with significant slope exists provides strong evidence that the temperature correction at high $|b|$ is unreliable.

The FIRAS temperature correction may also explain the $\sim 15\%$ normalization difference in best-fit dust extinction spectrum observed between the north and the south in Section 4.3. The ratio $X_{\text{FIRAS}}/X_{\text{SFD}}$ in regions with $E(B - V) < 0.05$ is about 10% higher in the south than in the north (Figure 22).

5.4. The Dereddened Blue Tip in the North and South

The color of the blue tip changes because of both dust and changing stellar populations. If we deredden the blue tip according to SFD and the best-fit R_{a-b} of this work, we expect the remaining variation in blue tip color to be due to changing stellar populations (Figure 7).

A surprising feature of the dereddened blue tip maps is that the SGC appears redder than the NGC in $g - r$, $r - i$, and $i - z$, especially outside a region in the southeast of the SGC (Table 4). This may be a genuine structure in the stellar population in the south, but we are unable to distinguish that possibility from calibration errors or errors in the dust map. However, because the south tends to prefer a smaller SFD normalization than the north, the dereddened south would have been expected to be too blue rather than too red (Figure 15). Moreover, the shape of the extra reddening in the different SDSS bands does not look like any plausible reddening law.

6. CONCLUSION

The blue tip of the stellar locus provides a viable color standard for testing reddening. It is also a sensitive probe of systematics in survey photometry: we detect striping artifacts from the SDSS camera columns as well as occasional runs with bad zero points. Reddening measurements based on the stellar locus are limited because the stellar locus varies with position on

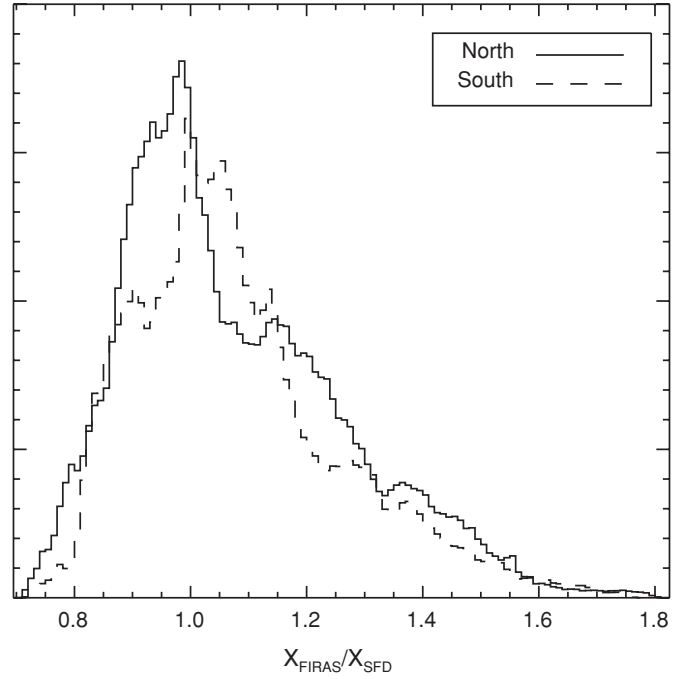


Figure 22. Ratio $X_{\text{FIRAS}}/X_{\text{SFD}}$ in the north (solid) and in the south (dashed). The temperature correction is systematically higher in the south than in the north by $\sim 10\%$, about compatible with the difference in best-fit normalization between the north and south found in Section 4.3.

Table 4
North/South Color Asymmetry

Region	$u - g$	$g - r$	$r - i$	$i - z$
North (mag)	0.817	0.228	0.064	-0.033
South (mag)	0.824	0.250	0.071	-0.020
Difference (mmag)	7.6	21.8	7.2	12.4

Notes. Median blue tip color in the north and south, with $40 < |b| < 70$. The south is systematically redder than the north. This may be a sign of an interesting stellar structure in the south, or a calibration problem or SFD error.

the sky, due to changing stellar populations. However, we find that we are able to overcome this limitation by looking for small-scale fluctuations that correlate with those in the SFD dust map. By removing the best-fit quadratic from the blue tip colors in each SDSS run, both survey systematics and sky-varying stellar populations seem adequately accounted for: Gaussian fits to the blue tip residuals have σ of 18.1, 12.3, 6.9, and 7.8 mmag, compared with the median formal statistical uncertainties σ of 17.5, 12.5, 5.7, and 5.8 mmag in $u - g$, $g - r$, $r - i$, and $i - z$, respectively. Because our errors are not Gaussian, in terms of χ^2/dof we do worse; the fits have χ^2/dof of 1.49, 1.30, 2.16, and 2.28 in the four colors.

Using these reddening measurements over the SDSS footprint, including, especially, the new, dustier, southern data, we can sensitively constrain the SFD dust map normalization in each SDSS color. The original SFD values for $A_b/E(B - V)$ were in error because the filter responses used in the SFD appendix did not match the eventual filter responses used in the SDSS. After taking this into account, our measurements and an $R_V = 3.1$ O'Donnell reddening law match closely, except in $i - z$, where the O'Donnell reddening law overpredicts reddening dramatically. We find an F99 reddening law provides a good

fit to the data, with $R_V = 3.1$ and $N = 0.78$. We recommend the use of this reddening law and normalization for use with SFD and dereddening optical data, or, for SDSS data, the use of the constants R_{a-b} presented in Table 1.

This result largely vindicates the SFD normalization at high Galactic latitudes and low column densities, which had been called into question by earlier studies in dustier regions. Except in $u - g$, where the SDSS system response assumed by SFD was in error, and in $i - z$, where the O'Donnell reddening law overpredicts reddening, we do not find that SFD overpredicts extinction by 40%. In $g - r$, the closest band to the SFD $B - V$ calibration, our normalization agrees with the SFD normalization within 4%. Extrapolating from the SDSS bands to $B - V$, we find that SFD overpredicts $E(B - V)$ by 14%. However, because the best-fit normalization varies over the sky, this result depends on the footprint that we have analyzed, and will be different in other areas. The fit results indicate that the normalization varies between clouds by 10%.

We have also made maps of the R_V and N over the SDSS footprint. However, we do not yet recommend the use of these maps except in regions where the S/N is high, where we use these values to compute the R_{a-b} covariance matrix. We are actively investigating incorporating similar maps of R_V and N into future dust extinction maps, properly combining them with the available FIR data.

The fact that the best-fit normalization of the dust map varies over the sky points to problems with the SFD temperature correction. However, the dust extinction spectrum is relatively stable, indicating that at least in regions with $E(B - V) \lesssim 0.5$, objects can be dereddened in the optical assuming a universal extinction law to within a few percent accuracy.

The blue tip colors, dereddened according to the SFD dust map with the coefficients from this work, show no coherent residuals greater than about 30, 30, 10, and 10 mmag in the footprint we analyze, which covers most of the high-latitude sky. Over much of the sky, residuals are within the statistical uncertainties.

These reddening measurements permit detailed tests of dust maps over a large sky area and over a range of dust temperatures and column densities. We have been able to find clear signs of shortcomings in the SFD temperature correction. In future work, we plan to construct new dust maps based on dust emission, constrained to best fit these measurements. Future surveys such as Pan-STARRS (Kaiser et al. 2002), the Dark Energy Survey (Flaugher 2005), and the Large Synoptic Survey Telescope (Tyson 2002) will permit this technique to be used in other bands and to fainter magnitudes with better accuracy, allowing extended wavelength coverage and admitting dustier regions near the Galactic plane to be studied.

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APPENDIX

USING SFD TO PREDICT EXTINCTION IN SPECIFIC CLOUDS

Frequently it is useful to estimate the reddening through a particular cloud for which the reddening law is expected to be different from the Galactic average, as when the cloud has R_V substantially different from three. The correct procedure in such cases is not to use $A_V = R_V E(B - V)_{\text{SFD}}$, because in such clouds $E(B - V) \neq E(B - V)_{\text{SFD}}$, as SFD is ultimately a map of optical depth at $100 \mu\text{m}$, and the ratio of the $100 \mu\text{m}$ optical depth to $E(B - V)$ is itself a function of R_V .

If the cloud in question has SDSS coverage, the surest footing is to use the measured blue tip colors for that cloud to derive the extinction law in that cloud. If SDSS coverage is not available, extrapolation from SFD or some alternative method is required.

In order to extrapolate from SFD, we have found that the best procedure is to take the SFD prediction for $E(B - V)$ and transform this to a prediction for extinction at $1 \mu\text{m}$. This gives $A_{1 \mu\text{m}} = 0.78/1.32 \cdot E(B - V)_{\text{SFD}}$, where 0.78 is our best-fit value for $A_{\text{bluetip}, \text{F99}}/A_{\text{SFD}, \text{O'D}}$ at $1 \mu\text{m}$ and 1.32 is the ratio $E(B - V)/A_{1 \mu\text{m}}$ for an O'Donnell $R_V = 3.1$ reddening law. Next, reddening in any other band can be estimated by extrapolating from $A_{1 \mu\text{m}}$ according to an F99 reddening law. Other reddening laws can be used, though they will require constants other than 0.78 in the above equation.

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