B335: A LABORATORY FOR ASTROCHEMISTRY IN A COLLAPSING CLOUD

NEAL J. EVANS II AND JEONG-EUN LEE

Department of Astronomy, University of Texas at Austin, 1 University Station C1400, Austin, TX 78712-0259;

nje@astro.as.utexas.edu, jelee@astro.as.utexas.edu

JONATHAN M. C. RAWLINGS Department of Physics and Astronomy, University College London, Gower Street, London WC1E 6BT, UK; jcr@star.ucl.ac.uk

AND

Мілно Сної

Taeduk Radio Astronomy Observatory, Korea Astronomy Observatory, Hwaam 61-1, Yuseong, Daejeon 305-348, Korea; minho@trao.re.kr Received 2004 December 2; accepted 2005 March 16

ABSTRACT

We present observations of 25 transitions of 17 isotopologues of nine molecules toward B335. With a goal of constraining chemical models of collapsing clouds, we compare our observations, along with data from the literature, to models of chemical abundances. The observed lines are simulated with a Monte Carlo code, which uses various physical models of density and velocity as a function of radius. The dust temperature as a function of radius is calculated self-consistently by a radiative transfer code. The gas temperature is then calculated at each radius, including gas-dust collisions, cosmic rays, photoelectric heating, and molecular cooling. The results provide the input to the Monte Carlo code. We consider both ad hoc step function models for chemical abundances taken from self-consistent modeling of the evolution of a star-forming core. The step function models can match the observed lines reasonably well, but they require very unlikely combinations of radial variations in chemical abundances. Among the self-consistent chemical models, the observed lines are matched best by models with somewhat enhanced cosmic-ray ionization rates and sulfur abundances. We discuss briefly the steps needed to close the loop on the modeling of dust and gas, including off-center spectra of molecular lines.

Subject headings: astrochemistry — ISM: abundances — ISM: individual (B335) — ISM: molecules

1. INTRODUCTION

The Bok globule, B335, is a rather round, dark globule at a distance of about 250 pc (Tomita et al. 1979). It is perhaps the best case for being a collapsing protostar. Observations of CS and H_2CO lines (Zhou et al. 1993; Choi et al. 1995) were reproduced very well with models of inside-out collapse (Shu 1977). To the extent that such models may describe the actual density and velocity fields in B335, this source provides an excellent test bed for astrochemical models. The only remaining variables in modeling the lines would be the chemical abundances of the species in question. It is even possible to trace variations in the abundance as a function of radius, because the different parts of the line profile arise in different locations along the line of sight. Adding the information from the excitation requirements of different lines provides a probe of the abundance through the static envelope and into the collapsing core of the protostar.

On the other hand, the depletion of molecules that is quite apparent in pre-protostellar cores (e.g., Caselli et al. 2002; Lee et al. 2003) warns us that molecular lines alone may be misleading. In the case of B335, Shirley et al. (2002) found that the Shu infall model that fitted the molecular lines (Choi et al. 1995) did not reproduce the dust emission. They found instead that a power-law density model with higher densities at all radii than the best-fit Shu model was needed to fit the dust emission. We consider models more similar to the best-fitting power law, as well.

In general, the molecular lines and dust emission have complementary advantages and disadvantages. The lines can be strongly affected by depletion that varies with radius, while the dust shows no convincing evidence so far for variation of opacities with radius (Shirley et al. 2002). On the other hand, variation in opacities with radius is also not ruled out, and the actual value of the opacity at long wavelengths is quite uncertain, by factors of at least 3 and possibly more. The dust emission is sensitive only to the column density along a line of sight, while the line emission can in principle probe the volume density via excitation analysis. Finally, only the lines can probe the kinematics, but that probe can be confused by depletion effects (Rawlings & Yates 2001), and the dust is needed to constrain these effects. Clearly, the best approach is a unified model for both gas and dust components.

We present new observations of a large number of species toward B335, using Haystack Observatory and the Caltech Submillimeter Observatory (CSO). We also present the results of detailed models of radiative transport in dust to determine the dust temperature for several different physical models. Next, we calculate the gas kinetic temperature, including gas-dust interactions, cosmic rays, and photoelectric heating. With these as a basis, we calculate the molecular excitation and radiative transport, using a Monte Carlo code (Choi et al. 1995). A telescope simulation code produces model line profiles, given an input model of the density, temperature, velocity, and abundances as a function of radius, for comparison with the observed line profiles. Based on the comparison, the abundances of various species are constrained. We use step function models for the abundances and also the results of new calculations of

TABLE 1
OBSERVING PARAMETERS

	ν			θ_b	δv		
Line	(GHz)	Telescope	$\eta_{ m mb}$	(arcsec)	$(km s^{-1})$	Reference	Date
CI $1 \rightarrow 0$	492.1607	CSO	0.47	16	0.080	1	1996 Jun
$CN \ 2 \rightarrow 1 \ldots \ldots$	226.874745	CSO	0.60	27	0.14	1	1998 Jul
$C^{17}O \ 2 \rightarrow 1$	224.714368 ^a	CSO	0.81	33	0.17	1	2000 Jun
$C^{18}\!O\ 2 \rightarrow 1$	219.560352	CSO	0.57	28	0.15	1	1998 Jul
$C^{18}O \ 3 \rightarrow 2$	329.3305453	CSO	0.82	26	0.10	1	2000 Jul
$HCO^+ 1 \rightarrow 0$	89.188512	Haystack	0.12	25	0.10	1	1994 Jun
$H^{13}CO^+ \ 1 \rightarrow 0 \ldots \ldots$	86.754330	Haystack	0.12	25	0.10	1	1994 Jun
$HCO^+ 3 \rightarrow 2$	267.557619	CSO	0.65	26	0.18	1	1995 Mar
$H^{13}CO^+ \ 3 \rightarrow 2 \ldots \ldots$	260.255339	CSO	0.65	26	0.18	1	1995 Mar
$HC^{18}O^+ \ 3 \rightarrow 2 \ldots \ldots$	255.47940	CSO	0.65	26	0.18	1	1995 Mar
$HCO^+ 4 \rightarrow 3$	356.734288	CSO	0.61	20	0.14	1	1995 Mar
$DCO^+ 3 \rightarrow 2$	216.112604	CSO	0.57	28	0.16	1	1998 Jul
HCN $1 \rightarrow 0$	89.635847	TRAO	0.40	61	0.068	2	1997
HCN $3 \rightarrow 2$	265.8864343	CSO	0.65	23	0.15	1	1996 Jun
$H^{13}CN \ 3 \rightarrow 2$	259.011814	CSO	0.65	23	0.15	1	1996 Jun
HNC $3 \rightarrow 2$	271.981142	CSO	0.62	22	0.11	1	1996 Jun
HNC $4 \rightarrow 3$	362.630303	CSO	0.53	19	1.62	1	1997 Jul
$HC_3N \ 24 \rightarrow 23$	218.324788	CSO	0.56	28	0.18	1	1996 Jun
$N_2H^+ \ 1 \rightarrow 0$	93.176258 ^b	Haystack	0.12	25	0.10	1	1994 Jun
$N_2H^+ 3 \rightarrow 2$	279.511757 [°]	CSO	0.56	22	0.12	1	1996 Oct
$N_2D^+ 3 \rightarrow 2$	231.321775	CSO	0.73	32	0.21	1	2001 Jul
Para- $H_2^{13}CO \ 1_{01} - 0_{00}$	71.02478	NRAO	0.95	89	0.206	3	
$H_2^{13}CO 2_{12} - 1_{11}$	137.44996	NRAO	0.72	42	0.1065	3	
$H_2CO 2_{12}-1_{11}$	140.839518	IRAM	0.68	17	0.083	4	
Para-H ₂ ¹³ CO 2_{02} -1 ₀₁	141.98375	NRAO	0.72	42	0.103	3	
$H_2^{13}CO 2_{11} - 1_{10}$	146.63569	NRAO	0.72	42	0.0998	3	
$H_2CO 3_{12}-2_{11}$	225.697772	IRAM	0.50	12	0.066	4	
$H_2CO 3_{12}-2_{11}$	225.697787	CSO	0.65	27	0.127	1	1996 Jun
Para-H ₂ CO 3_{03} - 2_{02}	218.222186	CSO	0.65	28	0.131	1	1996 Jun
$H_2CO 5_{15} - 4_{14}$	351.768645	CSO	0.53	20	0.083	1	1997 Jun
Para-H ₂ CO 5_{05} - 4_{04}	362.3530480	CSO	0.53	19	0.085	1	1997 Jun
Para-H ₂ CO 5_{23} - 4_{22}	365.3634280	CSO	0.53	19	0.085	1	1997 Jun

^a Reference frequency for the hyperfine shifts in Ladd et al. (1998).

^b For the isolated hyperfine component (Lee et al. 2001).

^c Reference frequency for the hyperfine shifts in Caselli et al. (2002).

REFERENCES.—(1) This paper; (2) Park et al. 1999; (3) Minh et al. 1995; (4) Zhou et al. 1993.

abundances in a cloud collapsing according to the Shu picture (Lee et al. 2004).

2. OBSERVATIONS

We obtained observations of the HCO⁺ and $N_2H^+J = 1 \rightarrow 0$ lines at the Haystack Observatory in 1995 March. Observations of a large number of lines were obtained at the Caltech Submillimeter Observatory in the period from 1995 March to 2001 July. Table 1 provides the reference frequency for the line, the telescope, the main beam efficiency ($\eta_{\rm mb}$), the FWHM beam size (θ_b) , the velocity resolution (δv) , and the date of observation. We also provide this information for several observations obtained previously that are used to constrain the modeling. The frequencies in Table 1 are either those used during observing or those used later to shift the observed data to an improved rest frequency. For most lines with hyperfine components, these are the reference frequencies suitable for a list of hyperfine components that were used to fit lines. In the case of the N_2H^+ $J = 1 \rightarrow 0$ line, it is the frequency of the isolated hyperfine component, best suited for determining the velocity.

In the following sections, we assume that the centroid of B335 is at $\alpha = 19^{h}34^{m}35^{s}4$, $\delta = 07^{\circ}27'24''$ in B1950.0 coordinates. This position agrees within 1" with the centroid of the submillimeter emission mapped with the Submillimeter Common-User Bolometric Array (SCUBA; Shirley et al. 2000). This position was originally based on the position of the millimeter continuum source seen by Chandler & Sargent (1993); more recent interferometric data find a compact component located 3".6 west and 1" south of this position (Wilner et al. 2000). At this position, a continuum source is also seen at 3.6 cm, attributed to a timevariable radio jet elongated along the outflow axis (Reipurth et al. 2002). The difference between our position and the position of the compact component is not significant for the resolution of these observations. Some of our data were obtained before we settled on this position. In cases where we have a map, we may have resampled the data spatially to synthesize a spectrum at the submillimeter centroid position, resulting in a slight degradation of the spatial resolution.

3. RESULTS

The primary observational results are presented in Table 2 and Figures 1–7. The table gives the integrated intensity $(\int T_A^* dv)$, the peak antenna temperature (T_A^*) , the velocity with respect to the local standard of rest (v_{LSR}) , and the line width (FWHM, Δv). For simple, single-peaked lines, these were determined from a Gaussian fit. For self-reversed lines without hyperfine structure $(\text{HCO}^+ J = 1 \rightarrow 0, J = 3 \rightarrow 2, \text{ and } J = 4 \rightarrow 3), \int T_A^* dv$ is the total area under the full line, T_A^* is the strength of the stronger

TABLE 2

	OB	SERVATIONAL RESULT	ГS		
Molecule	Line	$\int T_A^* dv \\ (\text{K km s}^{-1})$	T^*_A (K)	$v_{\rm LSR}$ (km s ⁻¹)	$\Delta v \ ({ m km~s^{-1}})$
CI	J=1 ightarrow 0	0.80 ± 0.04	1.51 ± 0.18	8.29 ± 0.01	0.50 ± 0.03
CN ^{a,b}	$J = 2 \rightarrow 1$	0.90 ± 0.02	0.43 ± 0.02	8.35 ± 0.04	0.62 ± 0.07
C ¹⁷ O ^c	$J = 2 \rightarrow 1$	0.46 ± 0.07	0.57 ± 0.07	8.39 ± 0.02	0.49 ± 0.07
C ¹⁸ O	$J = 2 \rightarrow 1$	0.63 ± 0.42	1.10 ± 0.10	8.27 ± 0.02	0.57 ± 0.04
C ¹⁸ O	J=3 ightarrow 2	0.78 ± 0.09	2.15 ± 0.26	8.33 ± 0.04	0.64 ± 0.08
HCO ^{+a}	$J = 1 \rightarrow 0$	0.71 ± 0.05	1.15 ± 0.11	8.35 ± 0.03	0.61 ± 0.10
H ¹³ CO ⁺	$J = 1 \rightarrow 0$	0.24 ± 0.06	0.33 ± 0.02	8.23 ± 0.04	0.58 ± 0.03
HCO ^{+a}	J=3 ightarrow 2	3.13 ± 0.05	3.32 ± 0.08	8.46 ± 0.04	0.94 ± 0.16
H ¹³ CO ⁺	$J = 3 \rightarrow 2$	0.46 ± 0.01	0.76 ± 0.03	8.25 ± 0.01	0.57 ± 0.02
HC ¹⁸ O ⁺	J=3 ightarrow 2	0.05 ± 0.01	0.09 ± 0.01	8.26 ± 0.04	0.58 ± 0.10
HCO ^{+a}	$J = 4 \rightarrow 3$	2.27 ± 0.15	2.35 ± 0.06	8.55 ± 0.03	0.97 ± 0.12
DCO ⁺	J=3 ightarrow 2	0.78 ± 0.03	1.32 ± 0.04	8.35 ± 0.01	0.55 ± 0.02
HCN ^{a,b}	$J = 1 \rightarrow 0$	0.59 ± 0.10	0.35 ± 0.05	8.39 ± 0.01	0.70 ± 0.10
HCN ^a	J=3 ightarrow 2	0.81 ± 0.03	0.80 ± 0.02	8.40 ± 0.20	1.01 ± 0.04
H ¹³ CN	$J = 3 \rightarrow 2$		< 0.1		
HNC	J=3 ightarrow 2	0.22 ± 0.01	0.49 ± 0.03	8.16 ± 0.01	0.42 ± 0.03
HNC	$J = 4 \rightarrow 3$	0.39 ± 0.05	0.16 ± 0.03	8.33 ± 0.16	2.3 ± 0.4
HC ₃ N	J=24 ightarrow23		< 0.08		
N ₂ H ^{+d}	$J = 1 \rightarrow 0$	0.13 ± 0.01	0.25 ± 0.02	8.33 ± 0.01	0.47 ± 0.02
N ₂ H ^{+a,b}	J=3 ightarrow 2	0.95 ± 0.08	1.00 ± 0.04	8.38 ± 0.03	0.38 ± 0.04
$N_2 D^{+c}$	J=3 ightarrow 2	0.32 ± 0.04	0.38 ± 0.04	8.36 ± 0.02	0.31 ± 0.05
H ₂ CO	$J_{K_{-1}K_{+1}} = 3_{12} \rightarrow 2_{11}$	0.55 ± 0.01	0.63 ± 0.02	8.26 ± 0.01	0.82 ± 0.02
Para-H ₂ CO	$J_{K_{-1}K_{+1}} = 3_{03} \rightarrow 2_{02}$	0.45 ± 0.01	0.59 ± 0.03	8.28 ± 0.01	0.71 ± 0.03
H ₂ CO	$J_{K_{-1}K_{+1}} = 5_{15} \rightarrow 4_{14}$	0.49 ± 0.03	0.57 ± 0.07	8.30 ± 0.02	0.80 ± 0.07
Para-H ₂ CO	$J_{K_{-1}K_{+1}} = 5_{05} \rightarrow 4_{04}$	0.40 ± 0.06	0.31 ± 0.11	8.53 ± 0.08	1.22 ± 0.23
Para-H ₂ CO	$J_{K_{-1}K_{+1}} = 5_{23} \to 4_{22}$		< 0.2		

^a Double-peaked: $\int T_A^* dv$ is for total area under both peaks, T_A^* refers to strongest peak, v_{LSR} refers to dip, and Δv is integrated intensity divided by peak T_A^* .

^b Hyperfine structure: $\int T_A^* dv$ refers to area under all lines and Δv is determined from isolated hyperfine component.

^c Hyperfine structure: $\int T_A^* dv$ refers to area under all lines, T_A^* refers to main peak of blended components, and v_{LSR} and Δv are from fit to blended components.

^d All entries refer to the isolated hyperfine component.

peak, v_{LSR} is the velocity of the dip, determined by eye, and Δv is $\int T_A^* dv$ divided by T_A^* . For lines with hyperfine structure (C¹⁷O $J = 2 \rightarrow 1$ and N₂D⁺ $J = 3 \rightarrow 2$), $\int T_A^* dv$ gives the area under all the hyperfine components, T_A^* gives the peak of the strongest, usually blended components, and v_{LSR} and Δv come from a fit with all the hyperfine components. For the most complex situation, lines that are self-reversed, with hyperfine structure, various strategies were adopted. For CN $J = 2 \rightarrow 1$, $\int T_A^* dv$, T_A^* , and v_{LSR} were determined as for double-peaked lines, but Δv was determined from an isolated component. The spectrum of CN (Fig. 6) clearly shows that the main hyperfine

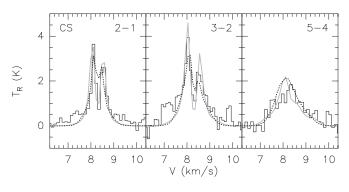


FIG. 1.—Observations of the CS lines observed at IRAM (Zhou et al. 1993; *black solid histogram*). The gray solid line is for the model with the step function abundance, and the dotted line shows the model with the chemical abundance.

line is self-reversed. For $N_2H^+J = 1 \rightarrow 0$, all line parameters were determined from the isolated component at the frequency given in Table 1, as suggested by Lee et al. (2001).

The observations that are compared to full models are shown as solid lines in Figures 1–6. The CN $J = 2 \rightarrow 1$ spectrum in Figure 6 has not been modeled, and the dashed line is just a fit to the hyperfine components. Other spectra that are not modeled in detail are shown in Figure 7. These include spectra with complex hyperfine splitting that we cannot model in detail and molecules without good collision rates.

The HCN $J = 3 \rightarrow 2$ line is peculiar in that there is essentially no emission at velocities that would normally be associated with the red part of the main hyperfine component. To ensure that this effect was not caused by emission in the off position (10' west), we took a deep integration in the off position. No emission was seen at a level of 0.08 K.

Single-peaked lines without overlapping hyperfine components provide the best measure of the rest velocity of the cloud. Based on those lines least likely to be optically thick, the cloud velocity is $\langle v_{\text{LSR}} \rangle = 8.30 \pm 0.05 \text{ km s}^{-1}$. For self-reversed lines, the mean velocity of the dip (determined by eye) is $\langle v_{\text{dip}} \rangle = 8.41 \pm 0.06 \text{ km s}^{-1}$. All the values for v_{dip} exceed those for $\langle v_{\text{LSR}} \rangle$, by amounts ranging from 0.05 to 0.25 km s⁻¹. The mean shift, $\langle v_{\text{dip}} - \langle v_{\text{LSR}} \rangle \rangle = 0.11 \pm 0.07$. Also, lines from higher J levels have higher v_{dip} than those from lower J levels, suggesting that the dip arises partially from inflowing gas. The three lines of HCO⁺, for example, have their dips at increasing velocity, with the $J = 4 \rightarrow 3$ showing $v_{\text{dip}} = 8.55 \text{ km s}^{-1}$. This

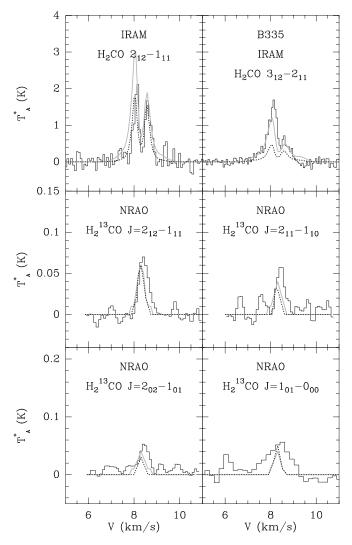


Fig. 2.—Observations of H_2CO , shown as black solid histograms, and models, shown as gray solid lines (step functions) and dotted lines (chemical abundances). The telescopes where the data were obtained are identified in each panel. The IRAM data were taken from Zhou et al. (1993), and the NRAO data were supplied by W. Irvine (1996, private communication), based on data in Minh et al. (1995). The bottom two panels are para- $H_2^{13}CO$.

progression is similar to a pattern seen in CS lines toward IRAM 04191 by Belloche et al. (2002).

4. THE MODELING PROCEDURE

We use the extensive observations described above to test models of the source. All the models are spherical with smooth (nonclumpy) density distributions. We focus on inside-out collapse models, although we discuss some variations on this basic model. All models include self-consistent calculations of the dust and gas temperature distributions (§ 4.1) and calculations of the molecular populations, radiative transport, and line formation (§ 4.3). Two kinds of models of the abundances as a function of radius are used: step function models and abundances from an evolutionary chemical calculation (Lee et al. 2004), as described in § 4.2.

4.1. Determining Temperatures

The first step in comparing a physical model to observations is to determine the temperatures that correspond to a particular density distribution. The dust temperatures can be calculated

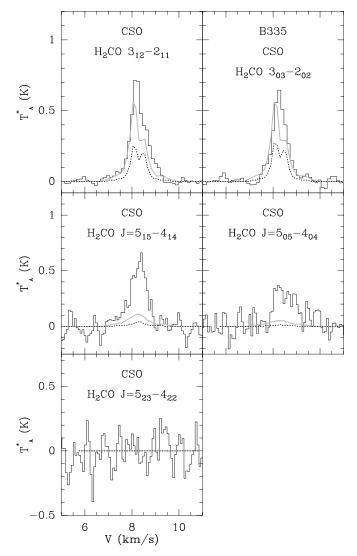


Fig. 3.—Further observations of H_2CO , shown as black solid histograms, and models, shown as gray solid lines and dotted lines. The telescopes where the data were obtained are identified in each panel.

self-consistently for a particular density distribution by various radiative transfer codes. We used the code of Egan et al. (1988) and the techniques described by Shirley et al. (2002) for constraining parameters.

We assumed that dust opacities are given by column (5) of the table in Ossenkopf & Henning (1994), known as OH5 opacities, because these have been shown to match many observations of star-forming cores (e.g., Shirley et al. 2002). One difference between the models by Shirley et al. and the current work is in the treatment of the interstellar radiation field (ISRF). In the previous work, we decreased the strength of the ISRF by a constant factor (s_{ISRF}) at all wavelengths (except for the contribution of the cosmic microwave background). For B335, we used $s_{ISRF} = 0.3$. In the present work, we instead attenuate the ISRF using the Draine & Lee (1984) extinction law and assuming $A_V = 1.3$ mag. This procedure affects short wavelengths much more than long wavelengths, leading to a somewhat less pronounced rise in dust temperature toward the outside of the cloud. The choice of $A_V = 1.3$ mag is somewhat arbitrary, but it accounts for the fact that molecules require some dust shielding. It will also produce consistent results when we consider the gas energetics.

Shirley et al. (2002) assumed an outer radius of 60,000 AU for most B335 models. We mostly use an outer radius of 0.15 pc

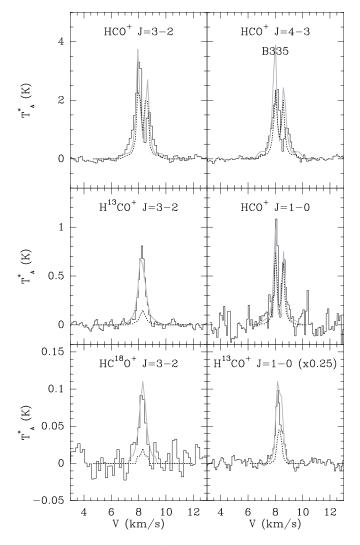


FIG. 4.—Observations of HCO⁺, shown as black solid histograms, and models, shown as gray solid lines (step functions) and dotted lines (chemical abundances). The $J = 1 \rightarrow 0$ lines were obtained at Haystack, and the other lines were obtained at the CSO. Both models and observations of the H¹³CO⁺ $J = 1 \rightarrow 0$ line have been multiplied by 0.25 to fit them on the same scale as the HC¹⁸O⁺ line.

(31,000 AU), as used by Choi et al. (1995). Studies of the extinction as a function of impact parameter from *Hubble Space Telescope* (*HST*) Near-Infrared Camera and Multi-Object Spectrometer (NICMOS) data are consistent with an outer radius of about this size (Harvey et al. 2001), in the sense that the extinction decrease with radius blends into the noise at that radius. The choice of outer radius makes little difference in most models. The inner radius for the dust models is taken to be 10^{-3} of the outer radius for the dust models in order to capture the conversion of short-wavelength radiation. The stellar temperature is set to 6000 K, but this choice is completely irrelevant because of the rapid conversion to longer wavelength radiation. The luminosity was set to 4.5 L_{\odot} , which provided the best fit to a Shu model in Shirley et al. (2002).

Once we have a dust temperature distribution, $T_d(r)$, and a density distribution, n(r), we can compute the gas temperature distribution, $T_K(r)$. This was done with a gas-dust energetics code written by S. Doty (see Doty & Neufeld [1997] and the appendix in Young et al. [2004] for descriptions). This code includes energy transfer between gas and dust, heating by cosmic

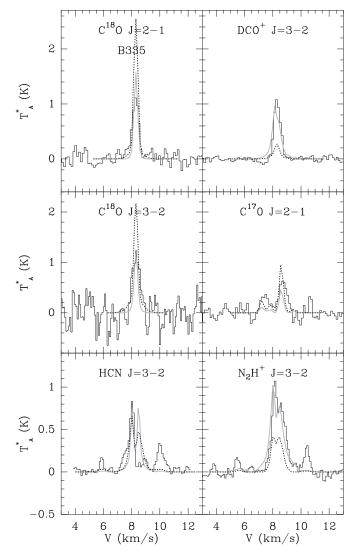


Fig. 5.—Selected observations of isotopes of CO, DCO^+ , HCN, and N_2H^+ , shown as solid black histograms, and predicted lines from the model, shown as gray solid lines (step functions) and dotted lines (chemical abundances).

rays and the photoelectric effect with polycyclic aromatic hydrocarbons, and molecular cooling.

The gas-dust energy transfer via collisions depends on the total grain cross section per baryon, averaged over the distribution of grain sizes (Σ_d). Following the discussion in the appendix of Young et al. (2004), we take this value to be $6.09 \times$ 10^{-22} cm². The cosmic-ray heating depends on the cosmic-ray ionization rate (ζ), which we take to be 3×10^{-17} s⁻¹ (van der Tak & van Dishoeck 2000). The photoelectric heating follows the equation of Bakes & Tielens (1994), which includes heating from the photoelectric effect on very small grains. The rate depends on the strength of the ultraviolet portion of the ISRF and the electron density. Because this heating is only important on the outside of the cloud, we set the electron density to $1 \times$ 10^{-3} cm⁻³. The radiation field is assumed to be attenuated by the surrounding medium according to $\tau_{\rm UV} = 1.8A_V$; with $A_V =$ 1.3, the scale factor for the ISRF impinging on our model's outer radius is $G_0 = 0.1$. Once inside the cloud, the radiation is attenuated according to a fit to the attenuation produced by the dust assumed to be in the cloud.

The result of these calculations is shown for a typical model in Figure 8. For small radii, $T_K \approx T_d$, as is usually assumed, but T_K falls below T_d with increasing radius, as the density becomes

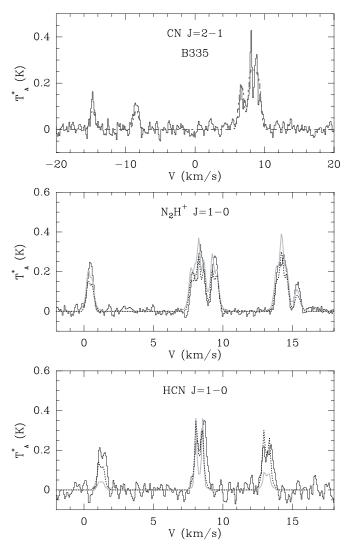


FIG. 6.—Observations of the CN $J = 2 \rightarrow 1$, N₂H⁺ $J = 1 \rightarrow 0$, and HCN $J = 1 \rightarrow 0$ lines, shown as black solid histograms. For CN, the dotted line is a fit of Gaussians to the hyperfine components, not a true model. The fit to hyperfine components clearly does not reproduce the shape of the main group of lines. The dip is centered at 8.35 km s⁻¹, indicating that the main group is self-reversed. For N₂H⁺ and HCN $J = 1 \rightarrow 0$, the gray solid (step functions) and dotted (chemical abundances) lines are predictions of the radiative transfer model.

too low for collisions with dust to maintain the kinetic temperature at the dust temperature. Then, at some radius, T_K rises as photoelectric heating takes over, and $T_K > T_d$. The downturn in T_K at the cloud edge appears to be real and caused by the cooling lines of CO becoming optically thin (see Young et al. 2004). However, this drop in temperature has no appreciable effect on the resulting line profiles.

The amount of photoelectric heating is the least certain of these inputs, as the external attenuation has a large effect on how warm the outer cloud gets. To constrain G_0 , we modeled the lower three lines of CO and compared these to data in the literature (e.g., Goldsmith et al. 1984; Langer et al. 1986). To avoid producing a CO $J = 1 \rightarrow 0$ line that exceeded the observations, G_0 definitely needed to be decreased from unity. The value of $G_0 = 0.1$ provided the best match, and this was actually used to constrain the external extinction to $A_V = 1.3$. Changes by a factor of 2 in G_0 (or ± 0.4 in A_V) produced CO lines that differed from the observations by about 30%, while having no appreciable effect on the lines of other species. While other variables are uncertain in the photoelectric heating, the attenuation

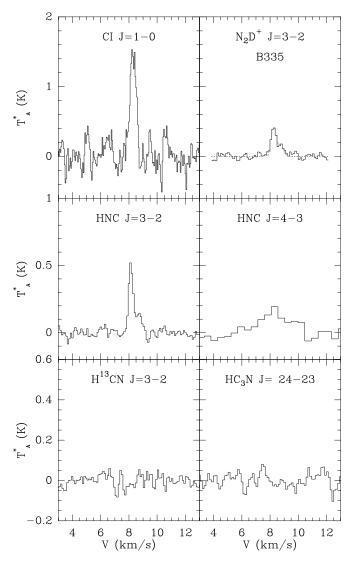


Fig. 7.—Observations of lines that are not modeled in full detail. Some have hyperfine structure. The ones with good fits using hyperfine components show the fit with a dotted line.

of the ultraviolet radiation from the ISRF is the most important variable; comparison to observations of CO readily constrains it. The results are reasonable; one does not expect significant molecular gas for $A_V < 1$ (van Dishoeck & Black 1988). One could trade off the value of s_{ISRF} and the external extinction, as long as the effective G_0 is not too different from 0.1. Constraining these separately is difficult (Shirley et al. 2005) and not particularly relevant for this paper.

The cooling rates (Doty & Neufeld 1997) depend primarily on the CO abundance and the width of the lines (through trapping); we assume $X(CO) = 7.4 \times 10^{-5}$ and b = 0.12 km s⁻¹, except for some tests described below. We note in passing the dangers of simplistic interpretation of observed CO lines; turning the observations into a kinetic temperature would lead one to conclude that T_K is constant within the cloud, while it clearly is not.

The parameters that describe the standard physical model are summarized in Table 3.

4.2. Chemical Modeling

Two kinds of abundance models are employed. The first is strictly ad hoc, using a step function to describe the abundance

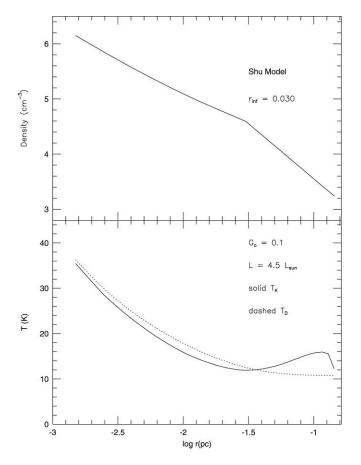


FIG. 8.—Density and temperatures for gas and dust plotted as a function of radius for the standard model.

of each species as a function of radius. These models have three free parameters per species: X, r_{dep} , and f_{dep} . The abundance in the outer parts of the cloud X is assumed to decrease inside a depletion radius r_{dep} by a factor f_{dep} .

The second kind is true chemical models, based on the calculations presented by Lee et al. (2004). These calculations follow the chemical evolution through an evolutionary sequence that includes at each step a self-consistent calculation of the dust and gas temperatures, using the techniques described in \S 4.1. The evolutionary model assumes a slow buildup in central density, via a sequence of Bonnor-Ebert spheres, to the point of a singular isothermal sphere, at which point an inside-out collapse (Shu 1977) is initiated. After this point, the chemistry is calculated for each of 512 gas parcels as it falls into the central region. Thus, gas inside the infall radius carries some memory of the conditions from farther out. We adopt the model of Young & Evans (2005) for the evolution of luminosity in order to calculate the evolution of the dust temperature. Physical parameters in the model are selected to have a total internal luminosity and a dust temperature profile similar to those obtained from the dust modeling of B335, at the time step of $r_{inf} = 0.03$ pc. The model core is assumed to stay in the same environment through

TAB Isotope		
C/ ¹³ C	O/ ¹⁸ O	¹⁸ O/ ¹⁷ O
70	540	3.5

its evolution with the same A_V and G_0 calculated in § 4.1. The chemical calculation includes the interaction between gas and dust grains as well as gas-phase reactions, but the surface chemistry is not considered in the calculation. For details of the chemical evolution model, refer to Lee et al. (2004).

For both types of models, isotope ratios were constrained so that the abundance was only a free parameter for the whole of the isotope complex. DCO^+ was the exception, as it is subject to large fractionation effects. Assumed isotope ratios are the same as those used by Jørgensen et al. (2004) and are given in Table 4. Wouterloot et al. (2005) have recently suggested a slightly higher ratio for ${}^{18}O/{}^{17}O$ of 4.1, but this value would fit our data on the CO isotopologues somewhat worse.

4.3. Modeling of Line Profiles

The line profiles were modeled with a Monte Carlo code (mc) to calculate the excitation of the energy levels and a virtual telescope program (vt) to integrate along the line of sight, convolve with a beam, and match the velocity resolution, spatial resolution, and main beam efficiency of the observations (Choi et al. 1995). All lines were assumed to be centered at 8.30 km s^{-1} , based on the average of optically thin lines.

The input physical conditions (density, temperature, and velocity fields) were taken from the physical model being tested, using the results of the gas-dust energetics code for $T_K(r)$. Models require input data about each molecule, as well as about the source. For CS, we used collision rates from Turner et al. (1992). For HCO⁺ and N₂H⁺, we used collision rates supplied by B. Turner (1996, private communication), based on his extension of previously calculated rates to higher temperatures and energy levels (Turner 1995). For H₂CO and para-H₂CO, we used rates computed by Green (1991). Rates for HCN came from Green & Thaddeus (1974), and those for CO from Flower & Launay (1985). In some cases, rates have been extrapolated to lower temperatures.

For C¹⁷O, HCN, and N₂H⁺, the lines have hyperfine structure that is partially resolved. For these lines, mc and vt models were run separately for each clearly resolved hyperfine component, with abundances adjusted to simulate the fraction of the transition probability in that component; the results were added to make the final simulated line. Components separated by less than the 1/e width of the velocity dispersion were aggregated into a single component; the aggregated components are listed in Table 5. This procedure captures the essence of the hyperfine splitting, but it is not rigorous, because trapping is not handled correctly when there is partial line overlap (see Keto et al. 2004).

All models were run with 40 shells. The inner radius was 2×10^{-3} pc, corresponding to 1"7 at a distance of 250 pc. This

TABLE 3 Standard Physical Mode

STANDARD PHYSICAL MODEL										
Туре	$a (\mathrm{km} \mathrm{s}^{-1})$	r_{inf} (pc)	r _{out} (pc)	$L (L_{\odot})$	A_V (mag)	G_0	(\mathbf{s}^{-1})	b (km s ⁻¹)	$\binom{n_e}{(\mathrm{cm}^{-3})}$	X (CO)
Shu	0.23	0.03	0.15	4.5	1.3	0.1	3×10^{-17}	0.12	1×10^{-3}	7.4×10^{-5}

TABLE 5						
Aggregated Hyperfine Shifts and Strengths						

C ¹⁷ O 2	$2 \rightarrow 1$	HCN 1	$\rightarrow 0$	HCN 3	$3 \rightarrow 2$	$N_2 H^+ \ 1 \rightarrow 0 \qquad \qquad N_2 H$		N_2H^+ 3	$\mathrm{H^+}\ 3 \to 2$	
Δv	r_i	Δv	r_i	Δv	r_i	Δv	r_i	Δv	r_i	
1.157	0.040	4.849	0.333	1.749	0.037	6.936	0.037	2.015	0.017	
0.431	0.122	0.000	0.556	0.303	0.200	5.984	0.185	0.669	0.015	
0.241	0.571	-7.072	0.111	-0.030	0.725	5.545	0.111	0.416	0.084	
-0.526	0.093			-0.611	0.001	0.956	0.185	0.266	0.094	
-0.926	0.016			-2.348	0.037	0.000	0.259	0.076	0.089	
-1.073	0.095					-0.611	0.111	-0.073	0.615	
-1.203	0.062					-8.006	0.111	-0.601	0.010	
								-2.644	0.011	
								-2.773	0.014	

Notes.—Shift is in km s⁻¹ relative to the assumed central velocity of 8.30 km s⁻¹. Relative strength (r_i) is normalized so that $\Sigma r_i = 1$.

radius is larger than the inner radius for the dust models, because the molecular lines are not sensitive to emission from very small scales because of beam dilution. The convergence criterion for populations was set to 10% for finding the region of best-fitting parameters. Final models were run with a 2% convergence criterion to ensure accuracy; differences between these models and those run with 10% accuracy were small. The minimum fractional population tested for convergence was 10^{-6} . For an explanation of these criteria, see the appendix in Choi et al. (1995).

5. INSIDE-OUT COLLAPSE MODELS

The physical properties of the standard model are given in Table 3. The standard physical model is the inside-out collapse model (Shu 1977) that best matched (Choi et al. 1995) the CS and H₂CO data taken by Zhou et al. (1993). Choi et al. (1995) modeled CS and H₂CO lines from the IRAM telescope, assuming constant abundances, and found a best fit of $r_{inf} = 0.03$ pc. This was a compromise, as H₂CO favored smaller r_{inf} than did CS.

While the CS data were still well matched with constant abundance, the new data on more H_2CO lines suggested enhanced abundances on small scales, as did the HCO^+ data. As a result, we tested step function abundance models.

5.1. Step Function Abundances

To avoid too many free parameters, we required that $r_{dep} = r_{inf}$. While this particular choice has no theoretical justification, it leaves only two free parameters per species. With the constraints on isotope ratios in Table 4, we are left with 15 free parameters for eight species, including the special case of DCO⁺, explained below. The abundances in Table 6 are those that fit the

TABLE 6 Step Function Abundances

STEP PONCTION TEDNOMINELS								
Species	$X(r > r_{inf})$	$X(r < r_{inf})$	AD (Step)	AD (Chem)				
CS	$6.0 imes 10^{-9}$	$6.0 imes10^{-9}$	6.88	6.78				
C ¹⁸ O	$7.4 imes 10^{-8}$	$2.5 imes 10^{-8}$	3.00	3.22				
HCO ⁺	3.5×10^{-9}	$3.5 imes 10^{-8}$	3.95	4.02				
DCO ⁺	6.0×10^{-11}	$6.0 imes 10^{-10}$	1.87	3.27				
N ₂ H ⁺	$3.0 imes 10^{-10}$	$3.0 imes 10^{-9}$	5.15	6.14				
HCN	$1.0 imes 10^{-8}$	$1.0 imes 10^{-9}$	5.43	4.73				
H ₂ CO	$7.0 imes10^{-10}$	$7.0 imes 10^{-9}$	2.64	3.22				
Para-H ₂ CO	$4.0 imes 10^{-10}$	$4.0 imes 10^{-9}$						

current data reasonably well, as judged by eye and statistical measures. We calculated both the reduced chi-square (χ_r^2) and the absolute deviation $[AD = \Sigma_i | T_A^*(model; i) - T_A^*(obs; i) | / N]$ over the line profiles. The absolute deviation is more influenced by strong lines for which the shape is important to match, so we use it primarily, although the χ^2_r criterion does not differ in the choice of best model. We have not run a complete grid of models; instead, we employed some judgment to locate regions of parameter space with decent fits to the line profiles. Once reasonably good fits were obtained, both X and f_{dep} were varied by factors of 3 in each direction, showing substantially worse fits. These parameters should be considered constrained at that level. The abundances in Table 6 are those for the best-fitting step functions, and the predicted line profiles are shown in Figures 1-6 as gray lines. The values of AD in Table 6 are an average over all the lines for all isotopologues of that species.

The CS lines were still matched best with constant abundance. On the small scales (0.003 pc) probed by interferometers, the CS is clearly depleted in the envelope, and the $J = 5 \rightarrow 4$ emission arises from a clump that is offset from the central source (Wilner et al. 2000). A model with CS depleted by a factor of 10 for $r_{dep} = 0.003$ pc showed no appreciable effect on the $J = 2 \rightarrow 1$ or $J = 3 \rightarrow 2$ lines, but it did decrease the predicted $J = 5 \rightarrow 4$ intensity slightly.

The H₂CO abundance that best fits the data is slightly higher than was found by Choi et al. (1995), mostly to improve the fit to the lines of H₂¹³CO and para-H₂¹³CO. We also increased the abundance of both H₂CO and para-H₂CO in the inner parts of the cloud to improve the fit to our new CSO observations of the higher J lines, whereas Choi et al. (1995) had found a constant abundance to be satisfactory. Even so, we do not reproduce the very high excitation H₂CO lines, indicating that a warm, dense region must exist that is not predicted by the basic model.

The abundance of H₂CO listed in Table 6 is actually the abundance of ortho-H₂CO. Minh et al. (1995) found that ortho-H₂CO/para-H₂CO was 1.7 in B335, assuming a uniform cloud. Our modeling, which employs density, temperature, and velocity gradients, confirms that this ratio works well in reproducing the observations, but we have not determined the range of acceptable values. Minh et al. (1995) noted that this ratio was consistent with ortho-para equilibration on cold dust grains and suggested that the gas-phase H₂CO in B335 had formerly resided on dust grains. In this picture, they suggested that warming by the newly formed star or by shocks had liberated the H₂CO from the dust grains. Our model for the dust temperature indicates that T_d stays below 20 K until r < 0.006 pc (6"),

where any H_2CO would be beam diluted. Thus, other means for releasing the H_2CO from dust mantles should be explored.

The lines of HCO⁺ and its isotopologues are best matched with a model with increased abundances inside r_{inf} . HCO⁺ is clearly quite abundant in B335, as witnessed by the detection of HC¹⁸O⁺. The observed $J = 3 \rightarrow 2$ and $J = 4 \rightarrow 3$ lines of HCO⁺ are somewhat weaker than the models predict, and the dip is shifted to the red (§ 5.2). The abundance of DCO⁺ was treated as a free parameter, but r_{dep} and f_{dep} were constrained to the same value as for HCO⁺; the best fit was obtained for HCO⁺/DCO⁺ of 55.

The C¹⁸O lines were fitted best with decreased abundances (but only by a factor of 3) inside r_{inf} . With the enforced C¹⁸O/C¹⁷O ratio of 3.5, the $C^{17}O$ model line is a bit weaker than the observed line, but the data are rather noisy. Using the standard isotope ratio, the best-fit abundance of C¹⁸O would imply $X(CO) = 4 \times$ 10^{-5} . This abundance is substantially less than expected from chemical models and even less than what we assume in our calculation of cooling rates (\S 4.1). To see the consequences, we ran a model with the abundance adjusted to this value in the calculation of cooling rates. The value of T_K in the outer parts of the cloud was increased by a few degrees, but the effect on most molecular lines was very small, indicating that the best fit is not affected by this slight inconsistency. The CO line predictions were exceptions, as these lines actually got stronger with decreased CO abundance because of the higher T_K in the relevant layers of the cloud.

The two lines of N₂H⁺ both have hyperfine structure, and our method for dealing with this is only approximate. Nonetheless, the $J = 1 \rightarrow 0$ transition is matched reasonably well (Fig. 6) with a factor of 10 increase in abundance inside r_{inf} . In contrast, the satellite hyperfine lines of the $J = 3 \rightarrow 2$ line are clearly stronger than the models can explain.

The most troublesome species was HCN. The satellite hyperfine lines of both $J = 1 \rightarrow 0$ and $J = 3 \rightarrow 2$ transitions are much stronger than the models can account for, even with a very large HCN abundance. Still larger abundances predicted lines of the stronger hyperfine components that were much stronger than observed. In addition, the HCN $J = 3 \rightarrow 2$ line is very peculiar, with the red side of the line essentially missing, indicative of a deep absorption layer. To try to match some of these features within the constraints of our model, we depleted HCN by a factor of 10 inside r_{inf} . This helped, but the fits are still poor. The fact that the H¹³CN $J = 3 \rightarrow 2$ line was not detected makes the strength of the hyperfine satellite lines (Fig. 7) even harder to understand.

5.2. Variations in the Physical Model

With the additional freedom of the step function abundance profile, is $r_{inf} = 0.03$ pc still the best model? This question was explored to a limited degree; for each new r_{inf} , the abundances of each species were optimized, but the shape of the step function was not allowed to change, except for CS, where changes in f_{dep} were allowed. For modest changes ($r_{inf} = 0.02-0.04$ pc), the overall fits were not much worse. As found by Choi et al. (1995), the CS favored $r_{inf} = 0.03$ pc, while H₂CO favored smaller r_{inf} . For factor of 3 changes, the fit degraded substantially (Fig. 9). For $r_{inf} = 0.01$ pc, optically thick lines were too narrow, and the two peaks were nearly equal in strength, unlike the observations. For $r_{inf} = 0.09$ pc, those lines were too wide and the blue/red ratio was too large. There was also a greater conflict between the requirements of optically thick and optically thin lines; if the abundance was increased to match the latter, the former became

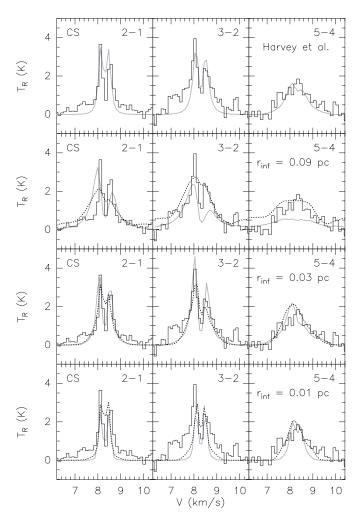


FIG. 9.—Observed CS lines from Zhou et al. (1993), plotted with the line profiles predicted by various models. The step function models are the gray lines, and the evolutionary models are the dotted lines. The bottom panel shows the best model with $r_{inf} = 0.01$ pc, the second panel from the bottom shows the best model with $r_{inf} = 0.03$ pc (same as Fig. 1), the third panel from the bottom shows the best model with $r_{inf} = 0.09$ pc, and the top panel shows the best model with the $r_{inf} = 0.03$ pc, but with densities enhanced by a factor of 5 everywhere, as favored by Harvey et al. (2001).

too strong. Within the constraints on abundances that we imposed, infall radii different by a factor of 3 would be strongly ruled out. The mean absolute deviations over *all* species ($\langle AD \rangle$) for these different models are listed in Table 7.

The constraints on the infall radius from the molecular line observations are inconsistent with those found by modeling the continuum emission (Shirley et al. 2002). The predicted intensity profiles of the model from Choi et al. (1995) were too flat to match the observations at 850 and 450 μ m (see Fig. 6 and Table 3 of Shirley et al. 2002). To make an inside-out collapse

TABLE 7 VARIATIONS IN THE PHYSICAL MODEL

$r_{ m inf}$	Density Factor	$\langle AD\rangle^a$	Chemical Model	$\langle AD\rangle^a$
0.01	1.0	4.62	6	4.93
0.03	1.0	3.75	6	4.15
0.09	1.0	5.38	6	4.95
0.03	5.0	4.02		

^a The mean value of AD for all species.

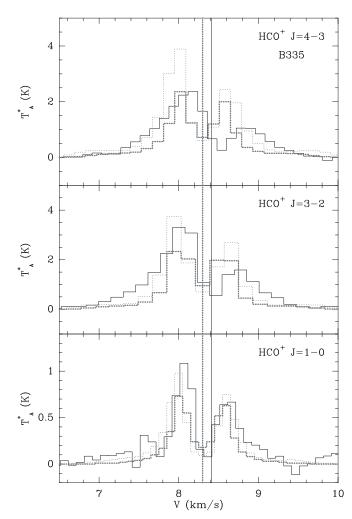


FIG. 10.—Observed HCO⁺ lines, plotted on an expanded scale, with the line profiles of the best step function model (*light dotted line*) and chemical model (*heavy dotted line*). The solid vertical line is at 8.41 km s⁻¹, the average velocity of the dip, while the dotted vertical line is at 8.30 km s⁻¹, the mean velocity for optically thin lines. The shift of the dip velocity to higher velocities seen in the observations is not reproduced in the models.

model fit the data, Shirley et al. had to use a very small infall radius, r = 0.0048 pc, more than 6 times smaller than the infall radius that matches the line profiles. Our modeling confirms that this small infall radius cannot match the line profiles. This fundamental discrepancy between the models of the dust and molecular line emission is discussed further in § 6.

Harvey et al. (2001) found that an inside-out collapse model with $r_{inf} \sim 0.03$ pc fitted the extinction data well, but only if the density was increased everywhere by a factor of about 5. We tried this model; decreases in abundances by about an order of magnitude were required for most species to bring line strengths back to near observed values. We had to decrease the CS abundance within r_{dep} to match the data, but this change is not unreasonable. The average deviation is somewhat larger than the standard model, but not terrible. Without constraints on abundances, it is hard to rule out variations in the physical model of this magnitude. However, the shapes of the CS lines were not reproduced well (top panel in Fig. 9), with blue/red ratios clearly less than the observations.

Moving farther afield, one may consider other collapse models. In some sense, the opposite extreme to the Shu (1977) model is the Larson-Penston similarity solution (Larson 1969; Penston 1969). Line profiles from this model were generated by Zhou (1992) and found to be considerably wider than those observed in regions of low-mass star formation. More recently, Masunaga et al. (1998) have shown that radiation hydrodynamic (RHD) calculations of collapse are well approximated by a modified Larson-Penston model. This model produces lower infall velocities than the original Larson-Penston model, which decrease with radius. Masunaga & Inutsuka (2000) have simulated line profiles from the RHD models, finding blue profiles and smaller line widths, qualitatively consistent with those seen in low-mass cores. While these models may indeed have application in some regions, the line widths listed in Table 4 of their paper for models after formation of the central core are larger than those in B335 by factors of at least 2.

There are hints in the spectra of deviations from the Shu model, particularly in the shift of v_{dip} to higher velocity for lines of higher excitation. This shift can be see more clearly in Figure 10, where three lines of HCO⁺ are shown. The best step function model is also shown; it does not reproduce this shift. The dip is caused by absorption from low-excitation material. In the Shu model, the outer, static envelope is dominating this absorption. A model with inward motion in this outer layer might better reproduce this shift.

5.3. Self-consistent Chemical Models

The chemical models are constrained by assuming an entire evolutionary history for the core, as detailed by Lee et al. (2004). We consider only their standard model of the evolution of physical conditions and luminosity to define the physical conditions, including the dust temperature profile, at the time step for which $r_{inf} = 0.03$ pc. Compared to the standard model of Lee et al., we allowed adjustment of only three free parameters: the binding energy to the dust, set by the assumed nature of the dust surface; the initial abundance of elemental sulfur; and the cosmic-ray ionization rate. The different models are summarized in Table 8.

First, binding energies of molecules onto three different dust grain surfaces were checked. For this comparison, the initial elemental abundances and the cosmic-ray ionization rate were the same as those in the standard model of Lee et al. (2004). For the CS lines, the binding energy onto a CO-dominant grain mantle works the best, and the value of $\langle AD \rangle$ is slightly better than for SiO₂. However, the low binding energy of molecules onto the CO mantle leads to less freezeout of CO, and, in turn, N₂H⁺ is destroyed by abundant CO in the gas phase. As a result, simulated CO isotopologue lines are too strong, and simulated N₂H⁺ lines are too weak compared to the observations. Attempts to improve the fit by reducing the initial abundance of carbon make the fit to CS worse while still not making the models fit CO and N₂H⁺ profiles.

TABLE 8 Chemical Models

			Х	ζ	
Model	Туре	Dust Surface	(S)	(s ⁻¹)	$\langle AD \rangle^a$
Model 1	Step				3.75
Model 2	Chemical	SiO_2	$4 imes 10^{-8}$	3.0×10^{-17}	5.05
Model 3	Chemical	CO	$4 imes 10^{-8}$	$3.0 imes 10^{-17}$	4.84
Model 4	Chemical	H_2O	$4 imes 10^{-8}$	$3.0 imes 10^{-17}$	5.89
Model 5	Chemical	SiO ₂	2×10^{-7}	3.0×10^{-17}	4.25
Model 6	Chemical	SiO ₂	2×10^{-7}	$6.0 imes10^{-17}$	4.15
Model 7	Chemical	SiO_2	2×10^{-7}	1.5×10^{-16}	4.23

^a The mean value of AD for all species.

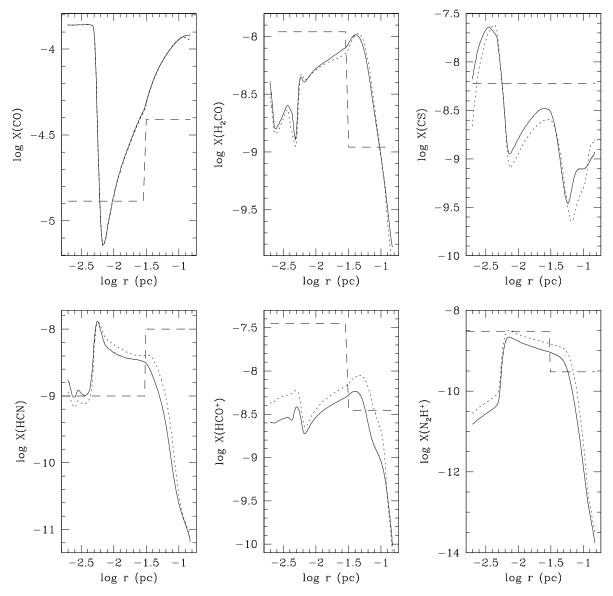


Fig. 11.—Abundance profiles. The dashed line shows the step function abundances, and the solid and dotted lines represent the abundances calculated from the chemical evolution model of Lee et al. (2004) in the time step for $r_{inf} = 0.03$ pc. In both chemical models, we used an initial sulfur abundance greater than the standard value in Lee et al. (2004) by a factor of 5. In the chemical model with dotted lines, the cosmic-ray ionization rate is 2 times greater than the standard value to give the best fit to observed line profiles (model 6 in Table 8). The solid line is model 5, which uses the standard value for the ionization rate.

At the other extreme, CO and CS are frozen out significantly onto H_2O -dominant grain mantles to produce much weaker lines than the observations indicate. HCO^+ , which is a daughter molecule of CO, is also depleted from the gas phase. Although N_2H^+ is less likely to be destroyed by CO, even nitrogen molecules are easily frozen out on the H_2O mantle, decreasing the N_2H^+ abundance. In addition, HCN increases by 3 orders of magnitude at radii smaller than 0.004 pc, compared to the abundance in the outer regions, giving a very broad line wing, which is not present in the observed lines. Except for weaker CS lines, the lines simulated with abundance profiles calculated for bare SiO₂ grain surfaces show much better fits to actual data than do those from other assumptions about grain surfaces.

We adopt the bare SiO_2 grain surface as our standard. In this model, the CO evaporation radius is about 0.006 pc. At radii less than this radius, almost all CO is desorbed from dust grain surfaces. Next, we varied the initial abundance of sulfur to improve the fit to the CS lines. An increase of the initial sulfur

abundance by a factor of 5 gives the best results with the SiO₂ grain surfaces. Other molecular lines do not vary much with the initial abundance of sulfur. The abundance profiles of this model are shown as solid lines in Figure 11. In all chemical models, the N₂H⁺ and HCO⁺ lines are weaker than the observed lines, so we tested various cosmic-ray ionization rates. A cosmic-ray ionization rate increased by a factor of 2 produced the best fit for N₂H⁺ and HCO⁺ lines. We increased the ionization rate in the energetics calculation for consistency. HCN lines become stronger with the cosmic-ray ionization rate, and $\langle AD \rangle$ becomes somewhat worse if we increase the ionization rate by a factor of 5. The abundances for the model with ionization enhanced by a factor of 2 are shown by the dotted lines in Figure 11.

The chemical models produce abundances with large (many orders of magnitude) variations with radius and quite complex radial structure. For explanations of these effects, see Lee et al. (2004). Note in particular the large decreases in abundance at large radii for most species caused by photodissociation. The large decrease in CO abundance over a wide range of radii reflects freezeout onto grain surfaces, and some other species follow this trend, but N_2H^+ behaves oppositely because CO destroys N_2H^+ . Likewise, most species show a peak at small radii, where CO evaporates, because those species also evaporate there, while N_2H^+ decreases when CO evaporates. The abundances for the step function model are also shown in Figure 11. In some cases, they are dramatically different.

The line profiles resulting from the best-fit chemical model are shown in Figures 1–6 as dotted lines. The average values of absolute deviation for the best chemical model are also listed in Table 6 for comparison to those from the step function models. In most cases, the values of AD are slightly worse, most notably for DCO^+ and H_2CO , but many are similar to those of the step function models. Compared to the best fit with step function abundances, the best fit with chemical abundances shows less deep absorption dips in the CS lines, weaker lines of the higher transitions in N₂H⁺ and H₂CO, and less blue asymmetry in HCO⁺ lines. In addition, the predicted lines of HCO⁺ isotopologues are weaker than in the step function models. To match the observations, the isotope ratios would need to be increased by factors of 3-5. The deuterium ratio for DCO⁺ 3-2 would also need to be increased by a factor of 5 to match the observed line. These discrepancies result from the fact that B335 has quite strong lines of rare isotopologues of HCO⁺. However, standard isotope ratios for C¹⁸O, ¹³CO, and C¹⁷O, or H₂CO and $H_2^{13}CO$, produce reasonably good matches to the observations. Chemical abundances predict still weaker H₂CO lines in highexcitation transitions than do step function abundances. As mentioned in \S 5.1, higher densities at small radii are necessary to account for the weak high-excitation H₂CO lines. Also, the N_2H^+ 3–2 line is relatively weaker than the 1–0 line when compared to the observed lines, again suggesting the presence of higher densities at small radii. HCO⁺ and HCN lines simulated with chemical abundances are narrower than the observed lines. These two molecules are abundant in outflowing gas. Therefore, the lines might be affected by the outflow, which is not considered in this work. The satellite hyperfine lines of HCN 1-0 are produced better with the abundance profile from the chemical model than with a step function. However, even chemical abundances cannot predict the satellite hyperfine lines of the HCN 3-2 as well as the absence of the red component of the main group. This result suggests the existence of a region with very high HCN abundance. The chemical models also do not reproduce the shift of v_{dip} with increasing J seen in HCO⁺ (Fig. 10).

We also tested different time steps in the same luminosity model. In time steps earlier than the time step for $r_{inf} = 0.03$ pc, the model core has higher densities at small radii, and the total internal luminosity is smaller than observed for B335, and vice versa for $r_{inf} > 0.03$ pc. According to the test, H₂CO and N₂H⁺ lines are fitted much better with the chemical abundances in an earlier time step for $r_{inf} = 0.015$ pc. The satellite hyperfine lines of the HCN 3-2 are also well fitted, while its main group is too strong. Higher densities at small radii cause these results. In addition, at this time, the CO evaporation radius is about 0.004 pc, so less CO evaporates compared to the time step for $r_{inf} =$ 0.03 pc. As a result, N_2H^+ is more abundant. However, at this time, the infall velocities are not big enough to produce the degree of the blue asymmetry in CS lines. The CS lines predicted by models with 3 times smaller and larger r_{inf} are also shown in Figure 9, and the values of $\langle AD \rangle$ are given in Table 7; unlike the step function models, the luminosity is different for these other values of r_{inf} , because the luminosity increases with

time. Nonetheless, similar problems to those encountered in the step function models appear at earlier and later times.

6. DISCUSSION

Both step function models and evolutionary chemical models do a reasonable job of fitting most of the data. Models with constant abundances are not adequate for fitting most observations. In addition, the evolutionary chemical models clearly indicate that abundances vary by orders of magnitude as a result of freezeout and desorption (Lee et al. 2004). These conclusions are similar to those of Jørgensen et al. (2004), who find that constant abundance models are unsatisfactory and that a drop function works better. The drop function, although simpler, is similar in shape to the abundance profile of CO in Figure 11. It allows a region of lower abundance at intermediate radii and a return to high abundances at small radii. The drop function cannot, of course, capture the full complexity of the abundance profiles in Figure 11.

Both models fit the CS lines despite the very different radial dependences of the CS abundance. The H₂CO lines are better fitted by the step function models, primarily because they allow a high abundance over a substantial range of radii, where the density is high, thus providing stronger lines of high-excitation transitions. Similarly, the chemical models, even with enhanced ionization, cannot produce sufficient HCO⁺ to match the observations of rare isotopologues. Interestingly, the chemical model can match the peculiar $J = 3 \rightarrow 2$ line profile.

In comparing models, one should bear in mind that the step function models were allowed 15 free parameters, while the chemical models enjoyed only three, and those were restricted by prior knowledge. In fact, the step function abundances that fit best are very inconsistent with what we know of chemistry. The CO abundance is depleted inside r_{inf} , while the HCO⁺ and H₂CO abundances increase; this combination is highly unlikely, especially for HCO⁺, which is a direct product of CO. The very high abundance of HCO⁺ inside r_{inf} invoked by the step function models to match the strong lines of rare isotopologues is very hard to produce in any chemical model.

The evolutionary model does not include grain surface reactions, so it does not predict an ortho-para ratio for H_2CO ; we assumed a ratio of 1.7. The most likely route for modifications to the chemical models is to add grain surface reactions, but this step will effectively add many free parameters to the chemical model, because rates for surface reactions are poorly known.

On the whole, it is in fact rather remarkable that the line profiles from the self-consistent chemical models are as close as they are to the observations. With variations in abundances of many orders of magnitude with radius, they could easily have failed to match observations by orders of magnitude. In addition, B335 is only one source, and it has a rather rich spectrum for a low-mass core, including unusually strong lines of HC¹⁸O⁺. Of course, this feature makes B335 an attractive source to test theories, but it also may mean that it is atypical.

What can explain the remaining differences between the models and the data? First, the Shu (1977) model of the infall may not be correct. There is a hint in this direction in the fact that the models do not reproduce the shift of v_{dip} to the red of v_{LSR} for optically thin lines (Fig. 10). This result suggests that the outer envelope is not stationary, as in the Shu solution, but is also moving inward. Second, the outflow is not considered in these models, but it will affect abundances and line profiles. To include the outflow, we must move beyond one-dimensional models. Third, the chemical models may not yet include enough

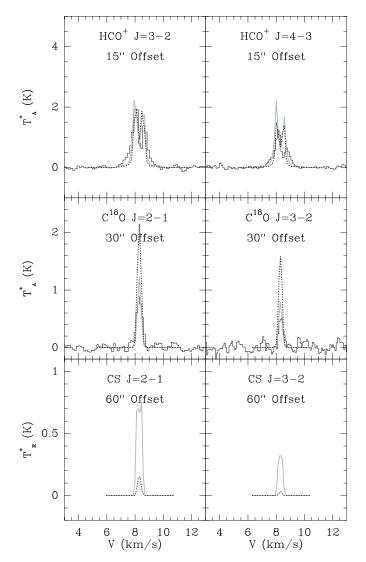


FIG. 12.—Off-center line profiles. The gray solid (step functions) and dotted (chemical abundances) lines are predictions of the radiative transfer model. For HCO^+ and $C^{18}O$, we show observed line profiles as histograms. The observations of the CS lines can be seen in Zhou et al. (1993).

processes for desorption of gas from grain mantles. These could increase the abundances at intermediate radii.

6.1. Off-Center Spectra

We have focused here on spectra toward the center of B335. The large differences between the empirical and evolutionary models in the abundances of some species at larger radii suggest that spectra off the center of B335 may help in testing chemical models. Figure 12 shows a sample of spectra at positions off the center predicted by the best-fit empirical and evolutionary models. For HCO^+ and $C^{18}O$, we show observed spectra at these positions, produced by averaging spectra displaced in all directions with that separation in our maps. We also show predictions of CS spectra displaced by 60''; we no longer have the observed spectra at those positions, but they are presented by Zhou et al. (1993). For the HCO⁺ $J = 4 \rightarrow 3$ line, the evolutionary model gives a weaker line, closer to the observations, than the empirical model at 15" offset. Conversely, the evolutionary model produces stronger lines of C¹⁸O at 30" offset than either the empirical model or the data. The differences are most dramatic for CS lines 60" away from the center. The strong decrease in CS abundance in the evolutionary models, seen in Figure 11, produces lines that are much weaker than those of the empirical model. Zhou et al. (1993) detected lines stronger than either prediction, but the noise was fairly high. Improved maps of CS with good spatial resolution would be very helpful in further constraining models. The decrease in CS abundance at large radii is quite sensitive to the external extinction (see Fig. 13 of Lee et al. 2004). Models with higher values of external extinction, but with all other parameters unchanged, do greatly increase the strength of CS lines at off-center positions. Maps of appropriate lines can help to constrain the environment of the core, while observations with much higher resolution can test the predictions of abundance peaks at small radii (Lee et al. 2005).

6.2. What about the Dust?

We noted above that the molecular line emission and the dust emission lead to inconsistent conclusions about the density distribution. To summarize, the dust emission data are consistent with an inside-out collapse model only if the infall radius is much smaller than the molecular line data indicate (Shirley et al. 2002). Attempts to adjust abundances to make the line profiles predicted for the small infall radius match the observations failed; the predicted line profiles are simply too narrow at the early times implied by the small infall radius.

The other possibility is that the model based on the dust emission is wrong. While Shirley et al. (2002) performed an extensive set of tests, there are two possibilities that remain to be considered: changes in the dust opacity as a function of radius and contributions to the dust emission from a disk. Both of these would work by adding flux at small radii, steepening the predicted radial intensity profile. For example, Young et al. (2003) found that one could overestimate p, the best-fit exponent in a power-law model, by up to 0.5 if the contribution of a disk was ignored. This difference could change the best-fit value of p = 1.8 to something more compatible with the inner part of an inside-out collapse.

In fact, Harvey et al. (2003) have found evidence for a disk in B335 and modeled multiconfiguration data from the IRAM Plateau de Bure Interferometer with an envelope-disk combination. They find a good fit with a disk producing a flux of 21 mJy at 1.2 mm and an envelope with a broken power law: $n = 3.3 \times 10^4 (r/r_b)^{-1.5}$ for $r < r_b$ and $n = 3.3 \times 10^4 (r/r_b)^{-2.0}$ for $r > r_b$. The best-fit r_b is 0.032 pc, essentially the same as our best fit for the infall radius, and the two broken power laws agree with the inside-out model for $r > r_{inf}$ and with the asymptotic behavior of inside-out collapse at small radii. However, the density just inside the infall radius has a slower dependence on r in the inside-out collapse solution; Harvey et al. (2003) note that this theoretical n(r) does not fit their data well.

We have scaled up the flux of the disk in the Harvey et al. (2003) model ($S_{\nu} \propto \nu^3$) and modeled the 850 and 450 μ m data from Shirley et al. (2000) with an inside-out collapse model and a point source with the flux of the disk. The intensity profiles are not well fitted unless the point source is 5–10 times stronger than in the Harvey et al. model. Models with disks and radial variations in dust opacity are needed to resolve these questions, but they are outside the scope of this paper.

We conclude that the issues of disks (or more generally, compact structure) and radial variations in dust opacity introduce enough uncertainty that it is not yet possible to close the loop fully on the modeling of molecular lines and dust continuum.

7. CONCLUSIONS

We have assembled data on a large number of molecular lines toward B335 and compared those lines to predictions of models. The models are of two primary types: those with step function chemical abundances and those with chemical abundances resulting from an evolutionary calculation (Lee et al. 2004). In both cases, the temperatures of dust and gas are calculated from the luminosity of the protostar and the density distribution under study. In both cases, the underlying physical model is the inside-out collapse model of Shu (1977).

Both step function and evolutionary chemical abundances can fit most of the data, with some residual puzzles remaining. Both favor an infall radius around 0.03 pc, as was found from earlier modeling by Zhou et al. (1993) and Choi et al. (1995). Models with the same infall radius, but with densities enhanced by a factor of 5, as suggested by Harvey et al. (2001), do not fit as well, but they cannot be ruled out. Models with much smaller infall radii, as favored by the dust continuum modeling (Shirley et al. 2002), do not fit the data well at all. Resolving this discrepancy between the conclusions of modeling dust and gas may require modifications to the dust models, including incorporation of compact sources and changes in the dust opacities with radius.

The standard chemical evolution model shows huge variations in abundance as a function of radius (Fig. 11 and Lee et al. 2004), but still comes reasonably close to matching the observations. This is quite a remarkable fact. Changes to the initial sulfur abundance and cosmic-ray ionization rate improve the fit to the lines, but these may simply be compensating for remaining unknowns in the chemistry. Rawlings & Yates (2001) have highlighted the extreme sensitivity of some abundances and line profiles to free parameters, especially the early evolutionary history. Accordingly, the reader is cautioned that other combinations of history, dynamics, and chemical parameters that we have not explored might also produce reasonable fits to the data. The important point is that chemical models now come close enough that one can begin to look in detail at what might improve the match. However, this should be done after more than one source is compared to the models, as there will be variations in conditions and evolutionary history from source to source.

In addition, the standard physical model of inside-out collapse does a remarkably good job of predicting the line profiles. However, there are clear hints of dynamics beyond the standard model in the shift of the velocity of the self-absorption dip to higher velocities in lines requiring higher excitation. Models with envelopes moving inward may be more successful in reproducing these features. Spectra at positions away from the center can constrain other parameters, especially the surrounding radiation environment. However, future work should also account for the nonsphericity and other effects of the outflow in this source. Further observations with better spatial resolution will be important to constrain these models, as the line profiles become more diagnostic of both dynamics (Choi 2002) and chemistry (Lee et al. 2004).

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