# S EQUULEI: A LOW MASS RATIO ALGOL-TYPE ECLIPSING BINARY AT THE ACTIVE PHASE OF MASS TRANSFER 

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#### Abstract

Orbital period change of a low mass ratio $(q=0.13)$ Algol-type eclipsing binary, S Equulei, is presented based on the analysis of its century-long times of light minimum. Alternate period changes are discovered to superimpose on a rather rapid period increase with rate of $d P / d t=+1.27 \times 10^{-6}$ days $\mathrm{yr}^{-1}$. The alternate period changes can be explained either by the variation in the gravitational quadruple momentum via the cyclic magnetic activity of the G-type secondary or by the light-time effect via the presence of a third body. Since the third-body assumption is in good agreement with Zola's photometric solution, S Equ may be a truly triple system. The third body is rotating in an eccentric orbit ( $e^{\prime}=0.37$ ) with an orbital inclination of $i^{\prime}=16^{\circ}$, which is rather smaller than that of the eclipsing binary system $\left(i=88^{\circ} 3\right)$. This indicates that the third body may be captured by the eclipsing pair. New accurate photometric and spectroscopic data over the next decade are very important to verify this conclusion. The rapid period increase suggests that S Equ is a low mass ratio Algol-type binary system in an active phase of mass exchange. To satisfy such a period increase, a conservative mass transfer from the less massive to the more massive components would be of the order $d m / d t=4.94 \times 10^{-8} M_{\odot} \mathrm{yr}^{-1}$. Subject headings: binaries: close — binaries: eclipsing — stars: evolution — stars: individual (S Equulei) — stars: variables: other


## 1. INTRODUCTION

S Equ (BD $4^{\circ} 4584=$ HD 199454) was discovered to be a variable by Mackie in 1916 on Harvard patrol plates. Subsequently, the Algol-type light variation of the binary star was found by O'Reilly (Plavec 1966). Photoelectric observations of the eclipsing binary were obtained by Plavec (1966), Catalano \& Rodono (1968), and more recently by Zola (1992). A detailed analysis of the spectroscopic data of S Equ observed at Victoria Observatory was carried out by Plavec (1966), who classified the two components as B9.5+F7 IV and later as B7 V+G8 III (Plavec 1983). Combining the spectroscopic elements with the photometric solutions he obtained the absolute parameters of the system. His investigation showed that S Equ is an Algol-type eclipsing binary system with an extremely low mass ratio ( $q \sim 0.11-0.15$ ). The photoelectric light curve published by Catalano \& Rodono (1968) was analyzed by Piotrowski et al. (1974) and by Cester et al. (1979), and absolute dimensions were also determined. By the analysis of his photoelectric light curves in $U, B$, and $V$ with the Wilson-Devinney method, a significant third light in the system was found by Zola (1992). The extremely low mass ratio and the presence of a third body in the system both made $S$ Equ a very interesting system to study.

## 2. $O-C$ CURVE FOR S EQUULEI

S Equ is a relatively bright Algol-type variable ( 8.2 mag ) with a rather deep primary minimum (about 2 mag), which made it a suitable object for times of light minimum even

[^0]with visual or photographic methods. After its discovery, many times of light minimum were published. The period variation of the binary star was first noticed by Cesevic (1958), who suggested that the change may have occurred suddenly sometime in the early thirties. Plavec (1966) collected all timings published before 1966 and presented an $O-C$ diagram. It was showed that the period was variable but properties of the period change were not clear. After Plavec's study, 36 yr have elapsed. Many times of light minimum have been compiled at the Eclipsing Binaries Minima Database (EBMD), ${ }^{3}$ and recently one timing observed by Kohl and two times of light minimum observed by Meyer and by Lange have been published in BBSAG No. 122 and in BAV Mitteilungen No. 143. A detailed period investigation of the systems is absolutely required.

All available times of light minimum are shown in Table 1. Those listed in the second and the seventh columns of the table are the observed methods where " vp" refers to visual or photographic observations, "pe" to photoelectric, and " CCD" to charge-coupling device data. The $(O-C)_{1}$ values of these timings based on the following linear ephemeris (Plavec 1964),

$$
\begin{equation*}
\text { Min. } \mathrm{I}=\text { HJD } 2,437,968.345+3.4360726 \times E \tag{1}
\end{equation*}
$$

are computed and are listed in Table 1. The first time of light minimum, HJD 2,410,002.337, published by Cannon (1916), is not listed in the table and not used for this present period study, since the time intervals between the minimum and the others are very large and its accuracy is uncertain (Plavec 1966). During the computation, some eclipse times with the same epoch have been averaged. Three times of minimum light, HJD 2,442,138.420, 2,442,524.552, and $2,447,053.368$, are discarded since their $(O-C)_{1}$ values show large deviations compared with the general trend

[^1]TABLE 1
$O-C$ Data for S EQUULEI

| HJD + 2400000 | Meth. | $E$ | $\begin{gathered} (O-C)_{1} \\ (\text { days }) \end{gathered}$ | $\begin{gathered} (\mathrm{O}-\mathrm{C})_{2} \\ (\text { days }) \end{gathered}$ | HJD + 2400000 | Meth. | $E$ | $\begin{gathered} (O-C)_{1} \\ (\text { days }) \end{gathered}$ | $\begin{gathered} (\mathrm{O}-\mathrm{C})_{2} \\ (\text { days }) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 23334.165........... | vp | -4259 | $+0.053$ | +0.003 | 43689.423........... | vp | 1665 | $+0.017$ | -0.010 |
| 23990.446........... | vp | -4068 | +0.044 | +0.001 | 43713.484 . | vp | 1672 | $+0.026$ | -0.002 |
| 24100.403.......... | vp | -4036 | +0.047 | +0.005 | 43723.789.......... | vp | 1675 | $+0.022$ | -0.005 |
| 24282.514........... | vp | -3983 | +0.046 | +0.006 | 43830.307.......... | vp | 1706 | $+0.022$ | -0.007 |
| 24385.583.......... | vp | -3953 | +0.033 | -0.006 | 44122.378 . | vp | 1791 | $+0.027$ | -0.005 |
| 24430.260........... | vp | -3940 | +0.041 | +0.003 | 44146.418 . | vp | 1798 | $+0.015$ | -0.017 |
| 24746.362 . | vp | -3848 | +0.024 | -0.011 | 44153.293 . | vp | 1800 | $+0.017$ | -0.015 |
| 25093.402 . | vp | -3747 | +0.021 | -0.011 | 44208.281 . | vp | 1816 | $+0.028$ | -0.004 |
| 25474.800........... | vp | -3636 | +0.015 | -0.013 | 44438.487 . | vp | 1883 | $+0.017$ | -0.017 |
| 25708.459.......... | vp | -3568 | $+0.021$ | -0.005 | 44448.805.......... | vp | 1886 | $+0.027$ | -0.008 |
| 25866.512........... | vp | -3522 | +0.015 | -0.010 | 44469.418.......... | vp | 1892 | $+0.024$ | -0.011 |
| 26581.208........... | vp | -3514 | +0.008 | -0.016 | 44472.853. | vp | 1893 | $+0.023$ | -0.012 |
| 27409.307. | vp | -3073 | $+0.013$ | +0.001 | 44479.730 . | vp | 1895 | $+0.027$ | -0.008 |
| 27670.440........... | vp | -2997 | +0.005 | -0.005 | 44524.393. | vp | 1908 | $+0.022$ | -0.014 |
| 27756.331........... | vp | -2972 | -0.006 | -0.016 | 44555.322 . | vp | 1917 | $+0.026$ | -0.010 |
| 27962.514........... | vp | -2912 | +0.012 | +0.004 | 44586.248. | vp | 1926 | $+0.027$ | -0.009 |
| 28072.449.. | vp | -2880 | -0.007 | -0.015 | 44847.387. | vp | 2002 | $+0.025$ | -0.014 |
| 32807.360........... | vp | -1502 | -0.004 | +0.009 | 44878.313. | vp | 2011 | $+0.026$ | -0.013 |
| 33178.465.......... | vp | -1394 | +0.005 | +0.018 | 44902.367 . | vp | 2018 | $+0.028$ | -0.012 |
| 33539.241........... | vp | -1289 | -0.006 | +0.008 | 44933.293 . | vp | 2027 | $+0.029$ | -0.011 |
| 34226.447........... | vp | -1089 | -0.015 | -0.001 | 45077.615.. | vp | 2069 | $+0.036$ | -0.005 |
| 34604.432........... | vp | -979 | +0.002 | +0.016 | 45163.512 . | vp | 2094 | $+0.031$ | -0.011 |
| 36133.480. | vp | -534 | -0.002 | +0.011 | 45173.825. | vp | 2097 | $+0.036$ | -0.006 |
| 37188.3613......... | pe | -227 | +0.004 | $+0.0148$ | 45541.496........... | vp | 2204 | $+0.047$ | +0.001 |
| 37559.445.......... | vp | -119 | -0.007 | +0.003 | 45544.9246......... | pe | 2205 | +0.0395 | -0.0067 |
| 37559.456........... | vp | -119 | +0.004 | +0.014 | 45603.344........... | vp | 2222 | $+0.046$ | -0.001 |
| $37968.3438 . . . . . . .$. | pe | 0 | -0.001 | $+0.0075$ | 45905.726.......... | vp | 2310 | $+0.053$ | +0.003 |
| 38253.5397......... | pe | 83 | +0.001 | $+0.0085$ | 45929.775........... | vp | 2317 | $+0.050$ | -0.001 |
| 38284.4641 ......... | pe | 92 | 0.000 | +0.0074 | 45960.699........... | vp | 2326 | $+0.049$ | -0.002 |
| 38315.377........... | vp | 101 | -0.011 | -0.004 | 46266.515.......... | vp | 2415 | $+0.055$ | 0.000 |
| 38315.3877......... | pe | 101 | -0.001 | +0.0062 | 46290.558........... | vp | 2422 | $+0.045$ | -0.010 |
| 38607.4530 ......... | pe | 186 | -0.001 | $+0.0051$ | 46321.487.......... | vp | 2431 | $+0.050$ | -0.006 |
| 39009.476........... | vp | 303 | +0.001 | +0.005 | $46328.3635 \ldots \ldots . .$. | pe | 2433 | +0.0539 | -0.0013 |
| 39394.304........... | vp | 415 | -0.011 | -0.008 | 46328.366... | vp | 2433 | $+0.056$ | +0.001 |
| 39710.428........... | vp | 507 | -0.006 | -0.005 | 46352.415. | vp | 2440 | $+0.053$ | -0.003 |
| 40088.401 ........... | vp | 617 | -0.001 | -0.002 | 46359.286........... | vp | 2442 | $+0.052$ | -0.004 |
| $40150.249 \ldots . . . . . .$. | vp | 635 | -0.002 | -0.003 | 46644.490........... | vp | 2525 | $+0.062$ | +0.003 |
| 40806.538.......... | vp | 826 | -0.003 | -0.008 | 47087.741 . | vp | 2654 | $+0.059$ | -0.005 |
| 40844.333........... | vp | 837 | -0.005 | -0.010 | 47431.359.......... | vp | 2754 | $+0.070$ | +0.001 |
| 40930.239.......... | vp | 862 | -0.001 | -0.007 | 47778.410.......... | vp | 2855 | $+0.078$ | +0.004 |
| 41222.3021 ......... | pe | 947 | -0.0037 | -0.0116 | 48094.538.......... | vp | 2947 | $+0.087$ | +0.009 |
| 41246.353........... | vp | 954 | -0.005 | -0.013 | 48187.316........... | vp | 2974 | +0.091 | +0.012 |
| 41507.492........... | vp | 1030 | -0.008 | -0.018 | 48448.460 . | vp | 3050 | $+0.094$ | +0.011 |
| 41569.344. | vp | 1048 | -0.005 | -0.015 | 48479.3804......... | pe | 3059 | $+0.0893$ | $+0.0063$ |
| 41593.402.......... | vp | 1055 | 0.000 | -0.010 | 48503.440 . | vp | 3066 | $+0.096$ | $+0.013$ |
| 41830.497........... | vp | 1124 | +0.006 | -0.006 | 48922.639........... | vp | 3188 | $+0.095$ | +0.005 |
| 41916.404........... | vp | 1149 | $+0.012$ | -0.001 | 49214.711........... | vp | 3273 | $+0.100$ | +0.007 |
| 42201.587........... | vp | 1232 | +0.001 | -0.014 | 49228.457........... | vp | 3277 | $+0.102$ | +0.008 |
| 42318.418........... | vp | 1266 | $+0.005$ | +0.009 | 49929.4221 ......... | pe | 3481 | +0.1084 | +0.0040 |
| 42524.592.......... | vp | 1326 | $+0.015$ | -0.003 | 50262.727.......... | CCD | 3578 | +0.1142 | +0.0045 |
| 42672.334........... | vp | 1369 | $+0.006$ | -0.013 | 50276.480........... | vp | 3582 | $+0.123$ | $+0.013$ |
| 42727.313........... | vp | 1385 | $+0.007$ | -0.012 | 50341.764........... | vp | 3601 | $+0.122$ | $+0.011$ |
| 42957.522........... | vp | 1452 | 0.000 | -0.021 | 50719.736.......... | vp | 3711 | $+0.126$ | $+0.009$ |
| 42988.463........... | vp | 1461 | +0.016 | -0.005 | 50726.605........... | vp | 3713 | $+0.122$ | $+0.005$ |
| 43012.509........... | vp | 1468 | +0.009 | -0.012 | 51097.715.......... | vp | 3821 | $+0.137$ | +0.014 |
| 43043.441........... | vp | 1477 | +0.017 | -0.005 | 51434.452.......... | vp | 3919 | $+0.139$ | $+0.010$ |
| 43311.445........... | vp | 1555 | $+0.007$ | -0.017 | 51757.428.......... | vp | 4013 | $+0.124$ | -0.011 |
| 43483.253........... | vp | 1605 | $+0.012$ | -0.014 | 51812.409.......... | vp | 4029 | $+0.128$ | -0.008 |

formed by other data. The corresponding $(O-C)_{1}$ diagram is displayed in Figure 1, which indicates that the period change of S Equ is very complex. As shown in the figure, the general $(O-C)_{1}$ trend can be described by an upward para-
bolic curve, suggesting a secular period increase in the system. With weights 1 to the VP data and 8 to the photoelectric or CCD observations, a weighted leastsquares solution leads to the following quadratic ephemeris


Fig. 1.- $(O-C)_{1}$ plot for S Equ with respect to the ephemeris of Plavec (eq. [1]). The solid line represents the best fit parabola to the data (eq. [2]). Solid dots refer to photoelectric or CCD and circles to visual or photographic data.
with the mean error for each term:
Min. $\mathrm{I}=$ HJD 2, 437, $968.3365(13)+3.43608425(37)$

$$
\begin{equation*}
\times E+5.97(17) \times 10^{-9} \times E^{2}, \tag{2}
\end{equation*}
$$

which can give a good fit to the general $(O-C)_{1}$ trend (Fig. 1 , solid line).

## 3. DISCUSSION OF THE $O-C$ CURVE OF S EQUULEI

The long-term general trend in Figure 1 indicates an increasing period. With the quadratic term of equation (2), a period increase rate, $d P / d t=+1.27 \times 10^{-6}$ days $\mathrm{yr}^{-1}$, is obtained. This trend can be interpreted as a mass transfer from the less massive to the more massive components. This is in agreement with the semidetached configuration of the binary system. Assuming that the period increase is due to a conservative mass transfer (with no magnetic effect), then putting $M_{1}=2.21 M_{\odot}$ and $M_{1}=0.30 M_{\odot}$ given by Zola (1992) to the following equation (Kwee \& van Woerden 1958),

$$
\begin{equation*}
\Delta P / P=3\left(M_{1} / M_{2}-1\right) \Delta M_{1} / M_{1}, \tag{3}
\end{equation*}
$$

a mass transfer rate is estimated to be $d m / d t=4.94 \times 10^{-8}$ $M_{\odot} \mathrm{yr}^{-1}$.

A careful examination of the $(O-C)_{1}$ curve in Figure 1 shows that S Equ possesses an alternating period change superimposed on the secular increase. This behavior is more easily seen in Figure 2 where the residuals computed from the parabolic fit are displayed. The corresponding $(\mathrm{O}-\mathrm{C})_{2}$ residuals from the quadratic ephemeris are also listed in Table 1. Since the $(O-C)_{2}$ residuals of two times of light minimum, given in BAV Mitteilungen No. 143, shows large scatters when compared with the general trend formed by other data, the two values are not displayed in Figure 2 and are not used for the following period analysis.

The $O-C$ residuals in Figure 2 may suggest a cyclic oscillation in the orbital period which may result from the orbital motion of the system around the center of mass of an assumed triple system. This model has been used to explain the cyclic period changes in Algols and other short-period binaries by Frieboes-Conde \& Herczeg (1973), Chambliss (1992), and recently by Borkovits \& Hegedüs (1996). The not strictly sinelike change of the $(\mathrm{O}-\mathrm{C})_{2}$ curve indicates that the third body is moving in an elliptical orbit. However, the nearly sinusoidal shape of the $(\mathrm{O}-\mathrm{C})_{2}$ curve indicates that the orbital eccentricity of the eclipsing pair around the common center of the gravity of the three bodies is very small. The following formula,

$$
\begin{equation*}
(O-C)_{2}=a_{0}+\sum_{i=1}^{2}\left[a_{i} \cos (i \omega E)+b_{i} \sin (i \omega E)\right] \tag{4}
\end{equation*}
$$

can be used to express those $(O-C)_{2}$ values where $a_{1,2}$ and $b_{1,2}$ are the Fourier coefficients and $\omega$ is the fundamental frequency. By various numerical trials with different value of $\omega$, a best solution of equation (4) was determined: $a_{0}=0.0002(4), \quad a_{1}=0.0060(9), \quad b_{1}=-0.0090(8), \quad a_{2}=$ $0.0021(11), b_{2}=0.0002(8)$. Putting the ephemeris period $P_{e}=3.4360726$ to the formulae,

$$
\begin{equation*}
\omega=360^{\circ} P_{e} / T \tag{5}
\end{equation*}
$$

the period of the eclipsing binary around the center of mass of the triple system was derived to be $T=42.8 \mathrm{yr}$.

The orbital parameters of the third body were derived from the formula given by $\operatorname{Kopal}(1959$, p. 112),

$$
\begin{gather*}
a_{12}^{\prime} \sin i^{\prime}=c \sqrt{a_{1}^{2}+b_{1}^{2}},  \tag{6}\\
e^{\prime}=2 \sqrt{\frac{a_{2}^{2}+b_{2}^{2}}{a_{1}^{2}+b_{1}^{2}}},  \tag{7}\\
\omega^{\prime}=\arctan \frac{\left(b_{1}^{2}-a_{1}^{2}\right) b_{2}+2 a_{1} a_{2} b_{1}}{\left(a_{1}^{2}-b_{1}^{2}\right) a_{2}+2 a_{1} b_{1} b_{2}},  \tag{8}\\
\tau^{\prime}=t_{0}-\frac{T}{2 \pi} \arctan \frac{a_{1} b_{2}-b_{1} a_{2}}{a_{1} a_{2}+b_{1} b_{2}}, \tag{9}
\end{gather*}
$$



Fig. 2.-The $(\mathrm{O}-\mathrm{C})_{2}$ residuals in days for S Equ after subtracting of the best-fit parabola given in eq. (2). Solid line represents the theoretical solution of an assumed third body.
where $c$ is the speed of light, $a_{12}^{\prime}$ is the semimajor axis of the eclipsing binary around the common center of the gravity of the triple system, $i^{\prime}, e^{\prime}, w^{\prime}$, and $\tau^{\prime}$ are the usual orbital parameters of the third body. The results are $a_{12}^{\prime} \sin i^{\prime}=1.87(14)$ $\mathrm{AU}, e^{\prime}=0.39(20), w^{\prime}=62^{\circ}(11)$ and $\tau^{\prime}=2440649^{d}(923)$. Then using the values of the semiamplitude of $a_{12}^{\prime} \sin i^{\prime}=1.87 \mathrm{AU}$ and the period of $T=42.8 \mathrm{yr}$ together with the following equation,

$$
\begin{equation*}
f(m)=\frac{\left(M_{3} \sin i^{\prime}\right)^{3}}{\left(M_{1}+M_{2}+M_{3}\right)^{2}}=\frac{4 \pi^{2}}{G T^{2}} \times\left(a_{12}^{\prime} \sin i^{\prime}\right)^{3} \tag{10}
\end{equation*}
$$

the mass function for the additional body is determined to be $f(m)=3.59( \pm 0.83) \times 10^{-3} \quad M_{\odot}$. With the masses $M_{1}=2.21 M_{\odot}$ and $M_{2}=0.30 M_{\odot}$ given by Zola (1992), the values of the masses and the orbital radii of the third body for different orbital inclinations ( $i^{\prime}$ ) are calculated and are listed in Table 2. If the third body is coplanar to the orbit of the eclipsing pair (i.e., $i^{\prime}=88^{\circ} .3$ ), the mass and the orbital radius would be $m_{3}=0.31( \pm 0.03)$ and $a_{3}=15.4( \pm 1.7)$ AU, respectively. However, the $(O-C)_{2}$ values in Figure 2, especially those of VP data, show large scatters (up to 0.010 ), the properties of the period changes are not clear at present. In order to check whether the $O-C$ variation is strictly periodic or not, more times of light minimum are required.

Apart from the presence of the additional body, the oscillation of the orbital period of a close binary containing at least one late-type star is usually explained as a consequence of possible magnetic cycle in the active component. In an important study of Hall (1989) comparing RS CVn to Algol binaries, he found a correlation between the alternating period change and the spectral type of the secondary, which has recently reproduced by Zavala et al. (2002). When the spectral type of the secondary is earlier than F5, alternating period change is never been found. Hall explained this finding as strong evidence of magnetic activity cycle in the secondary. This theory was first suggested by Matese \& Whitmire (1983) and developed by Applegate \& Patterson (1987) and Warner (1988), who attempted to interpret the $O-C$ patterns by assuming deformations of the star away from hydrostatic equilibrium via magnetic pressure or tidal.

TABLE 2
The Values of the Masses and the Orbital Radii for the Third Body in S Equulei

| Parameters | Values | Units |
| :---: | :---: | :--- |
| $\sqrt{a_{1}^{2}+b_{1}^{2}} \ldots \ldots \ldots \ldots \ldots$. | $0.0108( \pm 0.0008)$ | days |
| $T \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$. | $42.8($ assumed $)$ | yr |
| $e^{\prime} \ldots \ldots \ldots \ldots \ldots \ldots \ldots \ldots$. | $0.39( \pm 0.20)$ | No. |
| $a_{12}^{\prime} \sin i^{\prime} \ldots \ldots \ldots \ldots \ldots$. | $1.87( \pm 0.14)$ | A.U. |
| $f(m) \ldots \ldots \ldots \ldots \ldots \ldots$. | $3.59( \pm 0.83) \times 10^{-3}$ | $M_{\odot}$ |
| $m_{3}\left(i^{\prime}=90^{\circ}\right) \ldots \ldots \ldots .$. | $0.31( \pm 0.02)$ | $M_{\odot}$ |
| $m_{3}\left(i^{\prime}=70^{\circ}\right) \ldots \ldots \ldots \ldots$ | $0.33( \pm 0.03)$ | $M_{\odot}$ |
| $m_{3}\left(i^{\prime}=50^{\circ}\right) \ldots \ldots \ldots \ldots$ | $0.41( \pm 0.03)$ | $M_{\odot}$ |
| $m_{3}\left(i^{\prime}=30^{\circ}\right) \ldots \ldots \ldots \ldots$ | $0.66( \pm 0.06)$ | $M_{\odot}$ |
| $m_{3}\left(i^{\prime}=10^{\circ}\right) \ldots \ldots \ldots \ldots$. | $2.62( \pm 0.31)$ | $M_{\odot}$ |
| $a_{3}\left(i^{\prime}=90^{\circ}\right) \ldots \ldots \ldots \ldots$. | $15.4( \pm 1.8)$ | A.U. |
| $a_{3}\left(i^{\prime}=70^{\circ}\right) \ldots \ldots \ldots \ldots$. | $15.3( \pm 1.7)$ | A.U. |
| $a_{3}\left(i^{\prime}=50^{\circ}\right) \ldots \ldots \ldots \ldots$. | $15.0( \pm 1.7)$ | A.U. |
| $a_{3}\left(i^{\prime}=30^{\circ}\right) \ldots \ldots \ldots \ldots$. | $14.2( \pm 1.7)$ | A.U. |
| $a_{3}\left(i^{\prime}=10^{\circ}\right) \ldots \ldots \ldots \ldots$. | $10.3( \pm 1.4)$ | A.U. |

However, this model was ruled out by Marsh \& Pringle (1990) based on energetic considerations. In 1992, a detailed improvement on the theory was made by Applegate, who proposed that a quasi-periodic exchange of angular momentum between the inner and the outer parts in the convection zone may induce a modulation of stellar oblateness and consequently its quadruple moment. Therefore, the orbital period will be changed. Recently, the details of Applegate's mechanism have been studied by Lanza, Rodonò, \& Rosner (1998). They pointed out that apart from the redistribution of the internal angular velocity, the change in the azimuthal field intensity can likewise produce a change in the oblateness of the active component, and the stability of the azimuthal magnitude field was discussed by considering a more general magnetic field geometry (Lanza \& Rodonò 1999). For S Equ, its secondary is a G-type giant which contains a deep convective envelope and rotates very fast (several times as the Sun does). The periodic change in the period can also be plausibly interpreted as the result of the variation of the quadruple momentum via the magnetic activity of the cooler component as other Algol-type systems discussed by Zavala et al. (2002). With the equation given by Applegate (1992) and by Lanza et al. (1998),

$$
\begin{equation*}
\frac{\Delta P}{P}=-9\left(\frac{R}{a}\right)^{2} \frac{\Delta Q}{M R^{2}} \tag{11}
\end{equation*}
$$

the required change in the quadruple moment $\Delta Q$ in order to reproduce an orbital period change $\Delta P=1.51 \times 10^{-5}$ days is calculated to be $\Delta Q=2.27 \times 10^{50} \mathrm{~g} \mathrm{~cm}^{-2}$. However, since the secondary is a giant with an extremely small mass of $0.30 M_{\odot}$, the properties of magnetic activity cycle in this kind of stars are not clear.

## 4. CONCLUSIONS

Many photometric and spectroscopic studies have shown that S Equ is a very low mass ratio Algol-type binary star ( $q=0.13$ ) (e.g., Plavec 1966; Cester et al. 1979; Zola 1992). The rapid period increasing suggests that S Equ is a low mass ratio Algol-type binary in the active phase of mass transfer. According to the evolutionary theory of binary stars, Algol-type eclipsing binaries with very low mass ratio should be in a slow mass transfer stage on nuclear timescale. The present investigation may indicate that a rapid mass exchange still occurs in some of this kind of binaries. Thus, S Equ is a very important binary for understanding the evolution of Algol-type variables.

By the analysis of the photoelectric data, a significant third light in the systems was found by Zola (1992). This indicates that the alternating period change of S Equ may be cyclic, which is caused by the presence of a third body. These findings suggest that S Equ may be a truly triple system. In the previous section, the orbital parameters of the third body are determined and are listed in Table 2. Zola's photometric investigation shows that the amount of the third light is comparable to the contribution of the cooler component to the total flux of the system. If we assume that the third body is a main-sequence star and with Boehm's (1989) mass-luminosity relation, the mass of the third body is estimated to be $m_{3}=1.4 M_{\odot}$. Therefore, the orbital inclination of the third body should be $i^{\prime} \sim 16^{\circ}$, which is rather smaller than that of the eclipsing binary system $\left(i=88^{\circ} 3\right)$. If this is true, we can conclude that the third body is cap-
tured by the eclipsing pair. The triple system is not like planetary systems (and galaxies) as formed by contracting spinning gaseous clouds. However, it should be noted that, in the solution of the W-D code, THIRD LIGHT may be the result of a numerical artifact, since it is usually strongly correlated with many parameters. New accurate photometric and spectroscopic observations and a careful analysis of those data are needed. On the other hand, the secondary of S Equ is a late-type giant as in other Algols. The alternate period change may also be resulted from the variation of the gravitational quadruple momentum from periodic magnetic
activity of the G-type component. Since the third body would produce exactly periodic variations in the $O-C$ curve, more determinations of eclipsing times over next decade are very important to settle the question.

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[^1]:    ${ }^{3}$ Available at http://www.oa.uj.edu.pl/ktt/krttk_dn.html.

