THE TIME DELAY IN THE GRAVITATIONAL LENS PKS 1830-211

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ABSTRACT

We have measured a time delay of 26^{+4}_{-5} days and a magnification ratio of 1.52 ± 0.05 in the strong radio gravitational lens PKS 1830–211. Observations were made over the 18 month period from 1997 January to 1998 July with the Australia Telescope Compact Array at 8.6 GHz, and they have shown that the source started a large flux density outburst around 1997 June.

Subject headings: galaxies: individual (PKS 1830-211) - gravitational lensing

1. INTRODUCTION

A precise measurement of the time delay between the images in a gravitational lens is essential if it is to fulfill its potential as a tool for estimating the Hubble constant. The flat-spectrum radio source PKS 1830-211 (Rao & Subrahmanyan 1988) was found to be an Einstein ring/gravitational lens composed of two compact, flat-spectrum components located on opposite sides of a 1" diameter ring (Jauncey et al. 1991). It is by far the strongest radio lens yet found, being ~ 10 Jy at 4.8 GHz. Observations of molecular absorption at centimeter and millimeter wavelengths have revealed two intervening galaxies at z = 0.19 (Lovell et al. 1996b) and z = 0.89 (Wiklind & Combes 1996). VLBI observations of the two compact lensed components revealed striking structural differences on milliarcsecond scales (Garrett et al. 1996), suggesting that both galaxies may be involved in the lensing (Lovell et al. 1996b). PKS 1830-211 varies dramatically at radio wavelengths (Lovell et al. 1996a). VLBI observations show that the variations are confined to the two compact components (King 1994), making it an excellent candidate for relative time delay measurements.

This Letter describes our measurements with the 6×22 m Australia Telescope Compact Array (ATCA) to determine the lensing time delay in PKS 1830–211 through a correlation of the flux density light curves of its compact components. Section 2 describes the development of our observing strategy and data reduction; § 3 describes the analysis of our data to obtain a time delay and magnification ratio. In § 4 we describe our error analysis, and in § 5 we discuss the implications of our measurements on modeling the PKS 1830–211 lensing system.

2. OBSERVATIONS AND DATA REDUCTION

The presence of a single peak in the 8.4 GHz total flux density light curve in early 1992 (Lovell et al. 1996a) indicates that the lensing time delay is less than a few months (a time delay that was much longer would result in a broader or double-peaked light curve). Consequently, in order to sufficiently time resolve these variations in the compact components, it was

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necessary to measure the flux densities of the two components separately on timescales shorter than both the total flux density variations and the lensing time delay, previously estimated to be 44 \pm 9 days (van Ommen et al. 1995). We commenced our ATCA monitoring observations in 1995 August, making observations at approximately monthly intervals. The two compact and variable components can be measured separately, as explained below, on the 6 km east-west array of the ATCA at 8.6 GHz if observations are restricted to between 15 and 19 hr local sidereal time, when the ATCA provides subarcsecond spatial resolution along the position angle of the compact components. The strong, compact, flat-spectrum source PKS 1921-293 was observed in each session to provide the relative gain calibration of the individual antennas, while overall flux density calibration was determined through observations of the ATCA primary flux density calibrator PKS 1934-638. The total flux density variations of PKS 1830-211 will be presented in a future paper (Lovell et al. 1998). During the period 1996 July 26-August 8, a more closely spaced series of observations was undertaken in order to gain an understanding of the shorter term variability. Analysis of this 1996 July-August data showed more rapid variability than previously thought, so from 1997 January, one observation every 3-6 days was made to better sample the light curves. In this Letter, we restrict our analysis to the data from 1996 July onward, although the data from the period 1996 December 20 through 1997 January 10 were also excluded, since the source was too close to the Sun.

Since the two compact components of PKS 1830-211 are not fully resolved from the ring at the ~0".9 resolution of the ATCA at 8.6 GHz, we have adopted a model-fitting approach to determine the flux densities of the individual components. We chose a simple model that consists of two circular Gaussian components, each of which also contains a contribution from the nonvarying ring. The component separation was set initially to 0".95 at a position angle of 46°, as determined from VLBI observations (King 1994). These values were allowed to change slightly during model fitting but were found to deviate by no more than 3° in position angle and 12 mas in separation. All data were edited and calibrated by use of the Astronomical Image Processing System before being exported to DIFMAP (Shepherd 1997) for model fitting.

To verify that this model successfully describes the source, we analyzed an edited section from a full ATCA synthesis observation taken on 1994 December 19, when PKS 1830–211 had a total flux density of 7.2 Jy. We found that the individual fitted Gaussian component flux densities differed by no more than 70 mJy from those measured from the full synthesis data.

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Component flux density errors were estimated at each epoch by use of the method described by Tzioumis et al. (1989) and were found to be typically ~50 mJy. The northeast and southwest component flux density light curves obtained from the fitted 8.6 GHz ATCA data since 1996 January are shown in Figure 1a. We have detected clear changes in the flux densities of the two components, with a roughly linear increase seen to begin sometime between MJD 50,530 and MJD 50,670. The clear difference in gradient between the two light curves is a result of different image magnifications. The figure also shows significant differences in the light curves, the most prominent being a distinct "bump" of 400 mJy in the northeast component light curve near MJD 50,700 that is seen to occur significantly later in the southwest light curve, indicating a time delay of 20–30 days. In the following section, we discuss a detailed analysis of the data to obtain a quantitative estimate of the time delay and magnification ratio and their uncertainties.

3. ANALYSIS

To estimate the time delay, it is important to consider how the variability of the lensed source is detected by the observer. In the following analysis, the subscripts 1 and 2 refer to the northeast and southwest components of PKS 1830–211, respectively. We describe the time variation of the northeast and southwest compact components of the lensed image as $S_1(t)$ and $S_2(t)$, respectively. The southwest component light curve is expected to be identical to the northeast light curve but magnified by a different amount and shifted in time; thus,

$$S_2(t) = \frac{1}{\mu} S_1(t + \Delta \tau), \tag{1}$$

where $\Delta \tau$ is the time delay and μ is the relative magnification ratio. Also lensed is an extended component that forms the Einstein ring, which contributes a constant flux density S_{ring} . The total observed flux density can therefore be described as

$$S_m(t) = S_1(t) + S_2(t) + S_{ring}.$$
 (2)

The Einstein ring contributes a large proportion: up to 50% of the total flux density at centimeter wavelengths (Jauncey et al. 1991). Therefore, the effect of the ring flux density must be considered before attempting to determine a lensing time delay. In our ATCA observations, neither $S_1(t)$ nor $S_2(t)$ are measured directly; instead, the measured quantities are

$$S_{m1}(t) = S_1(t) + S_{c1}$$
(3)

and

$$S_{m2}(t) = S_2(t) + S_{c2} = \frac{1}{\mu} S_1(t + \Delta \tau) + S_{c2}, \qquad (4)$$

where the quantities $S_{c1,2}$ are constant but unknown and



FIG. 1.—(*a*) The 8.6 GHz light-curve data for both components of PKS 1830–211. The measured northeast component flux densities are represented by the open triangular symbols, and the measured southwest component flux densities are represented by the closed circular symbols. (*b*) Northeast and southwest component light curves after applying our solutions from the dispersion analysis ($\Delta \tau = -23$ days, $\mu = 1.52$, and d = -0.62 Jy).

 $S_{\text{ring}} = S_{c1} + S_{c2}$. It is unlikely that S_{c1} and S_{c2} are equal. Therefore, it is also necessary to solve for *d*, the difference between S_{c1} and S_{c2} . The two light curves may now be compared using trial values of μ , $\Delta \tau$, and *d* so that a solution for the relative magnification ratio and the time delay can be obtained.

3.1. Dispersion Analysis

A correlation of the two light curves was undertaken using the dispersion analysis method introduced by Pelt et al. (1994, 1996) to analyze the component light curves of the gravitational lens 0957+561. This method has been shown to be successful for 0957+561, which has a relatively large time delay of 417 \pm 3 days (Kundić et al. 1997). We chose this method because it avoids any interpolation between data points. Methods that are based on interpolation can lead to erroneous results, since they put equal weight on assumed and measured data.

Following Pelt et al. (1994, 1996), for every test value of μ , $\Delta \tau$, and d, two light-curve data sets a_i and b_i (i = 1, ..., N, where N is the number of observations) are obtained. Together they form a combined light curve in which a_i contains the northeast variable component data and b_i contains the southwest variable component data modified in flux density and time by the test values for μ , $\Delta \tau$, and d. The dispersion D^2 of this

light curve is calculated from the weighted sum of squared differences between nearby a_i , b_i pairs over the entire curve:

$$D^{2}(\Delta\tau,\mu) = \frac{\sum_{ij} W_{ij} V_{ij}' (a_{i} - b_{j})^{2}}{2\sum_{ij} W_{ij} V_{ij}'},$$
(5)

where

$$V'_{ij} = \begin{cases} 1 & \text{if } |t_i - t_j| \le \delta \\ \left[1 + \left(\frac{\delta - |t_i - t_j|}{\delta/2}\right)^2\right]^{-1} & \text{if } |t_i - t_j| > \delta, \end{cases}$$
(6)

$$W_{ij} = \frac{W_i W_j}{W_i + W_i},\tag{7}$$

and $W_i = 1/e_i^2$, where e_i is the standard error in data point *i*. The weighting factor V'_{ij} ensures that data pairs are only given significant weighting if they are less than $\sim \delta$ days apart, and it is modified from the V_{ij} of Pelt et al. to avoid strong weighting on data points with near-zero separation. These points add a bias toward a zero delay for relatively short time delays, as expected in PKS 1830–211. Values of $\Delta \tau$, μ , and *d* for which D^2 is a minimum are thus the best estimate of the time delay, magnification ratio, and constant flux density offset difference.

Before a correlation of the light curves can be made, an estimate of δ , effectively the longest timescale over which the source is believed not to show significant variability, must be determined. An inspection of the light curves in Figure 1 shows significant changes in flux density on timescales of the order of 10 days. We note that V' drops quite slowly, reaching 0.5 at a point separation of 1.5 δ . Therefore, we chose a value of $\delta = 5$, which is slightly less than the estimated timescale, so that points with separations greater than ~8 days did not unduly influence the solution.

A single, unambiguous solution was found for $\delta = 5$ days at $\Delta \tau = -23$ days (i.e., northeast component leading), $\mu =$ 1.52, and d = -0.62 Jy. We also investigated how the solution behaved for a range of δ and found that for $\delta < 7$ days, $\Delta \tau$ stayed within ± 4 days, μ stayed within ± 0.02 , and d stayed within ± 0.06 Jy of the $\delta = 5$ days solution. For $\delta \ge 7$ days, up to $\delta = 14$ days (the largest value we tried), the solutions for $\Delta \tau$ became shorter, ranging from -12 to -17 days, but solutions for μ and d changed little. A visual inspection of the combined light curves with these solutions applied clearly shows a poorer correlation than seen for $\delta < 7$.

It is likely that this sudden change in the delay solution is due to an effective smoothing of the features that help register the light curves in delay. However, μ and d are affected to a lesser degree since the overall smooth, rising light curves constrain these parameters well, and the short timescale changes have little influence.

4. ERROR ANALYSIS

We carried out Monte Carlo simulations to estimate the errors in our derivation of the time delay and magnification ratio. Five hundred light-curve pairs were created with data points at the same epochs of the actual observations. The flux density of each point was calculated using a random number generator but constrained such that each simulated point was within the uncertainty of the original measurement. An additional constraint forced the sum of a pair of same-epoch measurements



FIG. 2.—(*a*) The 8.6 GHz light-curve data for both components of PKS 1830–211 for the time period surrounding the bump described in § 2. The measured northeast component flux densities are represented by the open triangular symbols, and the measured southwest component flux densities are represented by the closed circular symbols. (*b*) Northeast and southwest component light curves after applying our solutions from the dispersion analysis ($\Delta \tau = -26$ days, $\mu = 1.68$, and d = -1.17 Jy).

to be equal to the total measured flux density within the uncertainty of that observation.

Each of the 500 light-curve pairs were then correlated to obtain estimates for $\Delta \tau$, μ , and d when $\delta = 5$ days. We found that the correlated values of μ and d were distributed in a Gaussian-like manner about the values obtained from our observations. We have used these distributions to estimate errors for μ and d by measuring the width of the distributions at half their peak. We thus estimate that the magnification ratio μ is 1.52 ± 0.05 and the flux density offset d is -0.62 ± 0.05 Jy. The distribution of $\Delta \tau$ from the simulations, however, is not distributed in a Gaussian-like fashion. Instead, a broad distribution of solutions between -12 and -30 days was obtained with peaks near -15, -23, and -28 days.

Eighteen years of monitoring the gravitational lens 0957+561 have demonstrated that nonvarying or smooth light curves contribute little information to a time delay solution; in fact, such data can lead to ambiguous solutions. The detection of strong features in both light curves is required to obtain a reliable time delay measurement (Kundić et al. 1997). Bearing

this in mind, we have also analyzed the subset of data surrounding the bump seen near MJD 50,700, where the most prominent and best-sampled feature occurs (Fig. 2a), specifically to avoid ambiguities in the time delay estimate.

We found a solution at $\Delta \tau = -26$ days, $\mu = 1.68$, and d = -1.17 Jy for $\delta = 5$ (Fig. 2b). As expected, Monte Carlo simulations show the magnification ratio and flux density offset to be less well constrained here than with the full data set. We have therefore adopted the values for μ and d as determined from the full data set as our best estimates. However, the simulations show the time delay for this subset to be well constrained without ambiguities with a Gaussian-like distribution of solutions around -26 days. By measuring the width of this distribution at half its peak, we have estimated an uncertainty and obtain a time delay of -26^{+5}_{-4} days.

We are continuing our ATCA monitoring observations. When the current trend of increasing flux density at 8.6 GHz ends, the change in gradient may provide even better constraints on the time delay.

5. DISCUSSION

Out ATCA monitoring observations have allowed us to measure the time delay and magnification ratio of the gravitational lens PKS 1830–211, providing new constraints for lensing models of this system.

Our time delay measurement is not in agreement with the -44 ± 9 day measurement of van Ommen et al. (1995) from VLA monitoring observations at 8.6 and 15 GHz. We believe that van Ommen et al. did not correctly account for the contribution of the Einstein ring flux density when calculating the magnification ratio. The difference between the total flux density of the source and the sum of the compact component flux densities fitted to the data, i.e., the contribution from the ring, should be constant. However, in van Ommen et al.'s analysis, the inferred Einstein ring contribution depends on the observing frequency and array configuration. We feel confident that our

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analysis of the ATCA data has correctly accounted for the constant Einstein ring flux density.

Millimeter observations in early 1996 by Frye, Welch, & Broadhurst (1997), which clearly separate the core components of the lens and show no extended jet structure on ~ 0.5 scales, provide an estimate for μ of 1.14 \pm 0.06. Also, Wiklind & Combes (1998) measured the magnification ratio in the millimeter band on three occasions over 11 months and found that it changed between 1.0 and 1.8 with an uncertainty in each case of 0.1. PKS 1830-211 has shown strong variability at millimeter wavelengths in the past (Tornikoski et al. 1996), and Wiklind & Combes observed a decrease in total flux density from 1.5 to 0.93 Jy over their observations. Such variability could influence the measurement of the magnification ratio at a single epoch. Also, the likelihood of subcomponents in the compact structure at these wavelengths, similar to those seen at 43 GHz by Garrett et al. (1998), should be investigated, since this has an impact on the magnification ratio. More detailed monitoring of the compact components at millimeter wavelengths can provide a test of our magnification ratio measurement if the time delay effect is accounted for.

It is not yet possible to obtain an estimate for H_0 from the PKS 1830–211 lensing system, since the redshift of the lensed active galactic nucleus is not known and the lensing galaxies are not well parameterized. However, if we assume that the intervening galaxy at z = 0.19 has a negligible gravitational affect on the system, then we can apply our time delay measurement to the model of Nair, Narasimha, & Rao (1993) for a lensing galaxy at z = 0.89 to put constraints on the redshift of the background source z_s . If H_0 is assumed to be between 50 and 100 km s⁻¹ Mpc⁻¹ and $q_0 = 1/2$, then a time delay of -26^{+5}_{-4} days implies $z_s > 1.4$.

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Note added in proof.—Since submitting the present Letter, we have learned that C. Lidman, F. Courbin, G. Meylan, T. J. Broadhurst, B. Frye, & J. Welch (in preparation [1998]) have measured a redshift of 2.507 \pm 0.002 in the near-infrared for the lensed quasar in PKS 1830–211. Combining this value with our measured time delay and taking the Nair et al. (1993) model at face value yields a value for H_0 of 65^{+16}_{-9} km s⁻¹ Mpc⁻¹ ($\Omega_0 = 1$, $\lambda_0 = 0$). However, given the presence of the two measured absorption redshifts (Lovell et al. 1996a; Wiklind & Combes 1996), a more detailed lensing model for PKS 1830–211 may need to be developed. Nevertheless, our value for H_0 is in good agreement with the value of 69^{+7}_{-10} km s⁻¹ Mpc⁻¹ (at 1 σ confidence) determined by A. Biggs, I. W. A. Browne, P. Helbig, L. V. E. Koopmans, P. N. Wilkinson, & R. A. Perley (MNRAS, submitted [1998]) for the lens system B0218+357 and the preliminary value of 63 ± 4 km s⁻¹ Mpc⁻¹ (at 1 σ confidence) for the B1608+656 lens system (C. D. Fassnacht, T. J. Pearson, A. C. S. Readhead, I. W. A. Browne, L. V. E. Koopmans, S. T. Myers, & P. N. Wilkinson, in preparation [1998]; L. V. E. Koopmans & C. D. Fassnacht, in preparation [1998]).