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Metastable supersymmetry breaking and multitrace deformations of SQCD

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ABSTRACT: Metastable vacua in supersymmetric QCD in the presence of single and multi-trace deformations of the superpotential are explored, with the aim of obtaining an acceptable phenomenology. The metastable vacua appear at one loop, have a broken R-symmetry, and a magnetic gauge group that is completely Higgsed. With only a single trace deformation, the adjoint fermions from the meson superfield are approximately massless at one loop, even though they are massive at tree level and R-symmetry is broken. Consequently, if charged under the standard model, they are unacceptably light. A multitrace quadratic deformation generates fermion masses proportional to the deformation parameter. Phenomenologically viable models of direct gauge mediation can then be obtained, and some of their features are discussed.

KEYWORDS: Supersymmetry Breaking, Supersymmetry and Duality, Supersymmetric gauge theory, Supersymmetric Effective Theories

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1 Introduction

Relaxing the requirement that supersymmetry breaking occurs in the true vacuum (see e.g. [1]–[3]) can help overcome many of the constraints of dynamical supersymmetry breaking with no supersymmetric vacua [4]. Recently, Intriligator, Seiberg and Shih [5] have shown that metastable dynamical supersymmetry breaking is rather generic and easy to

achieve. They found that metastable vacua occur in supersymmetric QCD (SQCD), in the free magnetic range, when the quarks have small masses,

$$W = \text{tr}(m\tilde{Q}Q). \tag{1.1}$$

This has opened many new avenues for model building and gauge mediation; see [6]–[21] for some examples of recent work, and [22] for a review and a more complete list of references.

It is not possible to build a phenomenologically viable model of gauge mediation using directly the ISS superpotential (1.1). This is due to an unbroken R-symmetry that forbids non-zero gaugino masses. A natural question is then how the phenomenology changes when the superpotential is a more general polynomial in $\tilde{Q}Q$. While this has been considered before for some particular superpotential deformations (see e.g. [11, 14, 16, 20, 23]), a more detailed account of the space of metastable vacua and the low energy phenomenology is needed. For instance, the light fermions of the model have not been fully explored. The aim of this work is to analyze the IR properties of the theory and its phenomenology in the presence of a generic $U(N_f)$ -preserving polynomial superpotential

$$W = m \text{tr}(Q\tilde{Q}) + \frac{1}{2\Lambda_0} \text{tr}[(Q\tilde{Q})^2] + \frac{1}{2\Lambda_0} \gamma [\text{tr}(Q\tilde{Q})]^2 + \dots, \tag{1.2}$$

where $\Lambda_0 \gg \Lambda$ is some large UV scale, γ is an order one coefficient, and ‘...’ are sextic and higher dimensional operators.

Deforming (1.1) by a generic polynomial in $\tilde{Q}Q$ breaks R-symmetry explicitly at tree level, and additional supersymmetric vacua are introduced [24]. The supersymmetric vacua for a single trace superpotential were analyzed in detail in [16], where it was found that the magnetic theory has classical supersymmetric vacua with various possible unbroken subgroups of the magnetic gauge group. This should be contrasted with the case of ISS, eq. (1.1), where the magnetic gauge group is completely Higgsed and supersymmetry is broken classically by the rank condition.

After taking into account one loop quantum corrections in the magnetic theory, one finds the deformed theory also has metastable vacua at low energies [16]. The dynamical reason for this is that the deformations to the magnetic superpotential come from irrelevant operators in the electric theory, which are parametrically suppressed. Therefore, we end up with a controllable deformation of the ISS construction in the IR. These vacua break R-symmetry spontaneously, and in phenomenologically interesting regions of parameter space the spontaneous breaking is much larger than the explicit breaking.

Since supersymmetric vacua allow for unbroken magnetic gauge groups, one might expect the same to occur for metastable vacua. However, the metastable vacua in the theories we explore below have a completely broken magnetic gauge group; vacua with unbroken subgroups of the magnetic gauge group do not occur. This is in some disagreement with [16] and it would be interesting to see how this effect appears in the brane constructions of metastable vacua [25].

Next we will analyze the phenomenological properties of the spectrum, with particular attention to the light fermions, including the Standard Model gauginos and a multiplet of fermions from the “meson” superfield $M = \tilde{Q}Q$. If the superpotential contains only single

traces of powers of M , the singlet and adjoint parts of the meson superfield $M = \tilde{Q}Q$ have the same one loop effective action. The singlet fermion is the Goldstino, and must be massless at one loop through a cancellation of its nonzero tree level mass against a one loop correction. The adjoint fermions (or more precisely, a certain subset thereof) have the same tree and one loop effective action, and so their masses arise only at two loops (and/or through equally small mixing effects.) Consequently their masses are small compared with those of the Standard Model gauginos, which arise at one loop.

In this paper we will be considering the case where the embedding of the Standard Model gauge group into the $U(N_f)$ flavor group endows these fermions with Standard Model quantum numbers. With such light masses, these fermions would already have been observed, and so these models would be phenomenologically unacceptable.

We are therefore led to consider a multitrace deformation of the superpotential; in particular, we must take $\gamma \neq 0$ in eq. (1.2). Then the cancellation between the tree level and one loop masses for the Goldstino fails for the adjoint fermions, leaving them with masses proportional to γ . The phenomenology of direct gauge-mediated models based on this theory is quite rich, since the adjoint fermions may be lighter or heavier than the Standard Model gauginos, depending on γ . Mixing between these fermions and the gauginos is negligibly tiny, due to a charge-conjugation symmetry in (1.2). We will briefly discuss some of the interesting phenomenological properties of such a scenario, leaving the details to a forthcoming publication [26].

The various sections are arranged as follows. In section 2, we discuss the moduli space of SQCD with the superpotential eq. (1.2), keeping only terms up to quartic order in the electric fields. In section 3, we review SQCD without deformations (ISS), with emphasis on the spectrum and associated phenomenological issues. In section 4, we study single trace deformations of the ISS superpotential, that is, the case $\gamma = 0$. We show that all metastable vacua have a magnetic gauge group that is completely Higgsed, and we discuss the spectrum, showing it is unacceptable for phenomenology. Next, in section 5 we consider $\gamma \neq 0$, describing the spectrum in detail. Finally, section 6 contains a brief overview of the phenomenology of and constraints on such models. Various computations are shown in detail in the appendix.

2 SQCD with a multitrace superpotential

In this section, we analyze the symmetries and supersymmetric vacua of SQCD in the presence of a generic $U(N_f)$ -preserving polynomial superpotential.

Supersymmetric QCD with gauge group $SU(N_c)$ and N_f flavors (Q_i, \tilde{Q}_j) with equal masses m has a global symmetry group

$$SU(N_f)_V \times U(1)_V \tag{2.1}$$

under which (Q_i, \tilde{Q}_i) transform as $(\square_{+1}, \bar{\square}_{-1})$. There is also a discrete \mathbb{Z}_2 charge conjugation symmetry $Q_i \leftrightarrow \tilde{Q}_i$. For phenomenological applications we will later weakly gauge a subgroup of $SU(N_f)_V$ and identify it with the Standard Model gauge groups. We will also gauge $U(1)_V$ to remove a Nambu-Goldstone boson.

The most general quartic superpotential preserving this symmetry is of the form

$$W = m \operatorname{tr}(Q\tilde{Q}) + \frac{1}{2\Lambda_0} \operatorname{tr}[(Q\tilde{Q})^2] + \frac{1}{2\Lambda_0} \gamma [\operatorname{tr}(Q\tilde{Q})]^2. \quad (2.2)$$

We will typically consider $\Lambda_0 \gg \Lambda \gg m$, and take γ to be of order one or smaller. We will not consider sextic or higher operators, since they are suppressed by higher powers of Λ_0 and would not affect our discussion. The nonrenormalizable superpotential (2.2) could be generated from a renormalizable theory, for example by integrating out fields with masses $\sim \Lambda_0$ that couple to $Q\tilde{Q}$.

Let us consider the theory in various limits. First, for $W = 0$ there is a moduli space of vacua parameterized by mesons and baryons modulo classical constraints. The global symmetry is enhanced to $SU(N_f)_L \times SU(N_f)_R \times U(1)_V$, and there is a non-anomalous $U(1)_R$ symmetry as well as an anomalous $U(1)_A$ axial current.

For $m/\Lambda \neq 0$ but $\Lambda_0 \rightarrow \infty$, the superpotential is renormalizable, and the theory has an exact classical $U(1)_R$ symmetry which is anomalous at the quantum level.¹ The non-anomalous symmetries of the model are

	$SU(N_f)_V$	$U(1)_R$	$U(1)_V$
Q_i	\square	+1	+1
\tilde{Q}_i	$\overline{\square}$	+1	-1
$\Lambda^{3N_c - N_f}$	0	$2N_c$	0

plus the \mathbb{Z}_2 charge conjugation. The F-term relations lift the moduli space and the only vacuum is at the origin.

On the other hand, for $m \neq 0$ and Λ_0 large but finite, all R-symmetries are explicitly broken at the classical level. New discrete supersymmetric vacua appear in the regime

$$\tilde{Q}Q \sim m\Lambda_0.$$

2.1 Magnetic dual

Below the scale Λ , the theory is described by an effective theory, called the “dual magnetic theory”, with gauge group $SU(\tilde{N}_c)$, singlet mesons Φ_{ij} , and N_f fundamental flavors (q_i, \tilde{q}_j) ; we define $\tilde{N}_c \equiv N_f - N_c$. The theory has a positive beta function and is weakly-coupled in the infrared. After an appropriate change of variables, the classical tree level superpotential reads

$$W = h \operatorname{tr}(q\Phi\tilde{q}) - h\mu^2 \operatorname{tr} \Phi + \frac{1}{2} h^2 \mu_\phi (\operatorname{tr} \Phi^2 + \gamma (\operatorname{tr} \Phi)^2). \quad (2.3)$$

where the first trace is over magnetic color and the remaining traces are over flavor indices. The relation with the electric variables is (roughly)

$$\Lambda\Phi \sim \tilde{Q}Q, \quad h\mu^2 \sim \Lambda m, \quad h^2\mu_\phi \sim \frac{\Lambda^2}{\Lambda_0}.$$

¹There is also an approximate non-anomalous R-symmetry “ $U(1)_{R'}$ ” which is restored as $m \rightarrow 0$, but we will not need to consider this symmetry.

More details may be found in [5].

As in ISS, we restrict to small quark masses $m \ll \Lambda$. We will also restrict ourselves to the range

$$\Lambda_0 \gg \sqrt{\frac{\Lambda}{m}} \Lambda, \tag{2.4}$$

which guarantees that $h\mu_\phi \ll \mu$. This will be needed to have long-lived metastable vacua. There are nonperturbative corrections to the superpotential (2.3), but they are all small enough not to affect our calculations given (2.4).

Also, these conditions ensure that the symmetries of the model at the scale Λ are approximately $SU(N_f)_L \times SU(N_f)_R \times U(1)_V \times U(1)_{R'}$, broken to $SU(N_f)_V \times U(1)_V$ only by effects of order m/Λ and Λ/Λ_0 . Therefore, to an excellent approximation, both the superpotential *and* the Kähler potential satisfy the larger symmetry group, under which the trace and traceless parts of Φ_{ij} transform as a single irreducible multiplet. We will work only to leading non-vanishing order in the symmetry-breaking effects from non-zero m and non-infinite Λ_0 .

Furthermore, the discrete \mathbb{Z}_2 charge-conjugation symmetry of the electric theory appears as the transformation

$$\Phi \rightarrow \Phi^T, \quad q_i \leftrightarrow \tilde{q}_i. \tag{2.5}$$

This transformation plays an important role in the phenomenology of gauge mediation models based on (2.3), and indeed in other ISS-related models (see e.g. [32]).

As in the electric theory, the R-symmetry is explicitly broken, and we expect new supersymmetric vacua parametrically at μ^2/μ_ϕ . Indeed, the solutions to the F-term constraints

$$\begin{aligned} (-h\mu^2 + h^2\mu_\phi\gamma \text{tr } \Phi) I_{N_f \times N_f} + h^2\mu_\phi \Phi + h\tilde{q}q &= 0 \\ q\Phi = \Phi\tilde{q} &= 0, \end{aligned} \tag{2.6}$$

are

$$\langle h\Phi \rangle = \frac{1}{1 + (N_f - k)\gamma} \frac{\mu^2}{\mu_\phi} \begin{pmatrix} 0_{k \times k} & 0_{k \times (N_f - k)} \\ 0_{(N_f - k) \times k} & I_{(N_f - k) \times (N_f - k)} \end{pmatrix} \tag{2.7}$$

and

$$\langle \tilde{q}q \rangle = \frac{1}{1 + (N_f - k)\gamma} \mu^2 \begin{pmatrix} I_{k \times k} & 0_{k \times (N_f - k)} \\ 0_{(N_f - k) \times k} & 0_{(N_f - k) \times (N_f - k)} \end{pmatrix} \tag{2.8}$$

with $k = 1, \dots, N_f - N_c$. (Here I represents the identity matrix, and a subscript $r \times s$ indicates a block matrix of the corresponding size.) The appearance of the extra parameter k classifying different classical vacua has been observed for $\gamma = 0$ by [16]. In particular, for $k < N_f - N_c$ there is an unbroken magnetic gauge group $SU(N_f - N_c - k)$.

3 Metastable DSB in the R-symmetric limit

In the next three sections, we will analyze the IR dynamics of (2.3) in three steps. First, we review the ISS model [5], the R-symmetric limit $\mu_\phi = 0$, which corresponds to an electric

SQCD with massive flavors and no irrelevant operators. We will highlight the spectrum and associated phenomenological problems. In section 4, we show how these problems are not entirely solved by making μ_ϕ non-zero but leaving $\gamma = 0$. Finally, in section 5, we show how the theory with $\gamma \neq 0$ resolves the remaining problems.

3.1 The model and its spectrum

The ISS model considers massive SQCD near the origin in field space in the free magnetic range $N_c + 1 \leq N_f < \frac{3}{2}N_c$, where the theory has a dual magnetic description with superpotential

$$W = -h\mu^2 \text{tr } \Phi + h\text{tr}(q\Phi\tilde{q}). \tag{3.1}$$

At the classical level the theory breaks supersymmetry by the rank condition. We parametrize the fields by

$$\Phi = \begin{pmatrix} Y_{\tilde{N}_c \times \tilde{N}_c} & Z_{\tilde{N}_c \times N_c}^T \\ \tilde{Z}_{N_c \times \tilde{N}_c} & X_{N_c \times N_c} \end{pmatrix} \tag{3.2}$$

$$q^T = \begin{pmatrix} \chi_{\tilde{N}_c \times \tilde{N}_c} \\ \rho_{N_c \times \tilde{N}_c} \end{pmatrix}, \quad \tilde{q} = \begin{pmatrix} \tilde{\chi}_{\tilde{N}_c \times \tilde{N}_c} \\ \tilde{\rho}_{N_c \times \tilde{N}_c} \end{pmatrix}, \tag{3.3}$$

where $\tilde{N}_c = N_f - N_c$ is the rank of the magnetic gauge group. The classical moduli space of vacua is parametrized by $\langle \chi\tilde{\chi} \rangle = \mu^2 I_{\tilde{N}_c \times \tilde{N}_c}$ and $\langle X \rangle$. The other fields have vanishing expectation values. In the rest of the paper we will restrict to metastable vacua with maximal unbroken global symmetry, by choosing the ansatz

$$\langle X \rangle = X_0 I_{N_c \times N_c}, \quad \langle \chi \rangle = q_0 I_{\tilde{N}_c \times \tilde{N}_c}, \quad \langle \tilde{\chi} \rangle = \tilde{q}_0 I_{\tilde{N}_c \times \tilde{N}_c}. \tag{3.4}$$

It will be checked that this is a self-consistent choice.

The vev for $\chi\tilde{\chi}$ breaks the gauge group $SU(\tilde{N}_c)_G$ completely, with the breaking pattern

$$SU(\tilde{N}_c)_G \times SU(N_f)_V \times U(1)_V \rightarrow SU(\tilde{N}_c)_V \times SU(N_c) \times U(1)'. \tag{3.5}$$

(Here all groups except $SU(\tilde{N}_c)_G$ are global; we remind the reader that $\tilde{N}_c = N_f - N_c$). The reduction of the global symmetry group leads to $2N_c\tilde{N}_c + 1$ Nambu-Goldstone modes. The fields $(\rho, \tilde{\rho}, Z, \tilde{Z})$ are charged under $U(1)'$, which plays the role of a messenger number symmetry. See [5] for a more detailed discussion.

The flat directions X are not protected by holomorphy or symmetries and, as we shall review shortly, become massive at one loop. (A field with these properties is called a “pseudo-modulus” [5].) In particular, X is stabilized at the origin. Near the origin of moduli space the rank condition imposes

$$|F_X| = |h\mu^2|, \tag{3.6}$$

and the scale of supersymmetry breaking is

$$V_{\min} = N_c |h^2\mu^4|. \tag{3.7}$$

To analyze the spectrum of the theory, it is convenient to rewrite the superpotential in terms of the component fields,

$$\begin{aligned}
 W = & -h\mu^2 \text{tr} X + h \text{tr} \begin{pmatrix} \rho & Z \end{pmatrix} \begin{pmatrix} X & \mu \\ \mu & 0 \end{pmatrix} \begin{pmatrix} \tilde{\rho} \\ \tilde{Z} \end{pmatrix} \\
 & + h\mu \text{tr} [Y(\chi + \tilde{\chi})] + h \text{tr} (\chi Y \tilde{\chi} + \rho \tilde{Z} \tilde{\chi} + \chi Z \tilde{\rho}).
 \end{aligned}
 \tag{3.8}$$

The spectrum consists of three sectors, each consisting of fields satisfying $\text{Str} M^2 = 0$.

(1) The (ρ, Z) sector: treating X as a background superfield, the (ρ, Z) supersymmetric mass matrix is

$$M_f = \begin{pmatrix} hX & h\mu \\ h\mu & 0 \end{pmatrix}
 \tag{3.9}$$

while the bosonic matrix is computed, as usual, including off-diagonal blocks with F-terms.

There are $2N_c \tilde{N}_c$ Dirac fermions that come from (ψ_ρ, ψ_Z) and $(\psi_{\tilde{\rho}}, \psi_{\tilde{Z}})$. Near the origin of field space, their masses are of order $h\mu$, from (3.9). The scalars combine into $4N_c \tilde{N}_c$ complex fields, which are linear combinations of $(\rho, Z, \tilde{\rho}^*, \tilde{Z}^*)$. There are $N_c \tilde{N}_c$ complex Nambu-Goldstone bosons from the combinations $\text{Re}(\rho + \tilde{\rho})$ and $\text{Im}(\rho - \tilde{\rho})$. The $3N_c \tilde{N}_c$ remaining complex scalars have splittings of order, and centered around, $h\mu$. The numerical coefficients adjust to preserve $\text{Str} M^2 = 0$.

This sector will play the role of the messenger sector in gauge mediation applications. Once a subgroup of the flavor symmetry is identified with the Standard Model, and gauged with couplings g_{SM} , the Nambu-Goldstone modes will acquire a one loop mass of order $g_{\text{SM}}\mu/(4\pi)$. (In particular, we will study the case where $\text{SU}(N_c)$ is gauged — see eq. (3.5).) The lightest state will be stable in the full theory, since the messenger sector is protected by the non-anomalous $\text{U}(1)'$ messenger number.

(2) The (Y, χ) sector: fermions from $Y, (\chi + \tilde{\chi})$ form \tilde{N}_c^2 Dirac fermions with mass $\sim h\mu$. The traceless part² of the chiral superfield $(\chi - \tilde{\chi})$, which contains the NG bosons $\text{Im}(\chi' - \tilde{\chi}')$, is eaten by the superHiggs mechanism when the magnetic group is gauged.

The field $\text{Im} \text{tr}(\chi - \tilde{\chi})$ is a NG boson associated to the breaking of $\text{U}(1)_V$. The field $\text{Re} \text{tr}(\chi - \tilde{\chi})$ corresponds to a pseudo-modulus, which will be lifted at one loop. The fermion from $\text{tr}(\chi - \tilde{\chi})$ is massless. This sector has a supersymmetric spectrum at tree level.

The massless fields from $\text{tr}(\chi - \tilde{\chi})$ would be phenomenologically forbidden. This forces us to gauge $\text{U}(1)_V$, so that the superfield $\text{tr}(\chi - \tilde{\chi})$ is eaten by the $\text{U}(1)_V$ gauge boson and at tree level acquires a mass of order $g_V\mu$.

(3) The X sector: X is a flat direction, with massless fermionic partner at tree level. In particular, $\psi_{\text{tr} X}$ is the Goldstino.

One loop contributions from heavy particles lift the pseudo-moduli. The fields $(Y, \chi, \tilde{\chi})$ do not couple at tree level to the supersymmetry breaking sector, so they do not contribute to the one loop effective potential for the pseudo-moduli. Because we are in the regime where $|F_X| = |h\mu^2|$ is of order the square of the messenger masses, the effect of integrating

²We denote traceless fields with primes; for instance X' is the traceless part of X .

out the messengers does not have a simple expression in superspace, and it is more convenient to work directly with nonsupersymmetric expressions. The bosonic action is given by the usual Coleman-Weinberg formula [27]

$$V_{\text{CW}} = \frac{1}{64\pi^2} \text{STr } M^4 \log \frac{M^2}{\Lambda^2}. \quad (3.10)$$

Near the origin of moduli space $X \ll \mu$, the potential is approximated by [5]

$$V_{\text{CW}} \approx \frac{a}{2} |h^4 \mu^2| \text{tr} \left(\text{Re} \frac{1}{\sqrt{2}} [\chi - \tilde{\chi}] \right)^2 + b |h^4 \mu^2| \text{tr} (X^\dagger X) \quad (3.11)$$

with

$$a = \frac{\log 4 - 1}{8\pi^2} N_c, \quad b = \frac{\log 4 - 1}{8\pi^2} \tilde{N}_c. \quad (3.12)$$

Therefore, in the ISS model the pseudo-moduli are consistently stabilized at the origin and R-symmetry is preserved. In this approximation, the one loop mass of the bosonic field X is given by

$$m_{\text{CW}}^2 = b |h^4 \mu^2| = \frac{\log 4 - 1}{8\pi^2} \tilde{N}_c |h^4 \mu^2|. \quad (3.13)$$

3.2 Phenomenological problems

One could try to use the ISS construction as the supersymmetry breaking sector in models of direct gauge mediation. However, since R-symmetry is preserved in the metastable vacuum, Majorana masses for the Standard Model gauginos are forbidden. The same applies to the fermions ψ_X and $\psi_{\chi-\tilde{\chi}}$, which may have SM quantum numbers after embedding the SM gauge group into the flavor symmetry group of the model. For these reasons, this model does not give an acceptable phenomenology.

There are various ways of improving this situation (see, for instance, [28]–[31]). One very interesting proposal [32] is that the gauginos could come from Dirac fermions, whose mass is not constrained to vanish by an unbroken R-symmetry. This idea was applied to the ISS model in [33], by adding new fields and interactions to the superpotential. Dirac masses appear from one loop diagrams mixing the MSSM Weyl gauginos with the new Weyl fermions. One problem with this approach is that doubling the number of fields (in order to have Dirac fermions) creates a Landau pole close to the messenger scale. In this case, corrections from the microscopic theory may become important.

Another possibility is to deform the superpotential by higher powers of the meson superfield, explicitly breaking the R-symmetry at tree level [11, 14, 16]. We consider this possibility in detail below.

4 Single trace deformation

We begin by considering the superpotential eq. (2.3) with $\gamma = 0$, that is, with only a single trace perturbation:

$$W = -h\mu^2 \text{tr } \Phi + h \text{tr}(q\Phi\tilde{q}) + \frac{1}{2} h^2 \mu_\phi \text{tr}(\Phi^2). \quad (4.1)$$

This model was discussed in [16], where it was suggested that new metastable vacua, with unbroken magnetic group, appear around $X \sim \mu$. However, this region of parameter space is subtle, because higher order corrections to (3.11) become important. We will have two new things to say about this model.

- (1) By considering the full logarithmic one loop potential (3.10), it is possible to show that the metastable vacua with unbroken magnetic gauge group are actually unstable. Thus, one is led to study only the ISS-like vacuum where the magnetic gauge group is completely Higgsed.
- (2) Gauginos indeed become massive at one loop in this model, as expected from the R-symmetry breaking. However (ignoring some subtleties which we will discuss later) the adjoint fermions $\psi_{X'}$ become massive only at two loops, because diagrammatic cancellations that make the Goldstino $\psi_{\text{tr } X}$ massless at one loop also force the adjoint fermions $\psi_{X'}$ to be massless at this order. This provides the main motivation for studying non-zero γ below.

4.1 Metastable supersymmetry breaking

The classical supersymmetric vacua are obtained by setting $\gamma = 0$ in (2.7) and (2.8). In order to analyze the effect of the deformation on the ISS metastable vacuum, the cases $k = N_f - N_c$ and $k < N_f - N_c$ have to be distinguished.

Case $k = N_f - N_c$. This is the analog of the ISS construction, with no unbroken gauge group. The fields are parameterized as in eqs. (3.2) and (3.3). We will now review why a metastable vacuum appears at a distance of order μ_ϕ/b away from the origin [16].

As a starting point, set $V_{\text{CW}} \rightarrow 0$. Due to the classical deformation, X is no longer a flat direction, unlike the ISS case. Rather, the origin $X_0 \sim 0$ is at the side of a paraboloid of classical curvature $|h^2\mu_\phi|^2$. In other words, the origin is unstable against classical flow of X_0 toward the supersymmetric vacua discussed before. The tree level spectrum near the origin is shown in table 1.

In order to create a local minimum, the quantum contribution $V_{\text{CW}} \sim m_{\text{CW}}|X_0|^2$ should overwhelm the curvature of the classical potential, i.e., $m_{\text{CW}} \gg |h^2\mu_\phi|$. This rather interesting effect, where a one loop contribution stabilizes a classical runaway direction, was analyzed in [15]. Here, the stabilization of X_0 can occur naturally, since μ_ϕ , arising from a nonrenormalizable operator in the microscopic theory, is parametrically small. The condition that the one loop potential introduces a supersymmetry breaking minimum,

$$\epsilon \equiv \frac{m_{\text{cl}}^2}{m_{\text{CW}}^2} \approx \left| \frac{\mu_\phi^2}{b\mu^2} \right| \ll 1, \tag{4.2}$$

is naturally satisfied.

The potentials at tree level and at one loop, as a function of X_0 , are shown in figure 1. As seen from the figure, the tree level potential (lower magenta curve), which is obtained from the superpotential in (4.1), has no supersymmetry breaking minimum. A metastable

	Fermions				Bosons			
	Weyl mult.	mass	$U(N_c)$	$SU(\tilde{N}_c)_D$	Real mult.	mass	$U(N_c)$	$SU(\tilde{N}_c)_D$
$\text{tr}X$	1	$h^2\mu_\phi$	1_0	1	2	$h^2\mu_\phi$	1_0	1
X'	$N_c^2 - 1$	$h^2\mu_\phi$	Adj ₀	1	$2(N_c^2 - 1)$	$h^2\mu_\phi$	Adj ₀	1
$Y, \chi, \tilde{\chi}$	\tilde{N}_c^2	$\mathcal{O}(h\mu)$	1_0	Adj	$2\tilde{N}_c^2$	$\mathcal{O}(h\mu)$	1_0	Adj
	\tilde{N}_c^2	$\mathcal{O}(h\mu)$	1_0	Adj	$2\tilde{N}_c^2$	$\mathcal{O}(h\mu)$	1_0	Adj
	$\tilde{N}_c^2 - 1$	$g_{\text{mag}}\mu$	1_0	Adj	$2(\tilde{N}_c^2 - 1)$	$g_{\text{mag}}\mu$	1_0	Adj
	1	0	1_0	1	1	0_{NGB}	1_0	1
$Z, \tilde{Z}, \rho, \tilde{\rho}$	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\square_1 + \bar{\square}_{-1}$	$\square + \bar{\square}$	$2N_c\tilde{N}_c$	0_{NGB}	\square_1	$\bar{\square}$
	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\square_1 + \bar{\square}_{-1}$	$\square + \bar{\square}$	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\bar{\square}_{-1}$	\square
	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\square_1 + \bar{\square}_{-1}$	$\square + \bar{\square}$	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$(\square_1 + \bar{\square}_{-1})$	$(\bar{\square} + \square)$
	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\square_1 + \bar{\square}_{-1}$	$\square + \bar{\square}$	$2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$	$\bar{\square}_{-1}$	\square

Table 1. The classical mass spectrum, grouped in sectors with $\text{Str} M^2 = 0$. Since supersymmetry is spontaneously broken only after including one loop effects, there is no Goldstino at tree level. g_{mag} is the magnetic gauge coupling. A subscript “NGB” indicates the particle is massless because it is a Nambu-Goldstone boson. Subscripts in the third column indicate the charge under the $U(1)$ subgroup. Note this table gives the spectrum before the Standard Model gauge group is gauged.

minimum is created near the origin once the one loop quantum corrections in the form of V_{CW} are included (upper blue curve).

As a result of the competition between the classical and quantum contributions, a metastable vacuum is created at

$$hX_0 \approx \frac{\mu^2\mu_\phi^*}{b|\mu|^2 + |\mu_\phi|^2}, \quad q_0\tilde{q}_0 = \mu^2; \tag{4.3}$$

see eq. (3.4) for the notation. As expected, X_0 is proportional to the explicit R-symmetry breaking parameter μ_ϕ . However, it is larger than this by the inverse loop factor $1/b$. This follows from the fact that the minimum appears from balancing a tree level linear term of order $\mu^2\mu_\phi$ against a one loop quadratic term of order $b\mu^2$.

The pattern of symmetry breaking in this vacuum is

$$SU(\tilde{N}_c)_G \times SU(N_f)_V \times U(1)_V \rightarrow SU(\tilde{N}_c)_V \times SU(N_c) \times U(1)', \tag{4.4}$$

where only the messengers transform under $U(1)'$. Unlike the ISS construction, here $X_0 \neq 0$, so that the R-symmetry is both explicitly and spontaneously broken, *with the latter dominating* since $|hX_0| \gg |\mu_\phi|$.

Case $k < N_f - N_c$. The possibility of metastable vacua with $k < N_f - N_c$ is very interesting; coupling this to the MSSM, it would imply unbroken gauge groups in the

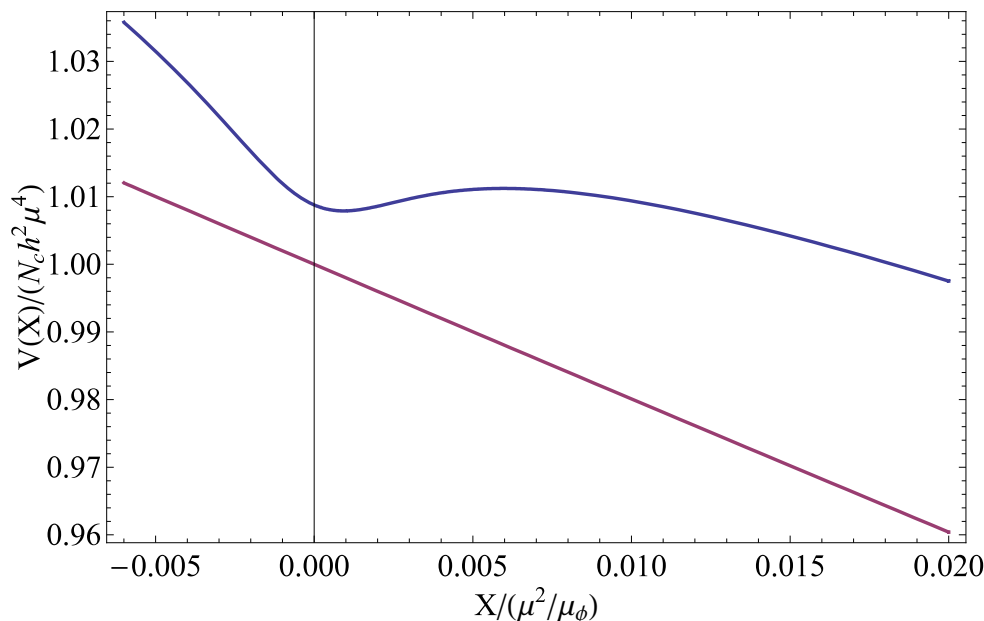


Figure 1. Metastable vacuum near $X \sim 0$, for a single trace quadratic deformation of the superpotential (i.e. $\gamma = 0$). All parameters have been chosen to be real. The bottom (magenta) line is the tree level potential, while the top (blue) line shows the tree level potential plus one loop Coleman-Weinberg corrections. The X -axis has been normalized such that the position of the tree level supersymmetric vacuum lies at $X/(\mu^2/\mu_\phi) = 1$. Notice how the one loop corrections create a (metastable) minimum near the origin.

hidden sector. Properties of such configurations were discussed in [16]. Unfortunately, we will now show that there are generically no metastable vacua in this regime.

Such vacua should be of the form

$$\Phi = \begin{pmatrix} 0 & 0 \\ 0 & X_{(N_f-k) \times (N_f-k)} \end{pmatrix}, \quad \tilde{q}q = \begin{pmatrix} \mu^2 I_{k \times k} & 0 \\ 0 & 0 \end{pmatrix}. \quad (4.5)$$

The parametrization of the fluctuations is slightly more involved,

$$\Phi = \begin{pmatrix} Y_{k \times k} & Z_{k \times (N_f-k)} \\ \tilde{Z}_{(N_f-k) \times k} & X_{(N_f-k) \times (N_f-k)} \end{pmatrix}, \quad q = \begin{pmatrix} V_{k \times k} & T_{k \times (\tilde{N}_c-k)} \\ P_{(N_f-k) \times k} & \varphi_{(N_f-k) \times (\tilde{N}_c-k)} \end{pmatrix} \quad (4.6)$$

and similarly for \tilde{q} . As in the case $k = N_f - N_c$, the expectation values are chosen to be of the form

$$\langle X \rangle = X_0 I_{(N_f-k) \times (N_f-k)}, \quad \langle V \rangle = q_0 I_{k \times k}, \quad \langle \tilde{V} \rangle = \tilde{q}_0 I_{k \times k}.$$

The new fields $(\varphi, \tilde{\varphi})$ and (T, \tilde{T}) do not exist for $k = N_f - N_c$. They are fundamental flavors of the unbroken magnetic group $SU(N_f - N_c - k)$.

As was found in [16], positivity of the bosonic mass matrix of $(\varphi, \tilde{\varphi})$ implies

$$|X_0|^2 \geq |\mu^2 - h\mu_\phi X_0|.$$

This places us in the regime $X_0 \gtrsim \mu$. In this regime, the quadratic approximation (3.11) to the Coleman-Weinberg potential is no longer valid. For $X_0/\mu \sim 1$, all the higher order terms in V_{CW} give contributions comparable to (3.11). In other words, it is necessary to use the full expression appearing in eq. (3.10).

Therefore, to establish the existence of such vacua, a detailed analysis of V_{CW} is required. As shown in the appendix, all such vacua are unstable once the full form of V_{CW} is included. The intuitive reason for this is that at large X_0 the logarithmic growth of V_{CW} cannot overwhelm the quadratic terms in the classical potential. A similar behavior was found in [15].

The plot of $V_{\text{tree}} + V_{\text{CW}}$ for this case is almost the same as that of figure 1. For sufficiently large $|X_0/\mu| > 1$, the classical falling potential dominates the logarithmic rise of the V_{CW} , and no critical points are found until the supersymmetric vacuum is reached.

Summarizing, metastable states occur only for $k = N_f - N_c$. The fields have expectation values eq. (4.3), breaking the magnetic gauge group completely at the scale μ .

4.2 Light fermions

We therefore return to the one remaining vacuum, the ISS-like case with $k = N_f - N_c$. From the previous analysis, the bosons from X and the traceless part of $\chi - \tilde{\chi}$ acquire masses of order m_{CW} . The aim of this section is to compute the fermion masses at one loop, and show that $\psi_{X_{ij}}$ remains massless at this order, contrary to naive expectations from R-symmetry breaking.

First we explore one loop effects involving the Goldstino $\psi_{\text{tr}X}$. At tree level it has a nonvanishing mass $h^2\mu_\phi$. We are not expanding around a critical point of the classical potential, but rather one of the full one loop potential, and therefore the Goldstino should become massless only once one loop effects are included. This implies that the one loop diagram has to give

$$m_{\psi_{\text{tr}X}}^{1\text{-loop}} \approx -h^2\mu_\phi, \tag{4.7}$$

such that $m_{\psi_{\text{tr}X}}^{\text{tree}} + m_{\psi_{\text{tr}X}}^{1\text{-loop}} \approx 0$. Indeed, the explicit evaluation of the one loop diagram in the appendix corroborates (4.7). These results are approximate because we are neglecting (subleading) mixings with other singlet fermions; see below and the appendix.

At a first glance it is surprising that the one loop contribution can be equal to the tree level one. This is so because the one loop diagram is of order

$$\frac{h^2}{16\pi^2} h X_0.$$

However, since $hX_0 \sim \mu_\phi/b$, with b defined in eq. (3.12), we obtain the result (4.7). This is another manifestation of the pseudo-runaway behavior discussed in the previous section.

Next, notice that within the classical superpotential (4.1), X_{ij} only appears in single traces. On the other hand, the one loop contribution is a single trace of a function of X_{ij} , because it comes from exponentiating bosonic and fermionic determinants (denoted by Δ) arising from messengers in the fundamental representation of $\text{SU}(N_c)$. Therefore, the full one loop effective action

$$S_{\text{eff}}(X, \psi_X) = S_{\text{tree}} + \text{Tr}(\log \Delta)$$

can be written as a single trace of products of X_{ij} and its superpartner. This means that *the tree level plus one loop* contribution to the masses of the X fields must be of the form $\text{Tr}(X^\dagger X)$, and therefore the singlet and adjoint parts of X get identical masses through one loop. The same is true for the fermionic partners of X : at one loop the masses of the singlet $\psi_{\text{tr } X}$ and the adjoint $\psi_{X'}$ are the same. Diagrammatically, there is a cancellation between the tree level Weyl mass and the one loop correction.

We note two small subtleties. First, we have assumed here that the kinetic terms for the singlet and adjoint parts of X have the same normalization. This is true to a very good approximation. We assumed $m \ll \Lambda \ll \Lambda_0$, which ensured that the high-energy theory's approximate $\text{SU}(N_f) \times \text{SU}(N_f)$ symmetry is only weakly broken to $\text{SU}(N_f)_V$ at the scale Λ . Under this larger symmetry, the singlet and adjoint transform as a single irreducible representation, assuring equally normalized kinetic terms, up to negligible order (μ/Λ) corrections.

Second, and irreducibly, the Goldstino is not quite $\psi_{\text{tr } X}$. As discussed in more detail in the appendix, it mixes slightly with the fields $\psi_{\text{tr } Y}$ and $\psi_{\text{tr } (\chi+\tilde{\chi})}$, with mixing angles of order a one loop factor, $\sim 1/16\pi^2$ and $\sim X_0/(16\pi^2\mu)$, respectively. Consequently the tree level and one loop ψ_X masses fail to cancel precisely, though by an amount that is one further loop-order suppressed. Thus our statement that the ψ_X masses vanish at one loop is effectively correct.

4.3 Phenomenology of the $\gamma = 0$ model

After gauging a subgroup of the flavor group $\text{SU}(N_c)$ — see eq. (3.5) — and identifying it with the Standard Model gauge group, the adjoint fermions $\psi_{X'}$ will carry Standard Model gauge charges. The fact that they are approximately massless at one loop is unacceptable phenomenologically. They do become massive at two loop order, through the above-mentioned mixings, and through explicit two loop diagrams. For example, Standard Model gauge bosons, which do not impact the singlet $\psi_{\text{tr } X}$, generate for the other fields a two loop mass of order

$$m_{\psi_{X'}} \sim g^2 \frac{X_0}{(16\pi^2)^2} \sim g^2 \frac{\mu_\phi}{16\pi^2}. \tag{4.8}$$

But the Standard Model gauginos have a one loop mass of order $X_0/16\pi^2 \sim \mu_\phi$. Importantly, the charge conjugation symmetry discussed in section 2 forbids significant mixing between λ and ψ_X , so the masses for the $\psi_{X'}$ fields cannot be raised through mixing effects. *Consequently, requiring the gauginos are at a scale $\sim 1 \text{ TeV}$ implies the $\psi_{X'}$ would be so light that they would have already been observed.*

5 The deformation with $\gamma \neq 0$

Clearly the root of this phenomenological problem lies in treating $\psi_{X'}$ and the Goldstino $\psi_{\text{tr } X}$ on the same footing in the tree level superpotential. A solution is to allow non-zero γ ,

$$W = h\text{tr}(q\Phi\tilde{q}) - h\mu^2 \text{tr } \Phi + \frac{1}{2}h^2\mu_\phi \left(\text{tr } (\Phi^2) + \gamma(\text{tr } \Phi)^2 \right). \tag{5.1}$$

such that the two have different tree level masses. Then the total one loop mass for $\psi_{X'}$ becomes proportional to $\gamma\mu_\phi$.

The motivation for considering non-zero γ

$$W = -h\mu^2 \text{tr } \Phi + h \text{tr}(q\Phi\tilde{q}) + \frac{1}{2}h^2\mu_\phi \left(\text{tr}(\Phi^2) + \gamma(\text{tr } \Phi)^2 \right), \quad (5.2)$$

extends beyond phenomenological utility. No symmetry enforces $\gamma = 0$ once μ_ϕ or even μ are non-zero, so it is quite natural for γ to be nonzero.³

Let us now analyze the metastable vacua of the theory. For $h\mu_\phi \ll \mu$ (and for $|\gamma|$ roughly of order 1), the Coleman-Weinberg potential is approximately as in ISS. The only stable local minimum occurs for $k = N_f - N_c$. The multitrace deformation adds a term proportional to the identity matrix to W_Φ , so we obtain

$$q_0\tilde{q}_0 = \mu^2 - h\mu_\phi N_c \gamma X_0. \quad (5.3)$$

$$hX_0 \approx \frac{\mu^2\mu_\phi^*(1 + N_c\gamma^*)}{b|\mu^2| + |\mu_\phi|^2 + f(\gamma, \gamma^*)} \quad (5.4)$$

with

$$f(\gamma, \gamma^*) = |\mu_\phi|^2 [N_c(\gamma + \gamma^*) + N_c^2 |\gamma|^2].$$

In the limit $h\mu_\phi \ll \mu$, the effect of γ is qualitatively unimportant:

$$hX_0 \approx \frac{\mu^2\mu_\phi^*(1 + N_c\gamma^*)}{b|\mu|^2}, \quad q_0\tilde{q}_0 \approx \mu^2, \quad (5.5)$$

so that $|hX_0| \gg |\mu_\phi|$. While $\gamma \neq 0$ does not alter the qualitative features of the vacuum, it is important, when computing the spectrum, that the precise values (5.3) and (5.4) be used.

5.1 Spectrum

We now analyze the spectrum in the metastable vacuum. As in section 4, the Goldstino is not massless at tree level. Some of the one loop diagrams exactly cancel the tree level contributions and for this reason we discuss directly the tree level plus one loop results.

We first consider the fermions of the pseudo-modulus X . The singlet fermion (the Goldstino) is massless at one loop. For the adjoint fermions, the tree level mass $h^2\mu_\phi$ is partially canceled against the one loop contribution, and the full mass is of order

$$m_{\psi_{X'}} \approx h^2\mu_\phi N_c \gamma. \quad (5.6)$$

Of course this vanishes in the limit $\gamma \rightarrow 0$, as required from section 4.

Interestingly, we will see in section 6 that the Majorana gaugino masses are proportional to $(1 + N_c\gamma)$. By changing the dimensionless parameter γ , the adjoint fermions may

³ Considering the preserved symmetries, one might wonder why the coefficients of $q\Phi\tilde{q}$ should be taken precisely equal. The point is that the physical couplings are constrained by the approximate $SU(N_f)_L \times SU(N_f)_R$ in the electric theory, which is still valid at and just below the scale Λ . In other words, the $\mu \rightarrow 0$ and $\mu_\phi \rightarrow 0$ limit implies equal couplings. Nothing comparable favors $\gamma = 0$.

	Fermions				Bosons			
	Weyl mult.	mass	$U(N_c)$	$SU(\tilde{N}_c)_D$	Real mult.	mass	$U(N_c)$	$SU(\tilde{N}_c)_D$
$\text{tr} X$	1	0	1_0	1	1 1	$\mathcal{O}(m_{CW})$ $\mathcal{O}(\sqrt{b}h^2\mu)$	1_0 1_0	1 1
X'	$N_c^2 - 1$	$h^2\mu_\phi N_c \gamma$	Adj ₀	1	$2(N_c^2 - 1)$	$\mathcal{O}(m_{CW})$	Adj ₀	1
$Y, \chi, \tilde{\chi}$	\tilde{N}_c^2 \tilde{N}_c^2 $\tilde{N}_c^2 - 1$ 1	$\mathcal{O}(h\mu)$ $\mathcal{O}(h\mu)$ $g_{\text{mag}}\mu$ $g_V\mu$	1_0 1_0 1_0 1_0	Adj Adj Adj 1	$2\tilde{N}_c^2$ $2\tilde{N}_c^2$ $2(\tilde{N}_c^2 - 1)$ 2	$\mathcal{O}(h\mu)$ $\mathcal{O}(h\mu)$ $g_{\text{mag}}\mu$ $g_V\mu$	1_0 1_0 1_0 1_0	Adj Adj Adj 1
$Z, \tilde{Z}, \rho, \tilde{\rho}$	$2N_c\tilde{N}_c$ $2N_c\tilde{N}_c$	$\mathcal{O}(h\mu)$ $\mathcal{O}(h\mu)$	$\square_1 + \bar{\square}_{-1}$ $\square_1 + \bar{\square}_{-1}$	$\square + \bar{\square}$ $\square + \bar{\square}$	$2N_c\tilde{N}_c$ $2N_c\tilde{N}_c$ $2N_c\tilde{N}_c$ $2N_c\tilde{N}_c$	0_{NGB} $\mathcal{O}(h\mu)$ $\mathcal{O}(h\mu)$ $\mathcal{O}(h\mu)$	\square_1 $\bar{\square}_{-1}$ $(\square_1 + \bar{\square}_{-1})$ $\bar{\square}_{-1}$	$\bar{\square}$ \square $(\bar{\square} + \square)$ \square

Table 2. The mass spectrum, including one loop corrections (but without Standard Model gauge interactions), grouped in sectors with $\text{Str } M^2 = 0$. Notice the appearance of the Goldstino in the $\text{tr}(X)$ sector. The details of the spectrum are described further in the text. Notation is as in table 1.

thus be made lighter or heavier than the gauginos. This allows a variety of spectra with different phenomenological signatures, see section 6.

As for the bosons of X , both the adjoint and one component of the singlet acquire one loop masses of order m_{CW} ; see eq. (3.13). The other part of the singlet, $\text{Arg}(X)$, is a massive R-axion. This is because X has a large nonzero expectation value $X_0 \sim 16\pi^2\mu_\phi \gg \mu_\phi$, which spontaneously breaks the approximate $U(1)_R$ symmetry at a scale much larger than any explicit breaking. The mass of the R-axion is given by

$$m_a^2 = \frac{2\sqrt{N_c}}{N_c|X_0|} \text{Re} [h\mu^2 (h^2\mu_\phi)^*] \sim b|h^4\mu^2|. \tag{5.7}$$

This is of the same order as the one loop mass m_{CW} , eq. (3.13).

Finally, the $(Y, \chi, \tilde{\chi})$ and $(Z, \tilde{Z}, \rho, \tilde{\rho})$ sectors are as in section 3.1. We remind the reader that we have gauged the $U(1)_V$ symmetry, and g_V denotes its gauge coupling. The (otherwise massless) fields from $\text{tr}(\chi - \tilde{\chi})$ acquire masses of order $g_V\mu$, as shown in the table. Furthermore, the NG bosons from $(\rho, \tilde{\rho}, Z, \tilde{Z})$ acquire a one loop mass of order $g_{\text{SM}}\mu/4\pi$ once the Standard Model is gauged, as a subgroup of the flavor symmetry group. The lightest of these is stable due to the unbroken messenger number $U(1)'$ from eq. (4.4).

5.2 Lifetime of the metastable vacuum

Here we check that the metastable non-supersymmetric vacuum can be sufficiently long-lived. This vacuum can decay to the ISS-like supersymmetric vacuum with $k = N_f - N_c$,

or to the supersymmetric vacua with $k < N_f - N_c$ (see section 2.1). The decay to the vacua with $k < N_f - N_c$ requires changing the expectation value of (some of the elements of) $q\tilde{q}$, from $h\mu^2$ to 0. This is strongly suppressed by the quartic potential term $V = \dots + |hq\tilde{q}|^2$. The dominant decay channel will be to the supersymmetric vacuum with $k = N_f - N_c$, which we now analyze.

The lifetime of the vacuum may be estimated using semiclassical techniques and is proportional to the exponential of the bounce action, e^B [34]. We will see that the tunneling takes place in the direction of $\text{tr} X$, in a region where $q\tilde{q} \approx \mu^2$ is almost constant. The potential as a function of $\text{tr} X$, including the one loop quantum corrections from the Coleman-Weinberg potential, is given in the appendix and shown in figure 1. It may be modeled as a triangular barrier, and the bounce action may be estimated using the results in [35].

We will see in the next section that, in order to have large enough gaugino masses but a low SUSY-breaking scale and low sfermion masses, the ratio μ_ϕ/μ cannot be made too small. Nonetheless, it is useful to first analyze the bounce action in the limit $\mu_\phi \ll \mu$, where it is clear the vacuum is parametrically stable.

The dimensionful parameters controlling the shape of the potential are μ and μ_ϕ . We assume h, γ, N_f , and N_c are all of order 1. The SUSY vacua are parametrically far away from the metastable vacua in the limit

$$\epsilon \equiv \left| \frac{\mu_\phi^2}{b\mu^2} \right| \ll 1. \tag{5.8}$$

In this limit, the calculation of the bounce action is very similar to that done in [15], as long as only $\text{tr} X$ varies. Let us assume $q\tilde{q}$ is essentially constant.

The metastable SUSY-breaking vacuum lies at $X_0 \sim \mu_\phi/b$, the peak of the potential is near $X_{\text{peak}} \sim b\mu^2/\mu_\phi$, and the SUSY vacuum is at $X_{\text{susy}} \sim \mu^2/\mu_\phi$, where phases and $\mathcal{O}(1)$ numbers have been ignored. Moreover, the potential difference between the peak and the metastable SUSY-breaking minimum is roughly $V(X_{\text{peak}}) - V(X_0) \sim b\mu^4$, much smaller than $V(X_0) - V(X_{\text{susy}}) \sim \mu^4$. The results of [35] then show that the field tunnels not to the SUSY vacuum directly but rather to $X_{\text{tunnel}} \gtrsim X_{\text{peak}}$. For this value of X_{tunnel} , eq. (2.6) implies $q\tilde{q} \approx \mu^2$, and thus $q\tilde{q}$ indeed stays approximately constant in the tunneling region. This confirms that the results in [35] apply.

In the limit $\epsilon \ll 1$, the bounce action scales parametrically as

$$B \sim \frac{(X_{\text{tunnel}})^4}{V(X_{\text{peak}}) - V(X_0)} \sim b \frac{1}{\epsilon^2}, \tag{5.9}$$

where we have neglected some numerical factors, see [35]. Thus, $B \rightarrow \infty$ as $\epsilon \rightarrow 0$, and the metastable vacuum can be made parametrically long-lived.

In section 6, we will see that in order to obtain sfermion masses that are roughly of the same size as gaugino masses, we need to take $\mu_\phi \sim b\mu$ (and thus $\epsilon \sim b$.) In this regime X_0, X_{peak} and X_{tunnel} are all parametrically of order bX_{SUSY} . A numerical study is required to determine the existence and lifetime of the metastable vacuum. Taking the gaugino masses to lie at their experimental lower bound, of order 100 GeV, we find that the

existence of a metastable vacuum sets a lower bound on the sfermion masses — typically a few TeV for the squarks and at least a few hundred GeV for the right-handed sleptons. Once such a metastable vacuum is obtained, it is easy to make the bounce action larger than the required 400 by a small increase (of order 5%) in the sfermion masses. The details of the spectrum, together with a more precise estimate of the lower bound on the sfermion masses, and the implications for the tuning of electroweak symmetry breaking, will be given in [26].

6 Comments on the phenomenology

This section briefly discusses some of the phenomenology associated with the multitrace deformation of the ISS model, equation (5.1). The details will be left to a forthcoming publication [26].

The ISS-like supersymmetry breaking models are interesting from a phenomenological point of view due to the presence of the large global symmetry group

$$\text{SU}(\tilde{N}_c)_V \times \text{SU}(N_c) \times \text{U}(1)'. \tag{6.1}$$

A model of direct gauge mediation can be built by weakly gauging a subgroup of (6.1) and identifying it with the Standard Model (SM) gauge group. The fields ρ , Z , $\tilde{\rho}$, and \tilde{Z} in (3.2) and (3.3) act as messengers that mediate the supersymmetry breaking effects to the visible sector. Loops involving these messengers can give non-zero masses to the scalar superpartners of the SM fermions and, provided there is no unbroken R-symmetry, non-zero Majorana fermion masses to the gauginos.

In this section, we will consider gauging the $\text{SU}(3) \times \text{SU}(2) \times \text{U}(1)$ subgroup of $\text{SU}(N_c)$ for $N_c = 5$ in the $\gamma \neq 0$ model, and identifying it with the SM gauge group. (The effect of gauging a subgroup of $\text{SU}(\tilde{N}_c)_V$ will be discussed in [26].)

Under the SM gauge group $\text{SU}(3)_C \times \text{SU}(2)_L \times \text{U}(1)_Y$, the adjoint field X' decomposes as

$$X' = X_{\mathbf{24}} = X_{(\mathbf{8},\mathbf{1})_0} \oplus X_{(\mathbf{1},\mathbf{3})_0} \oplus X_{(\mathbf{3},\mathbf{2})_{-5/6}} \oplus X_{(\bar{\mathbf{3}},\mathbf{2})_{5/6}} \oplus X_{(\mathbf{1},\mathbf{1})_0}. \tag{6.2}$$

The fermions from the superfields $X_{(\mathbf{8},\mathbf{1})_0}$, $X_{(\mathbf{1},\mathbf{3})_0}$, and $X_{(\mathbf{1},\mathbf{1})_0}$ carry the same gauge charges as the gluino, wino, and bino, respectively, and the first two could be directly produced at colliders.⁴ Also, there are new light fermions from the superfields $X_{(\mathbf{3},\mathbf{2})_{-5/6}}$ and $X_{(\bar{\mathbf{3}},\mathbf{2})_{5/6}}$; these are stable unless given new interactions, and require a special discussion below.

6.1 Phenomenology of $\psi_{X'}$ and λ

A very important property of the model is that *the gauginos and the adjoint $\psi_{X'}$ do not mix*. This is due to the fact that λ and $\psi_{X'}$ have charge conjugation transformations that differ by a sign,

$$C(\psi_{X'_{ij}}) = \psi_{X'_{ji}}, \quad C(\lambda_{ij}) = -\lambda_{ji}. \tag{6.3}$$

⁴The X bosons in (6.2) get a mass of order $\sqrt{b}h^2\mu \sim \mathcal{O}(10 \text{ TeV})$ from the Coleman-Weinberg potential and are thus rather heavy. If produced in the early Universe, they would have decayed promptly into ψ_X and a gaugino, excepting gauge singlets which would decay a bit more slowly through higher dimension operators.

This discrete symmetry forbids any mixing at low orders between the two sets of fermions. More precisely, C -violation in the SM allows λ and $\psi_{X'}$ to mix, but this occurs only at three loops and is thus negligibly small.

Let us estimate the gaugino and $\psi_{X'}$ masses. As discussed in section 5.1, the metastable vacuum has an approximate R-symmetry that is spontaneously broken through the non-zero vev $X_0 \sim (1 + N_c \gamma) \mu_\phi / b$, where $b \sim 1/(16\pi^2)$ is a loop factor (3.12). Therefore, gauginos obtain a one loop mass of order

$$m_\lambda \sim \frac{g^2}{16\pi^2} X_0 \sim g^2 (1 + N_c \gamma) \mu_\phi. \quad (6.4)$$

Neglecting $\mathcal{O}(1)$ numbers and factors of the gauge coupling g , an interesting phenomenology is obtained for

$$m_\lambda \sim \mathcal{O}(1 \text{ TeV}), \quad (6.5)$$

i.e. for

$$\mu_\phi \sim \mathcal{O}(1 \text{ TeV}). \quad (6.6)$$

The $\psi_{X'}$ also obtain a mass at one loop, which, using equation (5.6), is of order

$$m_{\psi_{X'}} \sim h^2 \mu_\phi N_c \gamma \sim \gamma \times \mathcal{O}(1 \text{ TeV}), \quad (6.7)$$

neglecting factors of h and g and other $\mathcal{O}(1)$ numbers. By adjusting γ , $\psi_{X'}$ can be made heavier or lighter than λ , leading to very different collider signatures as we will discuss next.

The $\psi_{X'}$ do not mix with the Standard Model gauginos at a level that determines their decays. Instead, if they are heavy enough, they can decay (promptly) into a gaugino and a gauge boson through the dimension five operator $\psi_{X'} \sigma^{\mu\nu} \lambda F_{\mu\nu}$:

$$\psi_{X'} \rightarrow \lambda + \text{gauge boson}. \quad (6.8)$$

The gauginos can decay through all the usual supersymmetric decay modes, and/or through the standard coupling of each gaugino to a gauge boson and Goldstino:

$$\lambda \rightarrow \psi_{\text{tr} X} + \text{gauge boson} \quad (6.9)$$

If instead the $\psi_{X'}$ are lighter than the gauginos, then the gauginos will decay into the $\psi_{X'}$ plus a gauge boson via the above-mentioned operator. The $\psi_{X'}$ decays to a gauge boson and an off-shell gaugino. The precise decay modes and the lifetime of the $\psi_{X'}$ depend on the details of the spectrum, and will be discussed further in [26].

From (6.2), we see that there are *new* $(\mathbf{3}, \mathbf{2})$ fermions, with charges $(\mathbf{3}, \mathbf{2})_{-5/6}$ and $(\bar{\mathbf{3}}, \mathbf{2})_{5/6}$. By binding to quarks, these form hadrons, some of which are charged. The lightest of these novel hadrons, whether charged or neutral, would be stable in the model as described so far. But this would be ruled out, since these hadrons would have been created in the early Universe, violating the bounds on the existence of heavy stable particles [36, 37]. These fermions must thus be made to decay through additional baryon-number violating operators in the superpotential and/or the Kähler potential. In [26], we will show that additional dimension five Kähler potential terms, coupling the adjoint X' to SM quarks and leptons, can allow the $(\mathbf{3}, \mathbf{2})$ fermions to decay without affecting Big-Bang Nucleosynthesis or violating current bounds on proton decay.

6.2 Sfermion masses, the SUSY-breaking scale and a light gravitino

Since the supersymmetry breaking scale is $|\sqrt{F}| = |\sqrt{h}\mu|$ and the mass scale of the messengers is of the same order, the soft scalar masses are roughly given by

$$m_S \sim \frac{g^2}{16\pi^2} \mu. \quad (6.10)$$

Comparing this to (6.4), the sfermions and gauginos have similar masses if

$$\mu_\phi \sim \mu/(16\pi^2). \quad (6.11)$$

We recall that the existence and longevity of the metastable vacuum requires $\mu_\phi \ll \mu$, see section 5.2.

More concretely, there is an interesting parameter region characterized by (6.11) and a low supersymmetry breaking scale

$$\sqrt{F} \approx \mu \sim \mathcal{O}(100 - 200 \text{ TeV}). \quad (6.12)$$

In this case, one can show (see [26]) that the heaviest sfermions (squarks) have masses of a few TeV, the lightest sfermions (right-handed sleptons) has masses of a few hundred GeV, the gaugino masses are of order several hundred GeV, and there is a large enough lifetime for the metastable vacuum. The gravitino mass is

$$m_{3/2} \sim \frac{F}{\sqrt{3}M_{\text{Pl}}} \sim \mathcal{O}(1-10 \text{ eV}), \quad (6.13)$$

where $M_{\text{Pl}} \simeq 2.4 \times 10^{18} \text{ GeV}$ is the reduced Planck mass. Such a light gravitino does not violate any cosmological or astrophysical constraints [43].

6.3 Further comments on the spectrum

As discussed in section 5, the messenger sector $(\rho, \tilde{\rho}, Z, \tilde{Z})$ contains $2N_c\tilde{N}_c$ real NG bosons, all of which become massive at one loop after weakly gauging the flavor symmetry. In the parameter range (6.12), this mass is of order of several TeV. The $U(1)'$ messenger number in (4.4) forbids the decay of the lightest of these messenger particles, which is thus stable. If the lightest messenger is neutral and weakly interacting and has an appreciable relic density, it would have a tree-level coupling to nuclei via Z -boson exchange and would have been seen at a dark matter direct detection experiment [38]–[42]. If the stable state is charged and/or colored, the experimental constraints are even stronger [36, 37]. Thus experimental constraints rule out the possibility that the lightest messenger is dark matter; this will be investigated further in [26].

We also note that the SM gauge couplings have a Landau pole well below the GUT scale, due to the presence of extra matter charged under the SM gauge group. As one runs up to the high scale, the $SU(3)_C$ gauge coupling blows up first at about 10^9 (10^7) GeV for $\tilde{N}_c = 1$ (3), so that new physics has to enter at or below this scale. Larger values of \tilde{N}_c lower this scale to the point that it affects our discussion materially. See [44] for a recent discussion of the Landau pole problem in ISS-like SUSY-breaking models.

6.4 Illustrative choices of parameters

We postpone a careful study of the various constraints to [26], but preliminarily it appears possible to satisfy simultaneously all of the conditions considered above. For example, for $\tilde{N}_c = 1$,⁵ the parameters of the electric theory eq. (2.2) that are consistent with (6.11) and (6.12) are m of order 0.01–10 TeV, $\Lambda \sim 10^{3-5}$ TeV, and $\Lambda_0 \sim 10^{6-9}$ TeV. With these choices, the models appear to have no insuperable problem below the scale of the Landau pole.

On the other hand, for $\tilde{N}_c \geq 3$, Λ has to be below 10^3 TeV, and the ratio m/Λ is not parametrically small. In this case, the corrections from the microscopic theory are not guaranteed to be small, and the violations of the approximate symmetries may be large. In particular, the cancellations described in section 4.2 may be imperfect, requiring a more elaborate analysis. However, the argument for nonzero γ still holds, and its effects can still dominate, in which case the phenomenology outlined here will be largely unchanged.

6.5 Summary

While these models are not yet entirely plausible, they represent an advance over the models with $SU(N_c)$ gauged and $\gamma = 0$, which as we showed are excluded by the presence of overly-light charged and colored fermions. We have demonstrated that with $\gamma \neq 0$, it is possible to obtain models with a long-lived metastable vacuum, a spectrum with all standard model superpartners in the TeV range, and with no obvious unresolvable conflict with any experiment.

The minimal versions of these models have new TeV-scale fermions in the adjoint representations of the Standard Model gauge group that do not mix with standard model gauginos. They also have squarks and sleptons significantly heavier than the gauginos, and exotic stable hadrons which must be made to decay through additional interactions. They also suffer from the ubiquitous intermediate-scale Landau pole for standard model gauge couplings. We will pursue various associated model-building issues, and study in more detail the phenomenology of these models in [26].

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⁵In this case, the magnetic gauge group is trivial and, after a field redefinition, the superpotential is given by (2.3) plus $\det \Phi/\Lambda^{N_c-2}$. For $N_c > 2$ this term is negligible near the origin, so our analysis is self-consistent.

A One loop calculations

In this appendix we collect the one loop calculations for the ISS model with multitrace quadratic deformations. The superpotential is

$$W = h \operatorname{tr} q \Phi \tilde{q} - h \mu^2 \operatorname{tr} \Phi + \frac{1}{2} h^2 \mu_\phi \operatorname{tr} \Phi^2 + \frac{1}{2} h^2 \mu_\phi \gamma (\operatorname{tr} \Phi)^2 \quad (\text{A.1})$$

where $\Phi = \Phi_{N_f \times N_f}$, $q = q_{\tilde{N}_c \times N_f}$ and $\tilde{q} = \tilde{q}_{N_f \times \tilde{N}_c}$.

A.1 Messenger sector

Let us consider separately the cases $k = N_f - N_c$ and $k < N_f - N_c$ (see section 4.1).

Case $k = N_f - N_c$. The parametrization of the metastable minima is given by eqs. (3.2) and (3.3). Around these minima the superpotential is

$$\begin{aligned} W = & h q_0 \tilde{q}_0 \operatorname{tr} Y - h \mu^2 \operatorname{tr} Y - h \mu^2 \operatorname{tr} X + h \operatorname{tr} q_0 Y \tilde{\chi} + h \tilde{q}_0 \operatorname{tr} \chi Y \\ & + h q_0 \operatorname{tr} Z \tilde{\rho} + h \tilde{q}_0 \operatorname{tr} \rho \tilde{Z} + \frac{1}{2} h^2 \mu_\phi (\operatorname{tr} Y^2 + \gamma (\operatorname{tr} Y)^2) + h^2 \mu_\phi \operatorname{tr} Z \tilde{Z} \\ & + \frac{1}{2} h^2 \mu_\phi (\operatorname{tr} X^2 + \gamma (\operatorname{tr} X)^2) + h^2 \mu_\phi \gamma \operatorname{tr} X \operatorname{tr} Y \\ & + h \operatorname{tr} \chi Y \tilde{\chi} + h \operatorname{tr} \rho X \tilde{\rho} + h \operatorname{tr} \rho \tilde{Z} \tilde{\chi} + h \operatorname{tr} \chi Z \tilde{\rho} \end{aligned} \quad (\text{A.2})$$

and the non-zero F-term is

$$\partial_{X_{ij}} W = (-h \mu^2 + h^2 \mu_\phi (1 + N_c \gamma) X_0) \delta_{ij}. \quad (\text{A.3})$$

We recall the ansatz (3.4),

$$\langle X \rangle = X_0 I_{N_c \times N_c}, \quad \langle \chi \rangle = q_0 I_{\tilde{N}_c \times \tilde{N}_c}, \quad \langle \tilde{\chi} \rangle = \tilde{q}_0 I_{\tilde{N}_c \times \tilde{N}_c}. \quad (\text{A.4})$$

The $q_0 \tilde{q}_0$ vev completely Higgses the dual gauge group $\text{SU}(\tilde{N}_c)_G$ and the $\text{U}(1)_V$. To determine X_0 , one must compute the Coleman-Weinberg potential from the tree level masses of the messenger sector. The ansatz (A.4), which will be checked self-consistently, simplifies the computations since the mass eigenstates are then independent of their flavor index. One can thus suppress color and flavor indices in the following.

The messenger sector contains the fields ρ , $\tilde{\rho}$, Z and \tilde{Z} , that couple to the non-zero F-term. Let us define

$$\hat{\psi} = (\psi_\rho \quad \psi_Z)^T \quad \hat{\tilde{\psi}} = (\psi_{\tilde{\rho}} \quad \psi_{\tilde{Z}})^T \quad \hat{\phi} = \left(\rho \quad Z \quad \tilde{\rho}^* \quad \tilde{Z}^* \right)^T \quad (\text{A.5})$$

for the messenger gauge eigenstates. The Weyl fermions combine into Dirac fermions and the messenger masses can be written as

$$\mathcal{L}_{mess, mass} = -\hat{\tilde{\psi}} M_{mess, f} \hat{\psi} - h.c. - \hat{\phi}^\dagger M_{mess, b}^2 \hat{\phi} \quad (\text{A.6})$$

where the messenger mass matrices are

$$M_{mess, f} = h \begin{pmatrix} X_0 & q_0 \\ \tilde{q}_0 & h \mu_\phi \end{pmatrix}, \quad M_{mess, b}^2 = \begin{pmatrix} M_{mess, f}^\dagger M_{mess, f} & -h^* F_X^* \\ -h F_X & M_{mess, f} M_{mess, f}^\dagger \end{pmatrix} \quad (\text{A.7})$$

and

$$-F_X^* = h \begin{pmatrix} -\mu^2 + h\mu_\phi(1 + N_c\gamma)X_0 & 0 \\ 0 & 0 \end{pmatrix}. \quad (\text{A.8})$$

For $\tilde{q}_0 = q_0$ the fermionic and bosonic messenger masses are ($\sigma = \pm 1$ and $\eta = \pm 1$)

$$m^2(X_0) = |h|^2 \left(|q_0|^2 + \frac{1}{2}|X_0|^2 + \frac{1}{2}|h\mu_\phi|^2 + \frac{1}{2}\sigma\sqrt{(|X_0|^2 - |h\mu_\phi|^2)^2 + 4|q_0X_0^* + q_0^*h\mu_\phi|^2} \right) \quad (\text{A.9})$$

$$\tilde{m}^2(X_0) = |h|^2 \left(|q_0|^2 + \frac{1}{2}|X_0|^2 + \frac{1}{2}|h\mu_\phi|^2 + \frac{1}{2}\eta|\mu^2 - h\mu_\phi(1 + N_c\gamma)X_0| + \frac{1}{2}\sigma\sqrt{(|X_0|^2 - |h\mu_\phi|^2 + \eta|\mu^2 - h\mu_\phi(1 + N_c\gamma)X_0|)^2 + 4|q_0X_0^* + q_0^*h\mu_\phi|^2} \right). \quad (\text{A.10})$$

The fermion masses have multiplicity $4N_c\tilde{N}_c$ while the complex boson masses have multiplicity $2N_c\tilde{N}_c$.

The messenger mass matrices can be diagonalized by unitary matrices U_f , \tilde{U}_f and U_b such that

$$\psi = U_f\hat{\psi} \quad \tilde{\psi} = \tilde{U}_f\hat{\tilde{\psi}} \quad \phi = U_b\hat{\phi} \quad (\text{A.11})$$

where ψ , $\tilde{\psi}$ and ϕ are messenger mass eigenstates. The quadratic lagrangian for the messengers is therefore of the canonical form

$$\mathcal{L}_{\text{mess}} = -\sum_{a=1}^4 \phi_a^\dagger (D^2 + \tilde{m}_a^2) \phi_a + \sum_{a=1}^2 \left(\bar{\psi}_a i\bar{\sigma}^\mu D_\mu \psi_a + \bar{\tilde{\psi}}_a i\bar{\sigma}^\mu D_\mu \tilde{\psi}_a - m_a(\tilde{\psi}_a \psi_a + \bar{\tilde{\psi}}_a \bar{\psi}_a) \right). \quad (\text{A.12})$$

Due to the charge conjugation symmetry, it is possible to write the mixing matrices such that $(U_b)_{a\{1,2\}} = (U_b)_{a\{3,4\}}^*$ and $\tilde{U}_f = U_f$. This can be easily seen from the mass matrices for $\tilde{q}_0 = q_0$. This property will be useful when computing one loop corrections to light masses.

Case $k < N_f - N_c$. The fluctuations are parametrized as in eq. (4.6), so there are extra messenger superfields $(\varphi, \tilde{\varphi})$. The analysis of $(\rho, \tilde{\rho}, Z, \tilde{Z})$ proceeds along the same lines as in the case $k = N_f - N_c$, except that the fermion messenger masses have now multiplicity $4(N_f - k)k$ while the complex boson messenger masses have multiplicity $2(N_f - k)k$.

The masses of φ and $\tilde{\varphi}$ are ($\eta = \pm 1$)

$$m_\varphi^2(X_0) = |hX_0|^2 \\ \tilde{m}_\varphi^2(X_0) = |h|^2 (|X_0|^2 + \eta|\mu^2 - h\mu_\phi X_0|). \quad (\text{A.13})$$

The fermion masses have multiplicity $4(N_f - k)(\tilde{N}_c - k)$ while the complex boson masses have multiplicity $2(N_f - k)(\tilde{N}_c - k)$. Importantly, in the limit of small deformation, (A.13) forces $|X_0| \gtrsim |\mu|$ to avoid tachyons.

A.2 One loop bosonic action

The tree level pseudo-moduli are given by X_0 and $\text{Re tr}(\chi - \tilde{\chi})$, and they are stabilized by one loop contributions. For $\mu_\phi \ll \mu$, the one loop effective potential for $\text{Re tr}(\chi - \tilde{\chi})$ is the same as in [5] (see eq. (3.11).) As a result, this field is stabilized at the origin and acquires a mass of order $|h^4 \mu^2|/(8\pi^2)$.

Let us now analyze the pseudo-modulus X_0 ; for $k \leq N_f - N_c$, this is a $(N_f - k) \times (N_f - k)$ matrix. The ISS-type vacua correspond to $k = N_f - N_c$. We will argue here that the new metastable vacua corresponding to the case $k < N_f - N_c$ do not exist, as they are located in a region where some of the fields become tachyonic. The only remaining metastable vacua will be the ISS-type vacua.

The one loop correction from integrating out the messenger fields is

$$V_{\text{CW}} = \frac{(N_f - k)k}{32\pi^2} \sum_{\sigma, \eta = \pm 1} \left[\tilde{m}(X_0)^4 \log \frac{\tilde{m}(X_0)^2}{\Lambda^2} - m(X_0)^4 \log \frac{m(X_0)^2}{\Lambda^2} \right] \quad (\text{A.14})$$

$$+ \frac{(N_f - k)(\tilde{N}_c - k)}{32\pi^2} \sum_{\eta = \pm 1} \left[\tilde{m}_\varphi(X_0)^4 \log \frac{\tilde{m}_\varphi(X_0)^2}{\Lambda^2} - m_\varphi(X_0)^4 \log \frac{m_\varphi(X_0)^2}{\Lambda^2} \right].$$

with masses given in section A.1. We find that the full potential

$$V = V_{\text{tree}} + V_{\text{CW}} \quad (\text{A.15})$$

has a metastable vacuum if $k = N_f - N_c$, but there are no metastable vacua for $k < N_f - N_c$. Let us discuss in more detail how this occurs.

For $k = N_f - N_c$, the messengers are non-tachyonic for any X_0 ; see eq. (A.9). As explained in section 4.1, the metastable vacuum appears because quantum corrections at small X_0 are large enough to overwhelm the slope of the classical potential, which would otherwise push X_0 toward the supersymmetric vacua. The supersymmetry breaking vacuum is located in the range $|X_0/\mu| \lesssim 1$, far from the supersymmetric vacuum.

The situation for $k < N_f - N_c$ is very different, because the messengers ($\varphi, \tilde{\varphi}$) are tachyonic at small X_0 ; see eq. (A.13). For $|X_0/\mu| \gtrsim 1$ these tachyons are absent, but in this regime the one loop corrections $V_{\text{CW}}(X_0)$ grow only logarithmically with $|X_0|$, and cannot compete with the classical potential to create a metastable vacuum. One may directly check that the Hessian of the potential always has a negative eigenvalue for $|X_0| \gtrsim |\mu|$ (and all values of k). Notice that if one used the quadratic expansion of V_{CW} around the origin $X_0/\mu = 0$, instead of the full logarithmic form, it would suggest the existence of metastable vacua with $k < N_f - N_c$ and $|X_0/\mu| \sim 1$ [16]. But this approximation is inconsistent, and when the full logarithmic dependence of V_{CW} is included, these vacua become unstable and disappear.

Summarizing, only the ISS-type minima with $k = N_f - N_c$ survive, and the adjoint (X') and singlet ($\text{tr } X$) components of the pseudo-modulus X acquire one loop masses

$$m_{X'}^2 \approx b|h^2\mu|^2 + |h^2\mu_\phi|^2 \quad (\text{A.16})$$

$$m_{\text{tr } X}^2 \approx b|h^2\mu|^2 + |h^2\mu_\phi(1 + N_c\gamma)|^2. \quad (\text{A.17})$$

The R-axion, discussed in section 5.1, has a mass of this same order, eq. (5.7). All bosons which were light at tree level thus become heavy at one loop, with masses of order $m_{\text{CW}} = \sqrt{b} |h^2 \mu|$.

A.3 One loop fermionic action

In this section we discuss the low energy fermionic spectrum of the theory, taking into account one loop effects.

Goldstino. At one loop, the Goldstino appears as a combination of $\psi_{\text{tr} X}$, $\psi_{\text{tr} Y}$ and $\psi_{\text{tr}(\chi+\tilde{\chi})}$, which we now determine. The charge conjugation symmetry forbids mixings with $\psi_{\text{tr}(\chi-\tilde{\chi})}$, which is eaten by the $U(1)_V$ gauge fermion and has mass $g_V \mu$.

First, at tree level, in the limit $\mu_\phi = 0$, $\psi_{\text{tr} Y}$ and $\psi_{\text{tr}(\chi+\tilde{\chi})}$ form a Dirac fermion of mass $h\mu$, while $\psi_{\text{tr} X}$ is massless; see eq. (A.2). When μ_ϕ and γ are nonzero, $\psi_{\text{tr} X}$ acquires a mass term proportional to μ_ϕ , and there is a $\psi_{\text{tr} X}$ - $\psi_{\text{tr} Y}$ mixing of order $\gamma\mu_\phi$. There is no linear combination of the fields $\psi_{\text{tr} Y}$, $\psi_{\text{tr}(\chi+\tilde{\chi})}$ and $\psi_{\text{tr} X}$ that is massless at tree level.

Once one loop effects are taken into account, supersymmetry is spontaneously broken, so we should get a massless Goldstino. Since the dominant F-term comes from $F_{\text{tr} X}$, the Goldstino will be approximately aligned with $\psi_{\text{tr} X}$. Indeed, the tree level plus one loop $\psi_{\text{tr} X} \psi_{\text{tr} X}$ mass element is (using the messenger mass eigenbasis),

$$m_{\psi_{\text{tr} X}} = h^2 \mu_\phi (1 + N_c \gamma) - \frac{2h^2 \tilde{N}_c}{16\pi^2} \sum_{j=1}^4 \sum_{k=1}^2 (U_f^*)_{k1} (\tilde{U}_f^*)_{k1} (U_b^*)_{j1} (U_b)_{j3} I[\tilde{m}_j, m_k] \quad (\text{A.18})$$

where the sums are over messenger fields and

$$I(\tilde{m}_j, m_k) = m_k \left[\ln \left(\frac{\Lambda^2}{m_k^2} \right) - \frac{\tilde{m}_j^2}{\tilde{m}_j^2 - m_k^2} \ln \left(\frac{\tilde{m}_j^2}{m_k^2} \right) \right]. \quad (\text{A.19})$$

It can be checked that the tree and one loop terms in (A.18) largely cancel, leaving only a term of order $\mu_\phi/(16\pi^2)$, of the same size as two loop corrections.

There are also one loop mixings between $\psi_{\text{tr} X}$ and $\psi_{\text{tr} Y}$, $\psi_{\text{tr}(\chi+\tilde{\chi})}$. For simplicity, let us consider first the ISS model, corresponding to the limit $\mu_\phi = 0$. The mass-mixing comes from the two-point function $\psi_{\text{tr} X} \psi_{\text{tr}(\chi+\tilde{\chi})}$, which is allowed by R-symmetry. A calculation along the same lines as in (A.18) shows that this mass-mixing is of order $\mu/(16\pi^2)$. The Goldstino is hence predominantly in the $\psi_{\text{tr} X}$ direction, with a small (of order $1/(16\pi^2)$) component along $\psi_{\text{tr} Y}$. This implies that in ISS, one loop corrections generate a nonzero F-term

$$|F_{\text{tr} Y}| \sim \frac{|F_{\text{tr} X}|}{16\pi^2}.$$

For μ_ϕ/μ nonzero but small, the Goldstino also has a small component along $\psi_{\text{tr}(\chi+\tilde{\chi})}$, with mixing angle of order $|X_0/(16\pi^2 \mu)|$. This is smaller than the mixing of $\psi_{\text{tr} X}$ and $\psi_{\text{tr} Y}$, and is consistent with a one loop F-term

$$|F_{\text{tr}(\chi+\tilde{\chi})}| \sim \left| \frac{X_0}{16\pi^2 \mu} \right| |F_{\text{tr} X}|.$$

Gauginos and the fermions $\psi_{X'}$. There are no mixings between the gauginos and the $\psi_{X'}$ fermions at one and two loops, because they are forbidden by charge conjugation. The expression for the one loop gaugino mass is

$$m_\lambda = \frac{2g^2\tilde{N}_c}{16\pi^2} \sum_{c=1}^2 \sum_{d=1}^2 \sum_{j=1}^4 \sum_{k=1}^2 (U_f^*)_{kc} (\tilde{U}_f^*)_{k,d} (U_b)_{jc} (U_b^*)_{j,d+2} I[\tilde{m}_j, m_k]. \quad (\text{A.20})$$

which is of order $g^2\mu_\phi$. The one loop computation for the masses of $\psi_{X'}$ is nearly identical to that of $\psi_{\text{tr}X}$, given in (A.18), since they have the same interactions with the messenger fields. The result is

$$m_{\psi_{X'}} = h^2\mu_\phi - \frac{2h^2\tilde{N}_c}{16\pi^2} \sum_{j=1}^4 \sum_{k=1}^2 (U_f^*)_{k1} (\tilde{U}_f^*)_{k1} (U_b^*)_{j1} (U_b)_{j3} I[\tilde{m}_j, m_k] \quad (\text{A.21})$$

The cancellation that occurs in (A.18) occurs here as well, but leaves over a large remainder, of order $|\gamma\mu_\phi|$.

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