

## THE DIFFUSE GAMMA-RAY BACKGROUND FROM TYPE Ia SUPERNOVAE

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### ABSTRACT

The origin of the diffuse extragalactic gamma-ray background (EGB) has been intensively studied but remains unsettled. Current popular source candidates include unresolved star-forming galaxies, starburst galaxies, and blazars. In this paper, we calculate the EGB contribution from the interactions of cosmic rays accelerated by Type Ia supernovae (SNe), extending earlier work that only included core-collapse SNe. We consider Type Ia events not only in star-forming galaxies, but also in quiescent galaxies that lack star formation. In the case of star-forming galaxies, consistently including Type Ia events makes little change to the star-forming EGB prediction, so long as both SN types have the same cosmic-ray acceleration efficiencies in star-forming galaxies. Thus, our updated EGB estimate continues to show that star-forming galaxies can represent a substantial portion of the signal measured by *Fermi*. In the case of quiescent galaxies, conversely, we find a wide range of possibilities for the EGB contribution. The dominant uncertainty we investigated comes from the mass in hot gas in these objects, which provides targets for cosmic rays; total gas masses are as yet poorly known, particularly at larger radii. Additionally, the EGB estimation is very sensitive to the cosmic-ray acceleration efficiency and confinement, especially in quiescent galaxies. In the most optimistic allowed scenarios, quiescent galaxies can be an important source of the EGB. In this case, star-forming galaxies and quiescent galaxies together will dominate the EGB and leave little room for other contributions. If other sources, such as blazars, are found to have important contributions to the EGB, then either the gas mass or cosmic-ray content of quiescent galaxies must be significantly lower than in their star-forming counterparts. In any case, improved *Fermi* EGB measurements will provide important constraints on hot gas and cosmic rays in quiescent galaxies.

*Key words:* cosmic rays – gamma rays: diffuse background – gamma rays: galaxies – supernovae: general

*Online-only material:* color figures

### 1. INTRODUCTION

The first observation of the diffuse extragalactic gamma-ray background (EGB) was reported by the SAS-2 satellite (Fichtel et al. 1977, 1978). Recently, the *Fermi Gamma-ray Space Telescope* updated the EGB determination from the *Energetic Gamma-ray Experiment Telescope* (Sreekumar et al. 1998) and provided the most reliable EGB observations so far (Abdo et al. 2009a). Measurements of EGB are model dependent in that they require subtraction of the large foreground emission from our Galaxy (e.g., Hunter et al. 1997). The accuracy of the EGB measurement thus greatly depends on our understanding of the Galactic emission. Despite the difficulty in its observation, the EGB encodes important information about the highest-energy environments in the cosmos.

The EGB arises from the combination of all the unresolved extragalactic gamma-ray sources (e.g., Dermer 2007b; Stecker & Venters 2011). “Guaranteed” EGB components arise from unresolved counterparts of known extragalactic populations, namely, blazars (those active galactic nuclei that have their relativistic jets pointing at us, e.g., Padovani et al. 1993; Stecker et al. 1993; Mukherjee & Chiang 1999; Pavlidou & Venters 2008; Dermer 2007a; Venters 2010; Venters & Pavlidou 2011; Inoue & Totani 2009), as well as normal star-forming galaxies and starburst galaxies (e.g., Pavlidou & Fields 2001, 2002; Prodanović & Fields 2006; Thompson et al. 2007; Stecker 2007; Fields et al. 2010; Makiya et al. 2011). Additional EGB

contributions might arise from more exotic sources, such as dark matter annihilation (Silk & Srednicki 1984; Rudaz & Stecker 1991), annihilations at the boundaries of cosmic matter and antimatter domains (Stecker et al. 1971), massive black holes at redshifts of  $z \sim 100$  (Gnedin & Ostriker 1992), and primordial black hole evaporation (Page & Hawking 1976).

In this paper, we will focus on the EGB contribution from both star-forming galaxies and quiescent galaxies. Quiescent galaxies refer to galaxies with little or no active star formation, and these objects have not been included in EGB estimations. In terms of galaxy types, quiescent galaxies usually include all elliptical galaxies and some S0 galaxies. However, the important factor for the EGB estimation is not the galaxy type but the amount of star formation. Therefore, we will separately consider star-forming and quiescent galaxies, and assume no star formation in quiescent galaxies. We will not consider the EGB contribution from starburst galaxies in this paper, due to the larger uncertainty in the cosmic-ray propagation in such galaxies (e.g., Thompson et al. 2007; Lacki et al. 2011). Also, recent work suggests that starburst galaxies only have small contribution to the EGB (Stecker & Venters 2011). We follow the criterion adopted in Fields et al. (2010) to distinguish star-forming and starburst galaxies. The EGB energy range we consider in this paper is from  $\sim 30$  MeV to  $\sim 30$  GeV, which is the energy range covered by *Fermi* data and includes the regime in which star-forming galaxies may contribute substantially to the EGB.

Our focus here is on the EGB contribution arising from hadronic cosmic-ray interactions with the interstellar medium (ISM) of their host galaxies, specifically pion production and decay  $pp \rightarrow \pi^0 \rightarrow \gamma\gamma$ . The most favored possibility of the cosmic-ray production sites in galaxies is supernovae (SNe).

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*Fermi* and air Čerenkov observations detect individual remnants of both core-collapse (hereafter CC; Abdo et al. 2010; Acciari et al. 2010; Weekes et al. 1989) and Type Ia events (Acciari et al. 2011; Acero et al. 2010). The energetics of these objects are consistent with the requirements of efficient cosmic-ray acceleration (e.g., Abdo et al. 2010; Reynolds & Ellison 1992), and the GeV spectra of these objects are consistent with pionic emission and thus hadronic acceleration (e.g., Abdo et al. 2009b; Tanaka et al. 2011; Ellison et al. 2011). Diffuse Galactic emission is similarly consistent with pionic emission dominating (Abdo et al. 2009a, 2009c). These data thus give empirical grounding to the long-held belief that SNe of all types are the dominant engines that accelerate Galactic cosmic rays (e.g., Baade & Zwicky 1934; Ginzburg & Syrovatskii 1964; Ellison et al. 1997). We are thus interested in SNe of both types, all of which accelerate cosmic rays in their host galaxies.

Many groups have studied the EGB emission from cosmic rays accelerated by SNe in star-forming galaxies (e.g., Dar & Shaviv 1995; Prodanović & Fields 2006; Fields et al. 2010; Stecker & Venters 2011; Makiya et al. 2011). Some estimations suggest that star-forming galaxies can be the dominant source of the EGB (Fields et al. 2010), while other groups predict that a major contribution of the EGB comes from blazars (Stecker & Venters 2011; Makiya et al. 2011; Inoue & Totani 2009). However, there exist large uncertainties from the source inputs. Most of the analyses regarding star-forming galaxies focused on the EGB contribution from cosmic rays accelerated by CC SNe and implicitly assume that *only* these events accelerate cosmic rays. We extend the analysis of the EGB from star-forming galaxies in Fields et al. (2010) to include Type Ia SNe as accelerators in the Milky Way and in other galaxies.

CC SNe arise in massive stars with short lifetimes, and thus trace ongoing star formation. In contrast, Type Ia SNe result from thermonuclear runaway of white dwarfs accreting mass from their companion stars and hence are related to star formation with some delay time. For this reason, observations have shown that Type Ia SNe exist in both star-forming galaxies and quiescent galaxies, while CC SNe are rarely seen in quiescent galaxies (Filippenko 2001; Mannucci et al. 2005). Observations have suggested that the intrinsic cosmic CC SN rate is about five times higher than the intrinsic cosmic Ia SN rate at redshift  $z < 0.4$  (Bazin et al. 2009). Also, studies suggest that the Ia rate in a star-forming galaxy is much larger than that in a quiescent galaxy; this reflects the distribution of delay times between progenitor birth and Ia explosion, which is weighted toward short delays (Mannucci et al. 2005; Sullivan et al. 2006).

The efficiency of cosmic-ray acceleration by SNe remains poorly understood but is crucial for understanding cosmic-ray acceleration physics as well as SN energy feedback. Theories propose that cosmic rays are produced by diffusive shock acceleration in the blast waves from SN explosions (e.g., Schlickeiser 1989; Berezhko & Ellison 1999). Current studies suggest that  $\sim 30\%$  of the initial kinetic energy from an SN needs to be transferred to cosmic-ray acceleration if we assume that SNe are the dominant sources for cosmic-ray production and the nucleosynthesis of lithium, beryllium, and boron in the Milky Way (Fields et al. 2001). Also, some theoretical predictions expect the cosmic-ray acceleration efficiency in quiescent galaxies is much lower than in star-forming galaxies. Dorfi & Voelk (1996) suggest that only  $\lesssim 1\%$  of the total explosion energy goes into cosmic-ray energy in quiescent galaxies. This is because an SN blast will have weaker shocks

due to the large sound speeds of the hot, low-density ISM in an elliptical galaxy.

Understanding the SN rate and their efficiency in producing cosmic rays is critical for studying the EGB contributions from these galaxies. Our observational understanding of cosmic SNe will increase significantly when the next generation optical survey telescope, the Large Synoptic Survey Telescope (LSST), comes online during the next decade. LSST is planning to scan the whole available sky, repeated every  $\sim 3$  days, with unprecedented survey sensitivity (Ivezic et al. 2008). The project will observe  $\sim 10^5$  CC SNe per year out to redshift  $z \sim 1$  (Lien & Fields 2009) and  $\sim 5 \times 10^4$  Type Ia events out to redshift  $z \sim 0.8$  (Bailey et al. 2009). The cosmic SN rate in different galaxy classes can thus be measured via *direct counting* to high redshift with extremely low statistical uncertainty.

In this paper, we will first describe the general formalism of estimating the EGB from cosmic rays accelerated by SNe in both star-forming and quiescent galaxies (Section 2). We will then discuss the cosmic Type Ia rate in each galaxy classification that will be used in our EGB analysis (Section 3). The estimations of the EGB contribution from Type Ia SNe in star-forming and quiescent galaxies are presented in Sections 4 and 5, respectively. Additionally, we discuss the uncertainties in the EGB predictions in Section 6. Finally, we summarize the results in Section 7.

## 2. GENERAL FORMALISM

The formalism we adopt generalizes that of Fields et al. (2010) to account for both SN types. Integration of the gamma-ray contributions from each unresolved extragalactic source over the line of sight to the cosmic horizon gives the well-known express for the EGB intensity,

$$\frac{dI}{dE} = \frac{c}{4\pi} \int \mathcal{L}_\gamma(E_{\text{em}}, z) (1+z) \left| \frac{dt}{dz} \right| dz, \quad (1)$$

where  $\mathcal{L}_\gamma(E_{\text{em}}, z) = dN_{\text{gamma}}/dV_{\text{com}} dt_{\text{em}} dE_{\text{em}}$  is the comoving luminosity density (or emissivity) at rest-frame energy  $E_{\text{em}}$ , and  $|dt/dz| = [(1+z)H(z)]^{-1} = [(1+z)H_0\sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}]^{-1}$  for the standard  $\Lambda$ CDM cosmology. We use  $\Omega_m = 0.27$ ,  $\Omega_\Lambda = 0.73$ , and  $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$  from the seven-year *Wilkinson Microwave Anisotropy Probe* (WMAP) data (Komatsu et al. 2011).

Because the pionic gamma-ray emission is produced from the interaction between cosmic rays and the hydrogen atoms in the ISM of each galaxy, the luminosity density is given by the product,

$$\mathcal{L}_\gamma = \langle L_\gamma n_{\text{gal}} \rangle, \quad (2)$$

of the pionic gamma-ray luminosity  $L_\gamma$  of an individual galaxy times the galaxy number density, appropriately averaged. Our problem then divides into two parts. First, we must express a galaxy's gamma-ray luminosity  $L_\gamma$  in terms of galaxy properties, such as SN rate and gas content, and relate these to galaxy observables. Then we must construct a luminosity function  $dn_{\text{gal}}/dL_\gamma$  for gamma-ray-emitting galaxies.

We first turn to the pionic gamma-ray luminosity from an individual galaxy. This can be written as

$$L_\gamma(E_{\text{em}}) = \int \Gamma_{\pi^0 \rightarrow \gamma\gamma}(E_{\text{em}}) n_{\text{H}} dV_{\text{ISM}} \quad (3)$$

$$= \Gamma_{\pi^0 \rightarrow \gamma\gamma}(E_{\text{em}}) \mathcal{N}_{\text{H}}, \quad (4)$$

where  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}(E_{\text{em}})$  represents a spatial average of the gamma-ray production rate per interstellar hydrogen atom. The total number  $\mathcal{N}_{\text{H}} = \int n_{\text{H}} dV_{\text{ISM}}$  of hydrogen atoms in a galaxy is obtained by integrating the number density of hydrogen atom  $n_{\text{H}}$  over the ISM volume.  $\mathcal{N}_{\text{H}}$  is proportional to the total gas mass  $M_{\text{gas}}$  in a galaxy and can therefore be expressed as  $\mathcal{N}_{\text{H}} = X_{\text{H}} M_{\text{gas}} / m_p$ , where  $X_{\text{H}}$  is the mass fraction of hydrogen atoms and  $m_p$  is the proton mass.

We take SNe (of both types) to be the engines of cosmic-ray acceleration; this implies that the cosmic-ray flux scales as  $\Phi_{\text{cr}} \propto \Lambda_{\text{esc}} R_{\text{SN,eff}}$ . Here,  $R_{\text{SN,eff}}$  is an effective SN rate weighted by the cosmic-ray acceleration efficiency  $\epsilon$ , discussed below.  $\Lambda_{\text{esc}}$  is the escape path length, which quantifies the cosmic-ray confinement in a galaxy. In this paper, we assume  $\Lambda_{\text{esc}}$  to be universal and constant, which leads to a universal galactic cosmic-ray spectrum that is the same as that of the Milky Way. Thus, the pionic gamma-ray production rate per hydrogen atom in a galaxy should scale as  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}(E_{\text{em}}) \propto \Phi_{\text{cr}} \propto \Lambda_{\text{esc}} R_{\text{SN,eff}}$ . We normalize the cosmic-ray spectrum to a known galaxy, which would be the Milky Way in our case, finding

$$\frac{\Gamma_{\pi^0 \rightarrow \gamma\gamma}(E_{\text{em}})}{\Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}})} = \frac{\Phi_{\text{cr}}}{\Phi_{\text{cr}}^{\text{MW}}} = \frac{R_{\text{SN,eff}}}{R_{\text{SN,eff}}^{\text{MW}}}. \quad (5)$$

The pionic gamma-ray luminosity of a particular galaxy is thus

$$L_{\gamma}(E_{\text{em}}) = \Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}}) \frac{R_{\text{SN,eff}}}{R_{\text{SN,eff}}^{\text{MW}}} X_{\text{H}} \frac{M_{\text{gas}}}{m_p}. \quad (6)$$

Because of their short lifespans, the rate of CC SNe (and short-delay Ia events) traces that of star formation:  $R_{\text{SN}} \propto \psi$ . Thus, we expect a star-forming galaxy's gamma-ray luminosity to scale as  $L_{\gamma} \propto M_{\text{gas}} R_{\text{SN}} \propto M_{\text{gas}} \psi$ . The new class of *Fermi*-detected star-forming galaxies is consistent with this trend (Lenain & Walter 2011).

This pionic gamma-ray spectrum always has a peak at  $E_{\text{em}} = m_{\pi^0}/2$ , at which the two gamma-ray photons inherit the rest-mass energy of the decayed  $\pi^0$  (Stecker 1971). At large energy, the spectrum shows the same asymptotic index as that of the cosmic-ray spectrum, which we take to be 2.75.

Both CC and Type Ia events should produce cosmic rays and hence pionic gamma rays. Therefore, the effective SN rate  $R_{\text{SN,eff}}$  in Equation (6) is a combination of the effective Type Ia rate  $R_{\text{Ia,eff}} \equiv \epsilon_{\text{Ia}} R_{\text{Ia}}$  and the effective CC SN rate  $R_{\text{CC,eff}} \equiv \epsilon_{\text{CC}} R_{\text{CC}}$ , where  $\epsilon_{\text{Ia}}$  and  $\epsilon_{\text{CC}}$  are the cosmic-ray production efficiencies of Type Ia and CC SNe, respectively. There exist different definitions of the cosmic-ray acceleration efficiency in current literature. For example, some studies present the efficiency as the fraction of the total cosmic-ray production energy out of the total kinetic energy output from an SN (e.g., Dorfi & Voelk 1996; Fields et al. 2001; Helder et al. 2010), while other studies define the parameter as the percentage of the energy flux that becomes relativistic particles after crossing the shock (e.g., Ellison et al. 2007). Most of these definitions describe the fraction of the SN explosion energy transferred to cosmic rays. Here, we define the cosmic-ray acceleration efficiency  $\epsilon$  to be the ratio of the SN baryonic explosion energy  $E_{\text{SN}}$  to the resulting cosmic-ray energy  $E_{\text{cr}}$ , i.e.,  $\epsilon = E_{\text{cr}}/E_{\text{SN}}$ . Therefore, if we assume that all SNe have the same explosion energy and the produced cosmic rays have the same energy spectrum, the cosmic-ray acceleration efficiency will be proportional to the total cosmic-ray production in a galaxy over the SN rate in that galaxy, i.e.,  $\epsilon \propto \Phi_{\text{cr}}/(\Lambda_{\text{esc}} R_{\text{SN}})$ . For the Milky Way, then, we have  $R_{\text{SN,eff}}^{\text{MW}} = \epsilon_{\text{Ia,MW}} R_{\text{Ia}}^{\text{MW}} + \epsilon_{\text{CC,MW}} R_{\text{CC}}^{\text{MW}}$ .

Since we normalized our prediction to the gamma-ray production in the Milky Way (Equation (6)), the important factor in the calculation is not the absolute value of  $\epsilon$ , but the difference between the acceleration efficiency  $\epsilon$  in different SN types (Ia and CC) and galaxy classes (quiescent and star-forming). Specifically, we will need to specify the ratios  $\epsilon_{\text{Ia}}/\epsilon_{\text{CC}}$  and  $\epsilon_{\text{Q}}/\epsilon_{\text{S}}$ . Unfortunately, these two fractions are poorly known. Thus for our fiducial numerical results, we will take  $\epsilon_{\text{Ia}}/\epsilon_{\text{CC}} = 1$  and  $\epsilon_{\text{Q}}/\epsilon_{\text{S}} = 1$ . Furthermore, we are unaware of any evidence for a substantial difference between the cosmic-ray acceleration efficiencies between Ia and CC SNe, and thus we will hereafter drop the Ia and CC notation in the acceleration efficiency to simplify the discussion. However, we will retain the notations of the acceleration efficiencies for different galaxy type  $\epsilon_{\text{Q}}$  and  $\epsilon_{\text{S}}$  in our formalism as an explicit reminder that the efficiencies are likely to depend on galaxy environment, as expected by some theoretical analyses (Dorfi & Voelk 1996; Hein & Spanier 2008). Further possibilities of choosing different cosmic-ray acceleration efficiencies will be discussed in Section 6.2.

Star-forming galaxies contain both Type Ia and CC SNe. Their pionic gamma-ray luminosity density  $\mathcal{L}_{\gamma,S}$  can be calculated by averaging over the galaxy density  $n_{\text{galaxy}}$ ,

$$\mathcal{L}_{\gamma,S} = \Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}}) \frac{X_{\text{H}}}{m_p} \times \frac{\langle M_{\text{gas}} \epsilon_{\text{S}} R_{\text{Ia,S}} n_{\text{galaxy}} \rangle + \langle M_{\text{gas}} \epsilon_{\text{S}} R_{\text{CC}} n_{\text{galaxy}} \rangle}{\epsilon_{\text{MW}} R_{\text{Ia}}^{\text{MW}} + \epsilon_{\text{MW}} R_{\text{CC}}^{\text{MW}}}. \quad (7)$$

In quiescent galaxies, there is almost no star formation. We will assume the star formation rate (and thus the CC SN rate) to be zero in a quiescent galaxy. However, Type Ia SNe do exist in quiescent galaxies because these events occur some time after the star formation. Therefore, the pionic gamma-ray luminosity density in quiescent galaxies  $\mathcal{L}_{\gamma,Q}$  only comes from Type Ia events,

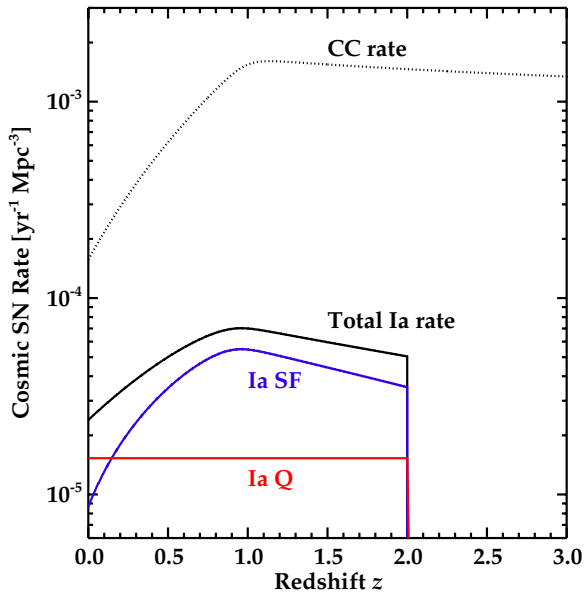
$$\mathcal{L}_{\gamma,Q} = \frac{\Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{Q0}}(E_{\text{em}})}{\epsilon_{\text{Q0}} R_{\text{Ia}}^{\text{Q0}}} \frac{X_{\text{H}}}{m_p} \langle M_{\text{gas}} \epsilon_{\text{Q}} R_{\text{Ia,Q}} n_{\text{galaxy}} \rangle. \quad (8)$$

$\Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{Q0}}(E_{\text{em}})$  and  $R_{\text{SN}}^{\text{Q0}}$  are the gamma-ray production rate and Type Ia event rate in a standard quiescent galaxy Q0 for normalization. However, since no gamma-ray emission from a (jet-less) quiescent galaxy has ever been measured, we will still adopt the values of the Milky Way and estimate the gamma-ray luminosity density for quiescent galaxies as

$$\mathcal{L}_{\gamma,Q} = \Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}}) \frac{X_{\text{H}}}{m_p} \frac{\langle M_{\text{gas}} \epsilon_{\text{Q}} R_{\text{Ia,Q}} n_{\text{galaxy}} \rangle}{\epsilon_{\text{MW}} R_{\text{Ia}}^{\text{MW}} + \epsilon_{\text{MW}} R_{\text{CC}}^{\text{MW}}}. \quad (9)$$

Note that since the gamma-ray production from the Milky Way comes from both Type Ia and CC SNe,  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}})$  needs to be normalized to the total SN rate in the Milky Way instead of just the Type Ia rate.

The total pionic gamma-ray luminosity density will be a combination of emissions from both star-forming and quiescent galaxies, that is,  $\mathcal{L}_{\gamma,\text{tot}} = \mathcal{L}_{\gamma,S} + \mathcal{L}_{\gamma,Q}$ . The EGB contribution from cosmic rays accelerated by CC SNe has been carefully examined in Fields et al. (2010) and by other groups (e.g., Stecker & Venters 2011; Makiya et al. 2011). Here, we will focus on the EGB contributions related to Type Ia events. In our



**Figure 1.** Adopted cosmic SN rate. The solid black curve plots the total cosmic Type Ia rate; blue curve plots the cosmic Ia rate in star-forming galaxies; red curve plots the cosmic Ia rate in quiescent galaxies. The cosmic CC SN rate is plotted as dotted black curve for comparison.

(A color version of this figure is available in the online journal.)

calculation, we do not include the intergalactic EGB absorption  $\gtrsim 30$  GeV (Salamon & Stecker 1998).

### 3. THE COSMIC TYPE Ia SUPERNOVA RATE IN STAR-FORMING AND QUIESCENT GALAXIES

Type Ia SNe do not all trace ongoing star formation, because these events have different origins from CC SNe. The prevailing scenarios for Type Ia SN origin include merging of two white dwarfs (double degenerate; Webbink 1984), or a white dwarf accreting from mass overflow of its supergiant companion (single degenerate; Nomoto et al. 1984; Iben & Tutukov 1984). Both of these scenarios involve white dwarfs merging in a binary system, and thus Type Ia SNe are delayed from the formation of the progenitor stars. For this reason, Type Ia SNe are found in all galaxies, including the quiescent galaxies where there is no longer star-forming activity. A complete account of the Type Ia SN contribution to the EGB must therefore include contributions from events in star-forming and quiescent galaxies.

There are many studies of the comoving cosmic Ia rate density  $\mathcal{R}_{\text{Ia}} = dN_{\text{Ia}}/(dV_{\text{com}}dt)$  as a function of redshift, most of which focus on the distribution of delay times (e.g., Scannapieco & Bildsten 2005; Sullivan et al. 2006; Kuznetsova et al. 2008; Dilday et al. 2010b; Horiuchi & Beacom 2010; Graur et al. 2011). Our adopted total (all-galaxy) cosmic Type Ia rate is based on current observational data. To find this we use the best-fit redshift and delay-time distribution of Horiuchi & Beacom (2010), integrated over all delay times (black curve in Figure 1). Although the number of observed cosmic Ia events is rapidly increasing, the data remain sparse beyond  $z \sim 1$ , where the rates are thus poorly constrained.

The cosmic Ia rate in different galaxy classes (i.e., star-forming and quiescent galaxies) as a function of redshift is still poorly understood. In our calculation, we adopt a constant value for the cosmic Ia rate in quiescent galaxies out to redshift  $z \sim 2$  (red curve in Figure 1). We use a normalization based

on observations of Ia rate per stellar mass in quiescent galaxies provided by Sullivan et al. (2006) and a non-evolving stellar-mass function from Pannella et al. (2009; see detailed discussion in Section 5). Recently, Type Ia SNe have been observed in galaxy clusters. The observed Ia rates show little redshift evolution within  $z \lesssim 1$  (Gal-Yam et al. 2002; Sharon et al. 2007; Graham et al. 2008; Mannucci et al. 2008; Dilday et al. 2010a; Sharon et al. 2010). Since galaxy clusters are mostly composed of quiescent galaxies, these results are consistent with our assumption of a constant Ia rate in quiescent galaxies. Moreover, these measurements show that Ia rate in clusters is  $\sim 10^{-13} \text{ yr}^{-1} M_{\odot}^{-1}$ , which is very similar to the value we adopted from Sullivan et al. (2006).<sup>3</sup> However, while we expect a roughly constant cosmic Ia rate in quiescent galaxies for moderate redshift, this trend must fail at some redshift. To be conservative, we therefore placed an artificial cutoff of the cosmic Type Ia rate at  $z = 2$ , beyond which uncertainties in the cosmic Type Ia rate observations remain substantial.

The cosmic Ia rate in star-forming galaxies (blue curve in Figure 1) can thus be obtained by subtracting the cosmic Type Ia rate in quiescent galaxies (red curve in Figure 1) from the total cosmic Ia rate (black curve in Figure 1).

Figure 1 shows the adopted cosmic Ia SN rate as a function of redshift. Although the uncertainty in the rate increases significantly at higher redshift, most of the EGB from Type Ia SNe, like that from CC SNe, arises from events at lower redshift ( $z \lesssim 1$ ; Ando & Pavlidou 2009). For example, in our calculation  $\sim 50\%$  ( $\sim 70\%$ ) of the EGB flux comes from sources within  $z \leq 1$  ( $z \leq 1.3$ ). Therefore, the choice of the Type Ia rate at  $z \gtrsim 1$  only has a small effect on the final estimation of the EGB. The solid black curve plots the total cosmic Ia SN rate in both star-forming and quiescent galaxies. The red curve shows the cosmic Ia SN rate in only quiescent galaxies. The blue curve represents the cosmic Ia SN rate in only star-forming galaxies.

Figure 1 also shows the cosmic CC SN rate (dotted black curve), which is higher than the Ia rate by a factor  $\sim 5$  at  $z \sim 0$  and increase to a factor of  $\sim 10$  at  $z \sim 1$ . This immediately suggests that we should expect CC events to dominate the star-forming EGB signal, with the Ia contribution at a  $\lesssim 20\%$  level. We will see that this is roughly the case for the Ia contribution from star-forming galaxies, but for Ia events in quiescent galaxies the situation is much more uncertain.

### 4. THE EXTRAGALACTIC GAMMA-RAY BACKGROUND FROM TYPE Ia SUPERNOVAE IN STAR-FORMING GALAXIES

As described in Section 2, the EGB luminosity density  $\mathcal{L}_{\gamma,S}^{\text{Ia}}$  is dominated by two physics inputs: the SN rate in a galaxy, which is associated with the amount of cosmic rays, and the total gas mass of that galaxy, which accounts for the total hydrogen targets that interact with the cosmic rays. To reflect these two physics inputs, we follow the approach adopted in Fields et al. (2010) and rewrite the EGB contribution from Type Ia events (the first term in Equation (7)) as below,

$$\mathcal{L}_{\gamma,S}^{\text{Ia}} = \frac{\epsilon_S \mathcal{R}_{\text{Ia},S}}{\epsilon_{\text{MW}} R_{\text{Ia}}^{\text{MW}} + \epsilon_{\text{MW}} R_{\text{CC}}^{\text{MW}}} \Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}}) \frac{X_{\text{H}}}{m_p} \langle M_{\text{gas},S} \rangle, \quad (10)$$

<sup>3</sup> We are greatly thankful for the anonymous referee for pointing out the measurements of Ia rate in galaxy clusters.

where

$$\langle M_{\text{gas,S}} \rangle \equiv \frac{\langle M_{\text{gas,S}} R_{\text{Ia,S}} n_{\text{galaxy,S}} \rangle}{\langle R_{\text{Ia,S}} n_{\text{galaxy,S}} \rangle} \quad (11)$$

$$= \frac{\int dL_{\text{H}\alpha,z} M_{\text{gas,S}}(L_{\text{H}\alpha,z}) R_{\text{Ia,S}}(L_{\text{H}\alpha,z}) \frac{dn}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} R_{\text{Ia,S}}(L_{\text{H}\alpha,z}) \frac{dn}{dL_{\text{H}\alpha,z}}}, \quad (12)$$

and  $\mathcal{R}_{\text{Ia,S}} \equiv \langle R_{\text{Ia,S}} n_{\text{galaxy,S}} \rangle$  is the cosmic Type Ia rate in star-forming galaxies, as shown in Figure 1. In a star-forming galaxy, the galaxy gas mass  $M_{\text{gas,S}}$  and the galaxy Type Ia rate  $R_{\text{Ia}}$  can be related to the star formation rate in that galaxy, which can be connected to the observable H $\alpha$  luminosity  $L_{\text{H}\alpha,z}$  of the galaxy by  $\psi(L_{\text{H}\alpha,z})/(1 M_{\odot} \text{ yr}^{-1}) = L_{\text{H}\alpha,z}/(1.26 \times 10^{34} \text{ W})$  (Hopkins 2004). Therefore, we express the gas mass  $M_{\text{gas,S}}$  and the Type Ia rate  $R_{\text{Ia}}$  in terms of  $L_{\text{H}\alpha,z}$ . The corresponding galaxy luminosity function at this wavelength can be expressed by the Schechter function (Nakamura et al. 2004).

At a specific redshift, the gas mass in star-forming galaxies  $M_{\text{gas,S}}$  and the star formation rate can be connected by

$$M_{\text{gas,S}} = 2.8 \times 10^9 M_{\odot} (1+z)^{-\beta} \left( \frac{\psi}{1 M_{\odot} \text{ yr}^{-1}} \right)^{\omega}, \quad (13)$$

with  $\beta = 0.571$  and  $\omega = 0.714$ , as shown in Fields et al. (2010). The Type Ia rate in a galaxy can be linked to the star formation rate via some delay-time distribution  $\Delta(\tau)$ ,

$$R_{\text{Ia}}(z) \propto \int_0^{t(z)} \psi(t-\tau) \Delta(\tau) d\tau, \quad (14)$$

where  $t(z)$  is the corresponding cosmic age at redshift  $z$ . The delay-time distribution  $\Delta(\tau)$  gives the probability that a Type Ia SN explodes a time  $\tau$  after the progenitor's birth. More detailed discussion about the delay-time distribution can be found in the Appendix. The galaxy luminosity function at a certain redshift for star-forming galaxies in the H $\alpha$  band can be presented in the form of a Schechter function of

$$\frac{dn}{dL_{\text{H}\alpha,z}} = \frac{n_{*,z}}{L_{*,z}} \left( \frac{L_{\text{H}\alpha,z}}{L_{*,z}} \right)^{-\alpha} e^{-L_{\text{H}\alpha,z}/L_{*,z}} \quad (15)$$

with  $\alpha = 1.43$  (Nakamura et al. 2004).

Because Type Ia SNe are delayed relative to star formation, the Type Ia rate in a galaxy depends on the star formation history of the galaxy via Equation (14). Unfortunately, this past star formation rate is not easily determined for distant galaxies even when the H $\alpha$  luminosity  $L_{\text{H}\alpha,z}$  is available to give the instantaneous star formation rate. However, we can investigate the evolution in two simplified cases: pure luminosity evolution and pure density evolution. Pure luminosity evolution assumes that galaxy luminosities evolve with redshift, while galaxy density stays unchanged, i.e.,  $L_{*,z}$  in Equation (15) has redshift dependence and  $n_{*,z}$  does not. Pure density evolution assumes that galaxy density evolves with redshift, while galaxy luminosity remains constant, i.e.,  $n_{*,z}$  in Equation (15) depends on redshift and  $L_{*,z}$  does not. The real situation should be bracketed by these possibilities.

In either limit, we can take advantage of the fact that the well-measured cosmic star formation rate is  $\dot{\rho}_{*} = \langle \psi n_{\text{gal}} \rangle \sim \langle L_{\text{H}\alpha} n_{\text{gal}} \rangle \sim L_{*,z} n_{*,z}$ . This fixes the redshift behavior of the product  $L_{*,z} n_{*,z}$ , so that in the limit where one factor is constant, the other must have the redshift dependence of the cosmic star formation rate.

#### 4.1. Pure Luminosity Evolution

In the case of pure luminosity evolution, there is no evolution of the galaxy density. Thus in the Schechter function of Equation (15),  $n_{*,z} = n_{*,0}$ , and thus all redshift dependence lies in  $L_{\text{H}\alpha,z}$ . Therefore, evolution of the star formation rate in each galaxy, and hence the evolution of the galaxy H $\alpha$  luminosity  $L_{\text{H}\alpha,z}$ , must trace the general evolution of the cosmic star formation rate  $\dot{\rho}_{*}$ . Under this assumption, we can show that  $\langle M_{\text{gas,S}} \rangle$  is independent of the choice of the delay-time function (see derivation in the Appendix). When adopting the Schechter function for  $dn_{\text{galaxy,S}}/dL_{\text{H}\alpha,z}$ , one will find that  $\langle M_{\text{gas,S}} \rangle \propto (1+z)^{-\beta} (L_{*,z})^{\omega} \propto (1+z)^{-\beta} (\dot{\rho}_{*}(z)/\dot{\rho}_{*}(z=0))^{\omega}$ , with a local value of  $\langle M_{\text{gas,S}} \rangle_{z=0} = 6.8 \times 10^9 M_{\odot}$  (see the Appendix).

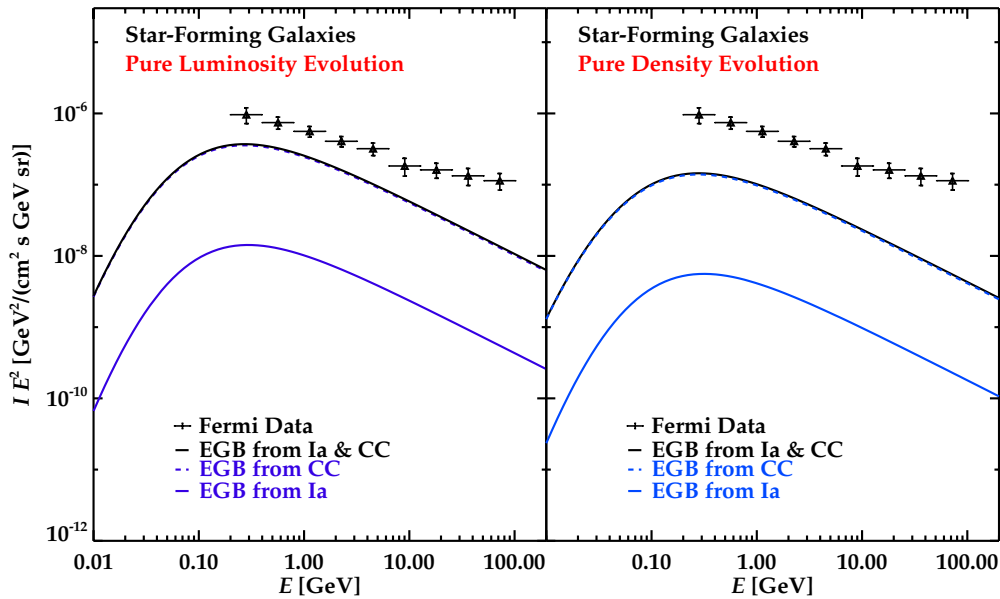
The predicted EGB from Type Ia SNe in star-forming galaxies is plotted as the solid blue line in the left panel of Figure 2. For comparison, the dashed blue line shows the EGB contribution from CC SNe in star-forming galaxies. The shapes of the dashed blue lines trace the results in Fields et al. (2010). However, the normalization of the CC SN curves is lower by the fraction of the CC SN rate over the total SN rate ( $\sim 0.8$  from Bazin et al. 2009), which is due to the fact that Fields et al. (2010) have implicitly assumed that CC SNe produce all of the gamma-ray emission in galaxies.

Figure 2 shows that the EGB from Type Ia SNe is around an order of magnitude lower than those from CC SNe, which is due to the lower Type Ia rate in star-forming galaxies. As noted above, this is easily understood as a reflection of the small Ia/CC ratio (Figure 1). The black curve in Figure 2 presents the total EGB emission from both Type Ia and CC SNe in star-forming galaxies. Note that the total EGB emission from star-forming galaxies turns out to be very similar to the prediction in Fields et al. (2010), in which the authors assumed that all of the EGB contribution comes from the CC events. The reason is that even though we added the EGB contribution from Type Ia SNe, we also lower the EGB emission from CC events estimated in Fields et al. (2010) by the corresponding CC SN fraction. Also, the Ia-to-CC fraction does not change much within  $z \sim 1$ , which is the redshift range where most of the EGB signals originate. Hence, the EGB contribution from CC SNe is always higher than those from Ia SNe by a similar factor.

The shape of the EGB curves in Figure 2 traces the general features of the pionic gamma-ray energy spectrum. This is because the observed EGB intensity at a specific energy originated from a combination of sources at different redshifts, as described in Equation (1). Therefore, the redshift evolution of the unresolved sources is smeared out in the energy plot and mostly affects the normalization of the EGB intensity but not the spectral shape.

#### 4.2. Pure Density Evolution

For pure density evolution, only the galaxy density evolves with redshift while the galaxy luminosity does not. Therefore, the star formation rate  $\psi$  in a galaxy also remains constant, and the evolution in the cosmic star formation rate will purely depend on the growth of the galaxy density. Hence, in the case of pure density evolution,  $L_{\text{H}\alpha,z+\Delta z} = L_{\text{H}\alpha,z}$ . With similar calculations as those in the case of pure luminosity evolution (the Appendix), one can find that  $\langle M_{\text{gas,S}} \rangle$  is also independent of the choice of the delay-time function. Additionally,  $\langle M_{\text{gas,S}} \rangle \propto (1+z)^{\beta}$  in the case of pure density evolution.



**Figure 2.** EGB from SNe in star-forming galaxies. Results in the left panel assume pure luminosity evolution. Results in the right panel assume pure density evolution. The dashed blue line shows the contribution from CC SNe; the solid blue line shows the contribution from Ia SNe; and the black line plots the total contribution from both CC and Ia SNe. The *Fermi* data are obtained from Abdo et al. (2009a).

(A color version of this figure is available in the online journal.)

Results for the case of pure density evolution are shown in the right panel of Figure 2. Again, the solid blue line and the dashed blue line represent the EGB from Type Ia and CC, respectively. The black line shows the combined gamma-ray contribution from both Type Ia and CC events. Similar to the results of pure luminosity evolution, the EGB from Type Ia SNe is lower than that from CC events because of the lower Type Ia rate. Moreover, the predicted EGB emission is lower if we assume pure density evolution instead of pure luminosity evolution. As discussed in Fields et al. (2010), this is because a typical galaxy’s gamma-ray luminosity  $L_\gamma \propto \psi M_{\text{gas}}$ ; in the pure luminosity evolution case, both factors are enhanced at early times, while in the pure density case this nonlinear boost is not present.

## 5. THE EXTRAGALACTIC GAMMA-RAY BACKGROUND FROM TYPE Ia SUPERNOVAE IN QUIESCENT GALAXIES

Following a similar procedure to Section 4, we will now discuss the EGB from cosmic rays accelerated by Type Ia SNe in quiescent galaxies. We again express the EGB luminosity density  $\mathcal{L}_{\gamma,Q}^{\text{Ia}}$  (Equation (9)) in the following form to describe the physics inputs from the average gas mass  $\langle M_{\text{gas},Q} \rangle$  and the cosmic Ia rate in quiescent galaxies  $\mathcal{R}_{\text{Ia},Q}$ ,

$$\mathcal{L}_{\gamma,Q}^{\text{Ia}} = \frac{\epsilon_Q \mathcal{R}_{\text{Ia},Q}}{\epsilon_{\text{MW}} R_{\text{Ia}}^{\text{MW}} + \epsilon_{\text{MW}} R_{\text{CC}}^{\text{MW}}} \Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{cm}}) \frac{X_{\text{H}}}{m_p} \langle M_{\text{gas},Q} \rangle, \quad (16)$$

where

$$\langle M_{\text{gas},Q} \rangle \equiv \frac{\langle M_{\text{gas},Q} R_{\text{Ia},Q} n_{\text{galaxy},Q} \rangle}{\langle R_{\text{Ia},Q} n_{\text{galaxy},Q} \rangle} \quad (17)$$

$$= \frac{\int dM_{\star,Q} M_{\text{gas},Q}(M_{\star,Q}, z) R_{\text{Ia},Q}(M_{\star,Q}, z) \frac{dn}{dM_{\star,Q}}}{\int dM_{\star,Q} R_{\text{Ia},Q}(M_{\star,Q}, z) \frac{dn}{dM_{\star,Q}}} \quad (18)$$

and  $\mathcal{R}_{\text{Ia},Q} \equiv \langle R_{\text{Ia},Q} n_{\text{galaxy},Q} \rangle$ . Unlike the star-forming galaxies, where both  $\langle M_{\text{gas},S} \rangle$  and  $\mathcal{R}_{\text{Ia},S}$  can be related to the observable  $\text{H}\alpha$  luminosity, it is easier to connect both  $\langle M_{\text{gas},Q} \rangle$  and  $\mathcal{R}_{\text{Ia},Q}$  to the total stellar mass  $M_{\star,Q}$  in a quiescent galaxy.

For the cosmic Type Ia rate in quiescent galaxies, we adopt the results of Sullivan et al. (2006), which link Type Ia rates to  $M_{\star,Q}$  directly. These authors assume a bimodal delay-time distribution and decompose the Ia rate into two groups: the long-delay time and short-delay time. In their model, the short-delay time group simply traces the star formation rate, while the long-delay time group has a constant probability for all delay times, i.e.,  $\Delta(\tau) = \text{constant}$ . Therefore, the Type Ia rate in a galaxy can be written as

$$R_{\text{Ia}} = A M_{\star,Q} + B \psi. \quad (19)$$

The star formation rate  $\psi \sim 0$  in a quiescent galaxy, thus  $R_{\text{Ia},Q} = A M_{\star,Q}$ , where  $M_{\star,Q}$  is the total stellar mass created throughout the star formation history in the quiescent galaxy. Sullivan et al. (2006) estimated  $A = 5.1 \times 10^{-14} \text{ yr}^{-1} M_{\odot}^{-1}$  in quiescent galaxies based on measurements of the Type Ia rate in the Supernova Legacy Survey.

According to the observational results in Pannella et al. (2009), the stellar-mass function  $dn/dM_{\star,Q}$  of early-type galaxies evolves only slightly with redshift. Therefore, we simply assume the same stellar-mass function throughout all redshift. Also, we find that the  $dn/dM_{\star,Q}$  shown in Pannella et al. (2009) can be roughly fitted by the following function,<sup>4</sup>

$$\frac{dn}{d(\log_{10} M_{\star,Q})} = C_m \exp\left(-\frac{\log_{10}^2(M_{\star,Q}/\mu)}{\sigma_m^2}\right), \quad (20)$$

<sup>4</sup> This fitting function is based on observations given in Figure 7 in Pannella et al. (2009), which contains measurements of stellar-mass functions at different redshift bins and environments. We choose the data set in the lowest redshift bin of  $0.25 < z < 0.55$  in medium-dense environment ( $\log_{10} \rho \sim -2.75$ ; see Pannella et al. 2009 for the definition of environmental density  $\rho$  and more details) to perform a  $\chi^2$  fitting. The reduced- $\chi^2$  of our fitting function is  $\sim 0.22$ .

**Table 1**  
Summary of Different Gas Models Adopted in the EGB Calculations

Gas Model	$M_{\text{gas,Q}}/M_{\star,\text{Q}}$	$\langle M_{\text{gas,Q}} \rangle$	Reference
1	2.14	$1.11 \times 10^{12} M_{\odot}$	Jiang & Kochanek (2007)
2	0.01	$5.17 \times 10^9 M_{\odot}$	David et al. (2006)
3	0.001	$5.17 \times 10^8 M_{\odot}$	David et al. (2006)

where  $C_m = 2.05 \times 10^{-3} \text{ Mpc}^{-3} \log^{-1} M_{\odot}$ ,  $\mu = 10^{10.7} M_{\odot}$ , and  $\sigma_m = 0.77$ . Equation (20) (the stellar-mass function for quiescent galaxies) and Equation (19) (Type Ia rate in a quiescent galaxy) give the cosmic Ia rate in quiescent galaxies

$$\begin{aligned} \mathcal{R}_{\text{Ia,Q}} &= \int dM_{\star,\text{Q}} R_{\text{Ia,Q}} \frac{dn}{dM_{\star,\text{Q}}} \\ &= 1.53 \times 10^{-5} \text{ yr}^{-1} \text{ Mpc}^{-3}. \end{aligned}$$

Here, the constant rate follows from the nearly redshift-independent quiescent stellar-mass function.

Most of the gas content in quiescent galaxies appears to be in the form of diffuse hot gas and can be observed in the X-ray (e.g., Forman et al. 1985; Canizares et al. 1987; Bregman et al. 1992). However, large uncertainties exist in estimations of the mass of hot gas. Some studies suggest that most of the quiescent galaxies are gas-poor (e.g., David et al. 2006; Fukazawa et al. 2006), while other studies imply that there can be significant amount of gas in these galaxies (e.g., Jiang & Kochanek 2007; Humphrey et al. 2011). Current theoretical models suggest that the gas could extend out to a few hundred kiloparsecs from the center. The total gas mass of a single galaxy can increase by orders of magnitude if one includes the gas at large radii (Humphrey & Buote 2010; Humphrey et al. 2011). Therefore, observational measures of gas mass can vary even for a single galaxy, depending on whether or not the observations enclose a large enough radius to include gas at large distances. If hot gas extends to large radii, this could serve as a reservoir of targets for cosmic rays accelerated by Type Ia SNe, provided the cosmic rays also reach large radii. This too is uncertain, and will depend on the cosmic-ray confinement versus escape properties of these galaxies.

Because of the large uncertainties in the gas content in quiescent galaxies, we illustrate a range of EGB predictions for these objects, based on three different gas amounts. Since quiescent galaxies are dominantly early-type, we will use estimates of the gas mass in early-type galaxies for the amount of gas in quiescent galaxies. The stellar-mass function in Pannella et al. (2009; Equation (20)) gives the average stellar mass in early-type galaxies to be  $\langle M_{\star,\text{Q}} \rangle = 5.17 \times 10^{11} M_{\odot}$ , which can be converted to the total gas mass by multiplying a gas-to-stellar-mass ratio  $M_{\text{gas}}/M_{\star}$ , i.e.,  $\langle M_{\text{gas,Q}} \rangle = (M_{\text{gas,Q}}/M_{\star,\text{Q}}) \langle M_{\star,\text{Q}} \rangle$ . The three models we adopted for different gas amounts correspond to different gas-to-stellar-mass ratios  $M_{\text{gas,Q}}/M_{\star,\text{Q}}$  for early-type galaxies. Table 1 summarizes the gas-to-stellar-mass ratios  $M_{\text{gas,Q}}/M_{\star,\text{Q}}$  for the three models we adopted, as well as the corresponding  $\langle M_{\text{gas,Q}} \rangle$ . Gas Model 1 estimates the gas-to-stellar-mass ratio based on the stellar-mass fraction of the total halo mass from Jiang & Kochanek (2007).<sup>5</sup> This model gives

<sup>5</sup> Jiang & Kochanek (2007) found that the average stellar-mass fraction of the total halo mass in early-type galaxies is  $M_{\star}/M_{\text{tot}} \sim 0.026$  or  $0.056$  based on different assumptions of the halo mass dynamics. Both of these numbers are significantly lower than the cosmological baryon-to-mass ratio  $\Omega_b/\Omega_m \sim 0.176$  measured by WMAP (Spergel et al. 2007). If we assume that the baryon-to-mass ratio in a galaxy can be well represented by the cosmological ratio, i.e.,  $M_b/M_{\text{tot}} \sim \Omega_b/\Omega_m$ , the result from Jiang & Kochanek (2007) implies a large amount of gas mass in early-type galaxies,

the highest gas-to-stellar-mass ratio of all three models. Gas Model 2 and 3 are both adopted from David et al. (2006), in which the authors reported the gas-to-stellar-mass ratio for more luminous (Gas Model 2) and less luminous (Gas Model 3) early-type galaxies. Note that both of the gas mass and the Ia rate in a quiescent galaxy are constant with redshift, as a result of assuming a non-evolving stellar-mass function, consistent with the early-type galaxy observations in Pannella et al. (2009).

The red curves in Figure 3 plot the EGB estimation from Type Ia SNe in quiescent galaxies, with different line styles correspond to estimations from different gas amounts (solid line: Gas Model 1, dashed line: Gas Model 2, dotted line: Gas Model 3). The EGB emissions from SNe in star-forming galaxies are plotted as blue curves for comparison. The black curves in Figure 4 plot the total EGB emissions from SNe in both star-forming and quiescent galaxies for different gas models. For both Figures 3 and 4, the left panel plots results under the assumption of pure luminosity evolution for the star-forming galaxies. The right panel shows the EGB predictions assuming pure density evolution for the quiescent galaxies.

The estimated EGBs shown in Figure 3 are linearly proportional to the average galaxy gas mass  $\langle M_{\text{gas,Q}} \rangle$  and thus to the adopted gas-to-stellar-mass ratio, as required by Equation (16). Gas Model 1 predicts the highest contribution in EGB from quiescent galaxies, where the result is significantly higher than the EGB emission from Type Ia events in star-forming galaxies, while Gas Model 2 and Gas Model 3 suggest much lower EGB emission from quiescent galaxies. In our estimation, the two important factors that affect the overall EGB are the average gas mass and the cosmic SN rate. In general, the cosmic Type Ia rate is about a factor of 5–10 smaller than the cosmic CC SN rate. Additionally, the cosmic Type Ia rate in all quiescent galaxies averaging over the entire redshift range is lower than that in star-forming galaxies by around a factor of three.

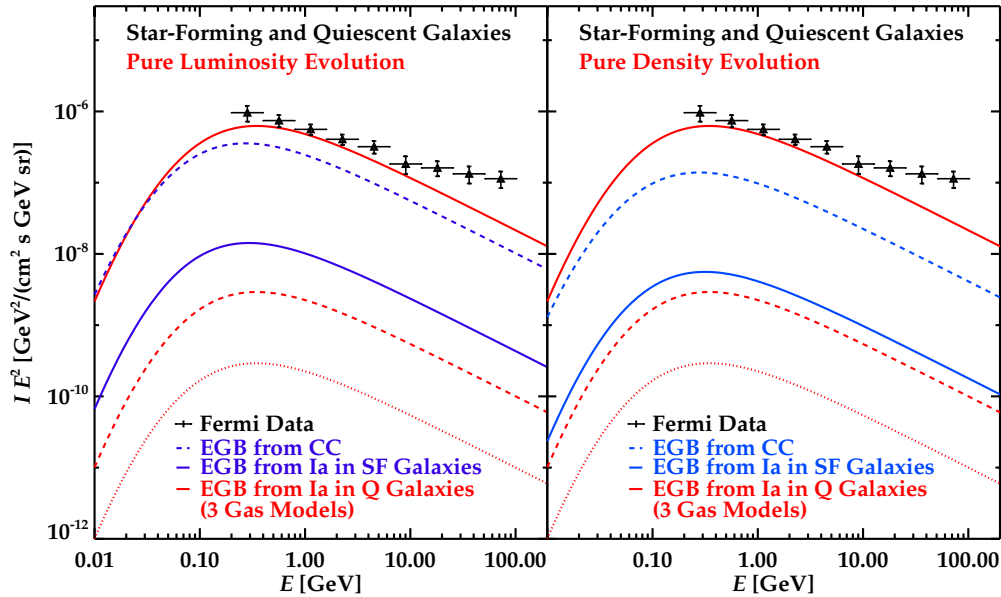
As for the gas mass in quiescent galaxies, Gas Model 1 assumes the gas amount to be about two orders of magnitude higher than that in star-forming galaxies, while Gas Model 2 and 3 assume gas amount to be similar or one order of magnitude lower than that in star-forming galaxies, respectively. Combining these two factors (gas mass and Type Ia rate), we would expect the EGB from quiescent galaxies to be about 30 times larger (for Gas Model 1), 3 times smaller (for Gas Model 2), or 30 times smaller (for Gas Model 3) than that from Type Ia in star-forming galaxies. Because of the EGB estimation is very sensitive to the gas amount, measurement of the EGB could put constraints on the gas mass in quiescent galaxies.

## 6. THE UNCERTAINTIES IN THE EXTRAGALACTIC GAMMA-RAY BACKGROUND ANALYSIS

### 6.1. Star-forming Galaxies

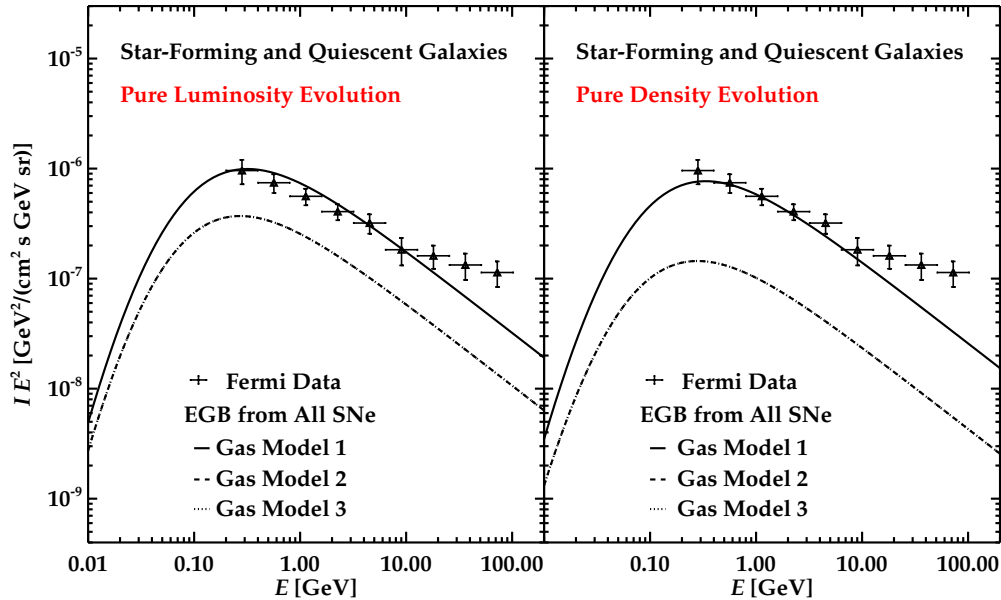
The gamma-ray emission from normal star-forming galaxies is the most constrained among the three galaxy classes that are considered possible SN-induced EGB sources (i.e., starburst galaxies, normal star-forming galaxies, and quiescent galaxies). The main uncertainties in the EGB prediction of star-forming galaxies come from four factors, as described in Fields et al. (2010): (1) uncertainty in the pionic gamma-ray production

which can be estimated by  $M_{\text{gas,Q}} = (M_{\text{baryon,Q}} - M_{\star,\text{Q}}) \sim M_{\star,\text{Q}} ((\Omega_b/\Omega_m)/(M_{\star}/M_{\text{tot}}) - 1)$ . The values of  $M_{\star}/M_{\text{tot}} \sim 0.026$  and  $0.056$  correspond to  $M_{\text{gas,Q}} = 5.77 M_{\star,\text{Q}}$  and  $M_{\text{gas,Q}} = 2.14 M_{\star,\text{Q}}$ , respectively. Here, we adopt the latter number to be more conservative in our estimation.



**Figure 3.** EGB from SNe in both star-forming and quiescent galaxies. Results in the left panel assume pure luminosity evolution for star-forming galaxies. Results in the right panel assume pure density evolution for star-forming galaxies. The dashed blue line shows the contribution from CC SNe; the solid blue line shows the contribution from Ia SNe in star-forming galaxies; the red lines show the contribution from Ia SNe in quiescent galaxies based on different gas models (solid red: Gas Model 1, dashed red: Gas Model 2, dotted red: Gas Model 3). The *Fermi* data are obtained from Abdo et al. (2009a).

(A color version of this figure is available in the online journal.)



**Figure 4.** Total EGB from Ia and CC SNe in both star-forming and quiescent galaxies. Results in the left panel assume pure luminosity evolution. Results in the right panel assume pure density evolution. Note that the lines for Gas Models 2 and 3 appear to overlap due to small difference. The *Fermi* data are obtained from Abdo et al. (2009a).

(A color version of this figure is available in the online journal.)

rate  $\Gamma_{\pi^0 \rightarrow \gamma\gamma}^{\text{MW}}(E_{\text{em}})$ , which is  $\sim 30\%$  (Abdo et al. 2009c), (2) uncertainty in the normalization of the Galactic SN rate  $R_{\text{SN}}^{\text{MW}}$ , which is  $\sim 40\%$  (Robitaille & Whitney 2010), (3) uncertainty in the luminosity scaling in  $\langle M_{\text{gas,S}} \rangle$ , which is  $\sim 25\%$  (Fields et al. 2010), and (4) uncertainty in the normalization of the cosmic SN rate  $\mathcal{R}_{\text{SN,S}}$ , which is  $\sim 16\%$  resulting from the uncertainties in the cosmic CC SN rate  $\mathcal{R}_{\text{CC}} \sim (1.0 \pm 0.2) \times 10^{-4} \text{ yr}^{-1} \text{ Mpc}^{-3}$  (Horiuchi et al. 2009) and the cosmic Ia rate  $\mathcal{R}_{\text{Ia}} \sim (0.25 \pm 0.05) \times 10^{-4} \text{ yr}^{-1} \text{ Mpc}^{-3}$  (Horiuchi & Beacom 2010). The total uncertainty in the EGB prediction will then be  $\sim 10^{\pm 0.25}$ .

The upcoming large synoptic surveys, such as the LSST, will provide novel information in both the cosmic SN rate and how they depend on the galaxy types out to high redshift. Within one year of observation, LSST is expected to detect  $\sim 10^5$  SNe out to  $z \sim 1$  and thus achieves a statistical precision of less than a few percent in the cosmic SN rate (Lien & Fields 2009; Bailey et al. 2009). Hence, LSST will essentially remove the uncertainty from the cosmic SN rate in the EGB analysis and make the EGB a better tool for studying cosmic rays and gamma-ray physics. Moreover, such a large SN population will provide excellent statistics for study of how SN rates evolve as a function of SN



type (and sub-type), host galaxy type and star formation rate, and cosmic environment. Thus, it will be possible to directly measure the Type Ia rate in quiescent galaxies and its evolution with redshift.

### 6.2. Quiescent Galaxies: Hot Gas and Cosmic-Ray Propagation

For quiescent galaxies, many characteristics related to their gamma-ray emissions are poorly understood. The Type Ia SN rate in these systems could be uncertain up to a factor  $\sim 2$ , particularly at  $z > 1$ . We have also seen that the gas mass in these systems is even more poorly known. Published estimates of the gas content in quiescent galaxies vary by orders of magnitude. Observations that use X-rays as tracers of hot gas found significantly less gas in quiescent galaxies (e.g., David et al. 2006; Fukazawa et al. 2006). However, several studies imply a much higher gas content in quiescent galaxies than previously thought, when using gravitational lensing and modeling that involved dark matter (e.g., Jiang & Kochanek 2007; Capelo et al. 2010; Humphrey et al. 2011). It is difficult to determine the causes of the large discrepancy of gas quantity from different analyses, because these studies adopted different observational and modeling techniques with different galaxy samples. One possible reason for the large variation in gas content measurements might come from whether or not one includes gas at larger radii, which are predicted by some theoretical models (Capelo et al. 2010; Humphrey & Buote 2010; Humphrey et al. 2011).

If gas content does extend to larger radii in quiescent galaxies, it is crucial to understand the cosmic-ray propagation in quiescent galaxies to determine the confinement volume of cosmic rays and how likely they can interact with gas at larger radii. Unfortunately, cosmic-ray propagation remains poorly understood. Until now, most of the studies have been focused on the Milky Way or spiral galaxies and not so much on quiescent galaxies. For spiral galaxies, both observations and theoretical modeling suggest that most of the cosmic rays are confined within  $\sim$  kpc of the disk (Stecker & Jones 1977; Strong et al. 2000, 2004). However, this might not be the case for quiescent galaxies. Hein & Spanier (2008) simulate cosmic-ray propagation in elliptical galaxies with the presence of diffusion, as well as adiabatic losses. They apply their formalism not to SN sources but rather to acceleration due to an M87-like relativistic jet; thus their detailed calculations are not applicable to our case. Nevertheless, their general finding is that cosmic rays expand into a larger volume in an elliptical galaxy than in a spiral galaxy, due to the larger minor axis in an elliptical galaxy. Additionally, they argue that adiabatic losses are much more important in elliptical galaxies and indeed dominate over escape losses. Hein & Spanier (2008) thus conclude that it is likely for elliptical galaxies to be extended gamma-ray sources.

There are two factors that are important for determining the probability of interactions between cosmic rays and gas, especially at large radii where the density of gas and cosmic rays are likely to be smaller: (1) the mean free time for pion production for each cosmic-ray particle  $\tau_{pp \rightarrow \pi^0} = (n_{\text{gas}} \sigma_{pp \rightarrow \pi^0} c)^{-1} \sim 1 \text{ Gyr} (0.1 \text{ cm}^2/n_{\text{gas}})$ , where  $\sigma_{pp \rightarrow \pi^0}$  is the cross section of pion production and  $n_{\text{gas}}$  is the number density of gas particles, and (2) time  $\tau_{\text{esc}}$  that a cosmic-ray particle takes to propagate through the galaxy before escape. In the limit of cosmic rays travel through a (non-magnetized) galaxy radially, that is, without any diffusion, the escape time is very short and probability of interactions between cosmic rays and gas particles is small.

On the other hand, in the presence of disordered magnetic fields extending to large radii, cosmic-ray propagation will not be radial but diffusive instead, which will make the escape time much larger and increase the chance of cosmic-ray interactions with ISM.

Clearly there are fundamental uncertainties (and opportunities) in a realistic treatment of elliptical galaxy cosmic rays, but even in our simplistic picture the parameters  $\Lambda_{\text{esc}}$  and  $\epsilon_Q$  are not well constrained. Although we treated these two quantities to be the same for both Type Ia and CC SNe in all environments due to limited knowledge, it is possible, and even likely, that these numbers are different in quiescent galaxies. In fact, Dorfi & Voelk (1996) have suggested that the efficiency in quiescent galaxies is at least 10 times lower than that in star-forming galaxies (Dorfi & Voelk 1996), which could lower our prediction of the EGB from quiescent galaxies by a factor of 10 or even larger. Tang & Wang (2005) model the evolution of SN remnants in low-density hot media and reach similar conclusion that the SN heating in such an environment is subtle and cover a large region because of small Mach numbers. Likewise, a smaller escape path length, i.e., a weaker cosmic-ray confinement, can also decrease our EGB estimation in quiescent galaxies. Note that adopting different values of  $\epsilon$  and  $\Lambda_{\text{esc}}$  would change the cosmic-ray spectrum, and hence also change the corresponding gamma-ray spectrum.

To summarize, current studies imply that cosmic-ray acceleration might be more difficult in quiescent galaxies than in star-forming galaxies due to weaker shocks in low-density and high-temperature environments (Dorfi & Voelk 1996; Tang & Wang 2005). However, quiescent galaxies might have larger confinement volume than spiral galaxies because they have larger semiminor radii (Hein & Spanier 2008). Further observational and theoretical study of the gas and cosmic-ray content of quiescent galaxies clearly are needed in order to pin down the gamma-ray production of these objects even to within an order of magnitude.

## 7. CONCLUSIONS

We have calculated the EGB contribution from Type Ia SNe in both star-forming and quiescent galaxies, extending the work of Fields et al. (2010). For star-forming galaxies, most of the gamma-ray emission comes from cosmic rays accelerated by CC SNe. This is mainly because there are about five times more CC SNe than Type Ia events in star-forming galaxies. We find that the net EGB contribution from both SN types is almost the same as the Fields et al. (2010) predictions that only included CC events. Our model allows for addition of cosmic Type Ia explosions, but also includes these in the cosmic ray/star formation ratio, which we normalize to the Milky Way values. Both factors change by nearly the same amount, so that the addition of Type Ia events causes almost no net change in the EGB prediction.

We also point out that Type Ia events in quiescent galaxies make a unique contribution to the EGB, because these systems lack CC events. We show that the EGB from Type Ia events in quiescent galaxies is highly sensitive to the gas amount in quiescent galaxies, which is still poorly known. Based on different gas models adopted, the EGB from Type Ia SNe in quiescent galaxies can vary from two orders of magnitudes higher to an order of magnitude lower than those produced by Type Ia SNe in star-forming galaxies. Therefore, quiescent galaxies can be a dominant source of the EGB if there exists a large amount of gas, as suggested by Jiang & Kochanek (2007)

and Humphrey et al. (2011). The measurement of the EGB will provide a useful constraint on the gas amount in quiescent galaxies. Additional uncertainties in the cosmic-ray acceleration efficiency and confinement could also change the EGB emission in these systems by a few orders of magnitude. Hence, the EGB can also provide limits on these two quantities in quiescent galaxies.

It is thus important to understand the characteristics of cosmic SNe of all types, in order to correctly predict their contribution to the EGB. We conclude that the large SN sample provided by LSST will offer critical information about the cosmic SN rate for both CC and Ia events, and their dependence on galaxy types out to high redshift.

The *Fermi* detection of the EGB contains crucial information about the extragalactic gamma-ray source spectrum. Particularly, it can provide an important probe to the gas amount, the cosmic-ray acceleration efficiency, and the cosmic-ray confinement in quiescent galaxies. With our knowledge about SNe increasing rapidly as future synoptic surveys come online, the EGB contribution from SNe in galaxies can possibly be disentangled from other source candidates.

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## APPENDIX

### THE DELAY-TIME DISTRIBUTION OF TYPE Ia SUPERNOVAE AND DETAILED CALCULATION OF $\langle m_{\text{gas,S}} \rangle$ IN EQUATION (10)

The delay time of each Type Ia SN can differ from  $\sim 0.1$  Gyr to  $\sim 10$  Gyr (Mannucci et al. 2005; Scannapieco & Bildsten 2005; Gal-Yam & Maoz 2004; Mannucci et al. 2006; Sullivan et al. 2006; Maoz et al. 2011). Observationally, the delay times of Type Ia SNe are usually studied via comparison between measurements of the cosmic Type Ia SN rate and the cosmic star formation rate, and are usually described by some functions of delay-time distribution, which describes the probability of a Type Ia event with a specific delay time. Current proposed delay-time distributions have included a single power law (e.g., Horiuchi & Beacom 2010; Graur et al. 2011), a Gaussian (e.g., Strolger et al. 2004; Dahlen et al. 2008), and a bimodal distribution (e.g., Sullivan et al. 2006). The difficulty in determining the delay-time distribution mainly comes from the uncertainty in the cosmic Ia SN rate measurements. Fortunately, the value  $\langle M_{\text{gas,S}} \rangle$  is independent of the choice of delay-time distribution, as we show in the following derivation.

Based on the relation between the gas mass  $M_{\text{gas,S}}$  and the star formation rate  $\psi$  (Equation (13)), and also the connection between  $\psi$  and  $L_{\text{H}\alpha,z}$ , i.e.,  $\psi(L_{\text{H}\alpha,z})/(1 M_{\odot} \text{ yr}^{-1}) = L_{\text{H}\alpha,z}/(1.26 \times 10^{34} \text{ W})$ , the  $M_{\text{gas,S}}$  for a galaxy at redshift  $z$  can be directly linked to the observable H $\alpha$  luminosity  $L_{\text{H}\alpha,z}$  by  $M_{\text{gas,S}} = 2.8 \times 10^9 M_{\odot} (1+z)^{-\beta} (L_{\text{H}\alpha,z}/1.26 \times 10^{34} \text{ W})^{\omega}$ .

Additionally, the Type Ia rate can also be related to  $L_{\text{H}\alpha,z}$  by

$$R_{\text{Ia,S}} \propto \int_0^t L_{\text{H}\alpha}(t-\tau)\Delta(\tau) d\tau, \quad (\text{A1})$$

where  $L_{\text{H}\alpha}(t-\tau) \equiv L_{\text{H}\alpha,z+\Delta z}(t,\tau)$ , which is the H $\alpha$  luminosity measured at some earlier time  $t-\tau$  or larger redshift  $z+\Delta z$ . Therefore,  $\langle M_{\text{gas,S}} \rangle$  can be expressed in terms of  $L_{\text{H}\alpha,z}$ ,

$$\langle M_{\text{gas,S}} \rangle \propto \frac{\int dL_{\text{H}\alpha,z} (1+z)^{-\beta} (L_{\text{H}\alpha,z})^{\omega} \left( \int_0^t L_{\text{H}\alpha,z+\Delta z}(t,\tau)\Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} \left( \int_0^t L_{\text{H}\alpha,z+\Delta z}(t,\tau)\Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}. \quad (\text{A2})$$

This equation expresses only the redshift-dependent terms and we will further calculate how  $\langle M_{\text{gas,S}} \rangle$  evolves with redshift in the case of pure luminosity evolution and pure density evolution, respectively, in Appendices A.1 and A.2. Fields et al. (2010) show that the local value of  $\langle M_{\text{gas,S}} \rangle_{z=0} = 6.8 \times 10^9 M_{\odot}$ .

#### A.1. Pure Luminosity Evolution

In the case of pure luminosity evolution, the star formation rate in each galaxy traces the general evolution of the cosmic star formation rate, i.e.,  $\psi(z+\Delta z)/\psi(z) = \dot{\rho}_{\star}(z+\Delta z)/\dot{\rho}_{\star}(z)$ . Therefore, from the directly proportional relation between the star formation rate  $\psi$  in a galaxy and the galaxy H $\alpha$  luminosity  $L_{\text{H}\alpha,z}$ , one can trace the evolution of the H $\alpha$  luminosity via the history of cosmic star formation rate, which is well known out to redshift  $z \sim 1$  (e.g., Hopkins 2004; Hopkins & Beacom 2006, and references therein). That is,  $L_{\text{H}\alpha,z+\Delta z}/L_{\text{H}\alpha,z} = \psi(z+\Delta z)/\psi(z) = \dot{\rho}_{\star}(z+\Delta z)/\dot{\rho}_{\star}(z)$ . Therefore, the galaxy luminosity at different redshifts can be found by

$$L_{\text{H}\alpha,z+\Delta z} = L_{\text{H}\alpha,z} \frac{\dot{\rho}_{\star}(z+\Delta z)}{\dot{\rho}_{\star}(z)} \equiv L_{\text{H}\alpha,z} \frac{\dot{\rho}_{\star}(t-\tau)}{\dot{\rho}_{\star}(t)}. \quad (\text{A3})$$

With this relation,  $\langle M_{\text{gas,S}} \rangle$  in Equation (A2) can be simplified to

$$\langle M_{\text{gas,S}} \rangle \propto \frac{\int dL_{\text{H}\alpha,z} (1+z)^{-\beta} (L_{\text{H}\alpha,z})^{\omega} \left( \int_0^t L_{\text{H}\alpha,z} \frac{\dot{\rho}_{\star}(t-\tau)}{\dot{\rho}_{\star}(t)} \Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} \left( \int_0^t L_{\text{H}\alpha,z} \frac{\dot{\rho}_{\star}(t-\tau)}{\dot{\rho}_{\star}(t)} \Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}. \quad (\text{A4})$$

$$= \frac{(1+z)^{-\beta} \left( \int_0^t \frac{\dot{\rho}_{\star}(t-\tau)}{\dot{\rho}_{\star}(t)} \Delta(\tau) d\tau \right) \int dL_{\text{H}\alpha,z} (L_{\text{H}\alpha,z})^{\omega+1} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\left( \int_0^t \frac{\dot{\rho}_{\star}(t-\tau)}{\dot{\rho}_{\star}(t)} \Delta(\tau) d\tau \right) \int dL_{\text{H}\alpha,z} L_{\text{H}\alpha,z} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}. \quad (\text{A5})$$

$$= \frac{(1+z)^{-\beta} \int dL_{\text{H}\alpha,z} (L_{\text{H}\alpha,z})^{\omega+1} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} L_{\text{H}\alpha,z} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}. \quad (\text{A6})$$

Therefore  $\langle M_{\text{gas,S}} \rangle$  is independent of the choice of delay-time distribution.

The assumption of pure luminosity evolution implies that  $n_{\star,z}$  in the Schechter function remains constant and  $L_{\star,z}$  in the Schechter function evolves as  $\dot{\rho}_{\star}$  (Equation (A3)). Hence the

redshift dependence of  $\langle M_{\text{gas,S}} \rangle$  can be further calculated using the Schechter function,

$$\langle M_{\text{gas,S}} \rangle \propto (1+z)^{-\beta} L_{\star,z}^{\omega} \times \frac{\int^{L_{\text{max}}} d\left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right) \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{\omega+1} \frac{n_{\star,z}}{L_{\star,z}} \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{-\alpha} e^{-L_{\text{H}\alpha,z}/L_{\star,z}}}{\int^{L_{\text{max}}} d\left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right) \frac{L_{\text{H}\alpha,z}}{L_{\star,z}} \frac{n_{\star,z}}{L_{\star,z}} \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{-\alpha} e^{-L_{\text{H}\alpha,z}/L_{\star,z}}} \quad (\text{A7})$$

$$= (1+z)^{-\beta} L_{\star,z=0}^{\omega} \left( \frac{\dot{\rho}_{\star}(z)}{\dot{\rho}_{\star}(z=0)} \right)^{\omega} \times \frac{\int^{L_{\text{max}}} d\left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right) \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{\omega+1} \frac{n_{\star,z}}{L_{\star,z}} \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{-\alpha} e^{-L_{\text{H}\alpha,z}/L_{\star,z}}}{\int^{L_{\text{max}}} d\left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right) \frac{L_{\text{H}\alpha,z}}{L_{\star,z}} \frac{n_{\star,z}}{L_{\star,z}} \left(\frac{L_{\text{H}\alpha,z}}{L_{\star,z}}\right)^{-\alpha} e^{-L_{\text{H}\alpha,z}/L_{\star,z}}} \quad (\text{A8})$$

$$\propto (1+z)^{-\beta} \left( \frac{\dot{\rho}_{\star}(z)}{\dot{\rho}_{\star}(z=0)} \right)^{\omega}, \quad (\text{A9})$$

where  $L_{\text{max}}$  is the maximum luminosity for star-forming galaxies, which corresponds to the maximum star formation defined in Fields et al. (2010). Galaxies with luminosities greater than  $L_{\text{max}}$  are considered starburst galaxies and are not included in this calculation. Additionally, we adopt the cosmic star formation rate  $\dot{\rho}_{\star}$  described in Horiuchi et al. (2009) based on current observations. Note that because the factors related to delay-time distribution canceled out, this result turns out to be the same as the one obtained in Fields et al. (2010).

### A.2. Pure Density Evolution

In the case of pure density evolution  $L_{\text{H}\alpha,z+\Delta z} = L_{\text{H}\alpha,z}$  as discussed in Section 4.2. Thus in the Schechter function,  $L_{\star,z}$  remains constant while  $n_{\star,z}$  evolves as  $\dot{\rho}_{\star}$ . With similar calculations shown in the case of pure luminosity evolution (Appendix A.1) and adopting the Schechter function for  $dn_{\text{galaxy,S}}/dL_{\text{H}\alpha,z}$ , we can derive the redshift evolution of  $\langle M_{\text{gas,S}} \rangle$  in the case of pure density evolution:

$$\langle M_{\text{gas,S}} \rangle \propto \frac{\int dL_{\text{H}\alpha,z} (1+z)^{-\beta} (L_{\text{H}\alpha,z})^{\omega} \left( \int_0^t L_{\text{H}\alpha,z} \Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} \left( \int_0^t L_{\text{H}\alpha,z} \Delta(\tau) d\tau \right) \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}} \quad (\text{A10})$$

$$= \frac{(1+z)^{-\beta} \left( \int_0^t \Delta(\tau) d\tau \right) \int dL_{\text{H}\alpha,z} (L_{\text{H}\alpha,z})^{\omega+1} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\left( \int_0^t \Delta(\tau) d\tau \right) \int dL_{\text{H}\alpha,z} L_{\text{H}\alpha,z} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}} \quad (\text{A11})$$

$$= \frac{(1+z)^{-\beta} \int dL_{\text{H}\alpha,z} (L_{\text{H}\alpha,z})^{\omega+1} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}}{\int dL_{\text{H}\alpha,z} L_{\text{H}\alpha,z} \frac{dn_{\text{galaxy,S}}}{dL_{\text{H}\alpha,z}}} \quad (\text{A12})$$

$$\propto (1+z)^{-\beta}. \quad (\text{A13})$$

Again, because  $\langle M_{\text{gas,S}} \rangle$  is independent of the choice of delay-time distribution, the result is identical to the one calculated in Fields et al. (2010).

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